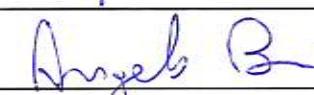
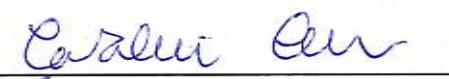
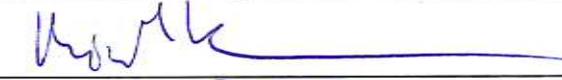


TEQ - Kick off Meeting

Name and Surname	Institution	Signature
James Bain	M2	
Peter Barker	UCL	
Angelo Bassi	UniTs	
Max Bazzi	INFN	
Matteo Carlesso	UniTs	
Catalina Curceanu	INFN	
Luca De Trizio	TUD	
Michael Drewsen	AU	
Alessandro Ferraro	QUB	
Giulio Gasbarri	UniTs	

Oussama Houhou	QUB	Oussama Houhou
Marta Marchese	QUB	Marta Marchese
Mauro Paternostro	QUB	Mauro Paternostro
Antonio Pontin	UCL	Antonio Pontin
Anishur Rahman	UCL	Anishur Rahman
Muddassar Rashid	UoS	Muddassar Rashid
Ashley Setter	UoS	Ashley Setter
Christopher Timberlake	UoS	Christopher Timberlake
Hendrik Ulbricht	UoS	Hendrik Ulbricht
Andrea Vinante	UoS	Andrea Vinante
MARKO TROŠ	UoS	Marko Troš
Thomas Penny	UCL	Thomas Penny
GIULIO GASBARRO	UNTS	Giulio Gasbarri
CN		



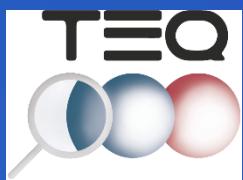
Testing the large-scale
limit of
quantum mechanics

Design and Realization of the TEQ experiment – Southampton, June 22nd, 2018

Southampton, June 22nd, 2018

Andrea Vinante

Preparing for the TEQ experiment at Southampton



University of Southampton, UK



Some questions about TEQ experiment

- What is the optimal size of the nanoparticle in order to do relevant (noninterferometric) tests of collapse models ?
- We want/need very low pressure ($P < 1E-10$ mbar) & very low temperature ($T < 1$ K)
Can we ever cool a levitated nanoparticle in such conditions?
- Can we keep the particle cold when doing measurements?
Could a stroboscopic measurement strategy work?

Continuous Spontaneous Localization (CSL)

Schrödinger equation + Stochastic term (collapse noise field)

$$d|\psi_t\rangle = \left[-\frac{i}{\hbar} H dt + \boxed{\sqrt{\lambda} \int d^3x (N(\mathbf{x}) - \langle N(\mathbf{x}) \rangle_t) dW_t(\mathbf{x}) - \frac{\lambda}{2} \int d^3x (N(\mathbf{x}) - \langle N(\mathbf{x}) \rangle_t)^2 dt} \right] |\psi_t\rangle$$

2 phenomenological constants (free parameters)

- Correlation Length r_C
(N = number density of nucleons, “smeared” over r_C)
conventional “literature value” $r_C = 10^{-7}$ m

- Collapse rate λ

Lower bounds (to guarantee collapse at “macroscopic” or “mesoscopic” scale)

$\lambda \sim 10^{-16} \text{ s}^{-1}$ @ $r_C = 10^{-7}$ m following Ghirardi, Rimini, Weber (GRW)

$\lambda \sim 10^{-8} \text{ s}^{-1}$ @ $r_C = 10^{-7}$ m following Adler

Measurable effects

1) Collapse of massive quantum superpositions

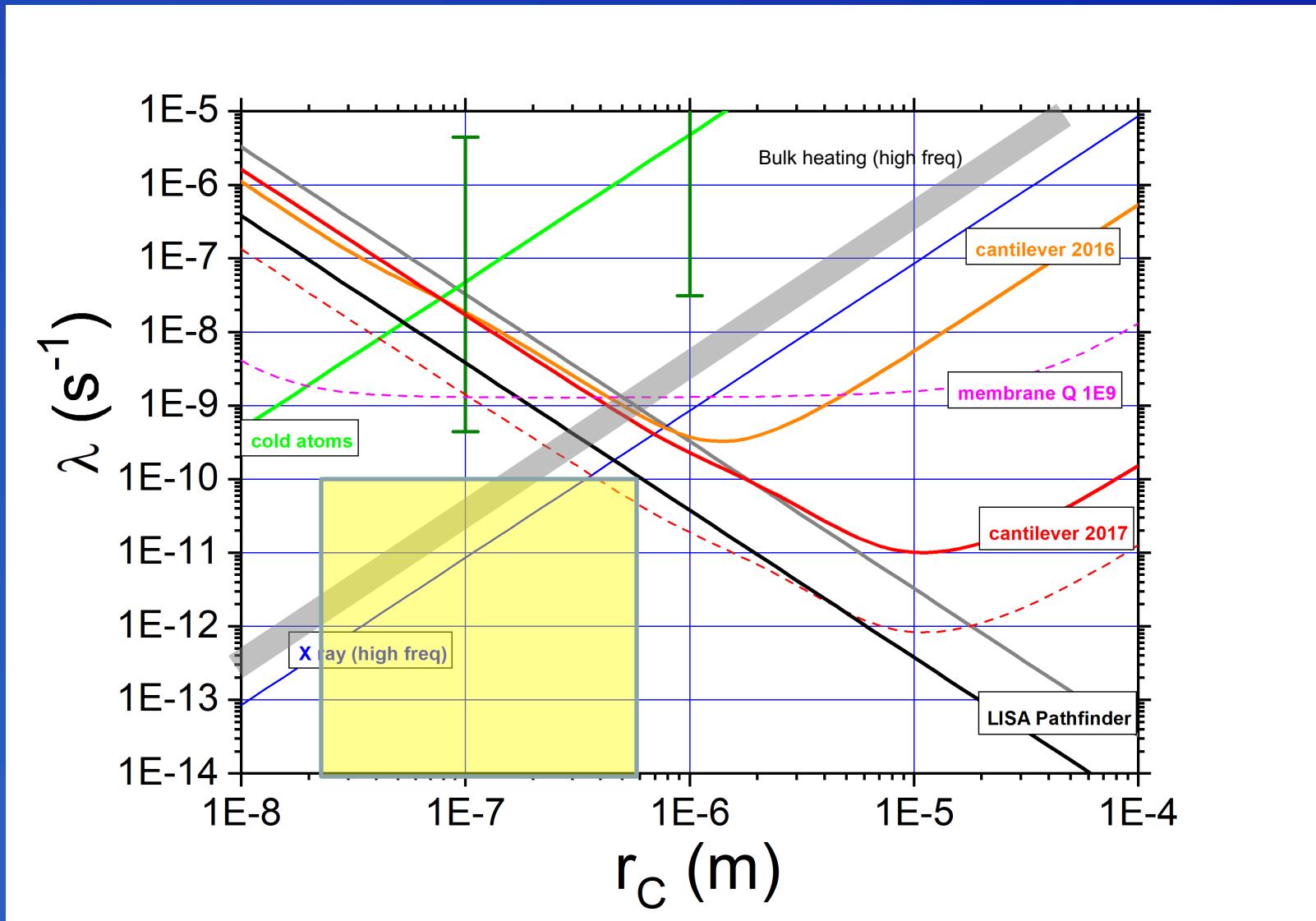


Matter wave interferometers

2) Indirect effects (non-interferometric)

- X-ray spontaneous emission from free electrons
- Spontaneous heating of materials systems (i.e. solid matter)
- Spontaneous diffusion / force noise in mechanical systems/resonators

Current bounds on CSL parameter space



REGION OF INTEREST for NANOSPHERES !

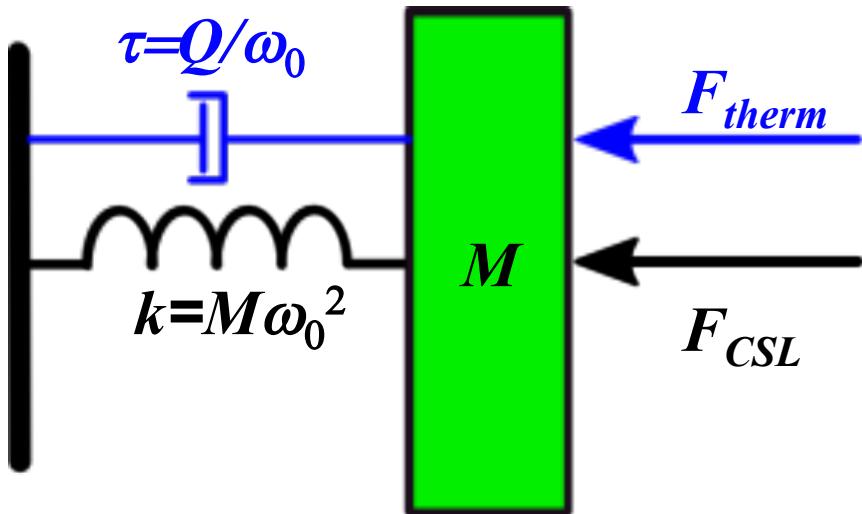
Random Collapses



Momentum kicks



Stochastic driving force



$$\langle E \rangle = k_B T + \Delta E_{CSL} = k_B (T + \Delta T_{CSL})$$

S. Nimmrichter et al, PRL 113 020045 (2014)

L. Diosi, PRL 114, 050403 (2015)

A. Vinante et al, PRL 116, 090402 (2016)

CSL-heating on a mechanical resonator

$$\langle E \rangle = k_B T + \frac{\hbar^2 \eta Q}{2m\omega_0}$$

$$S_{ff} = \frac{4k_B T m \omega}{Q} + 2\hbar^2 \eta$$

$$\begin{aligned} \eta &= \frac{2\lambda}{m_0^2} \iint d^3\mathbf{r} d^3\mathbf{r}' \exp\left(-\frac{|\mathbf{r}-\mathbf{r}'|^2}{4r_C^2}\right) \frac{\partial\rho(\mathbf{r})}{\partial z} \frac{\partial\rho(\mathbf{r}')}{\partial z'} \\ &= \frac{(4\pi)^{\frac{3}{2}} \lambda r_C^3}{m_0^2} \int \frac{d^3\mathbf{k}}{(2\pi)^3} k_z^2 e^{-\mathbf{k}^2 r_C^2} |\tilde{\rho}(\mathbf{k})|^2 \end{aligned}$$

MAXIMIZATION of Signal to Noise (actually Noise to Noise):

High $\tau = \frac{\varrho}{\omega_0}$  Low Frequency! (opposite as in quantum optomechanics)

Low T

Low $\frac{\eta}{m}$  1) Size $\ll r_c$ (coherent) $\eta/m \propto m$

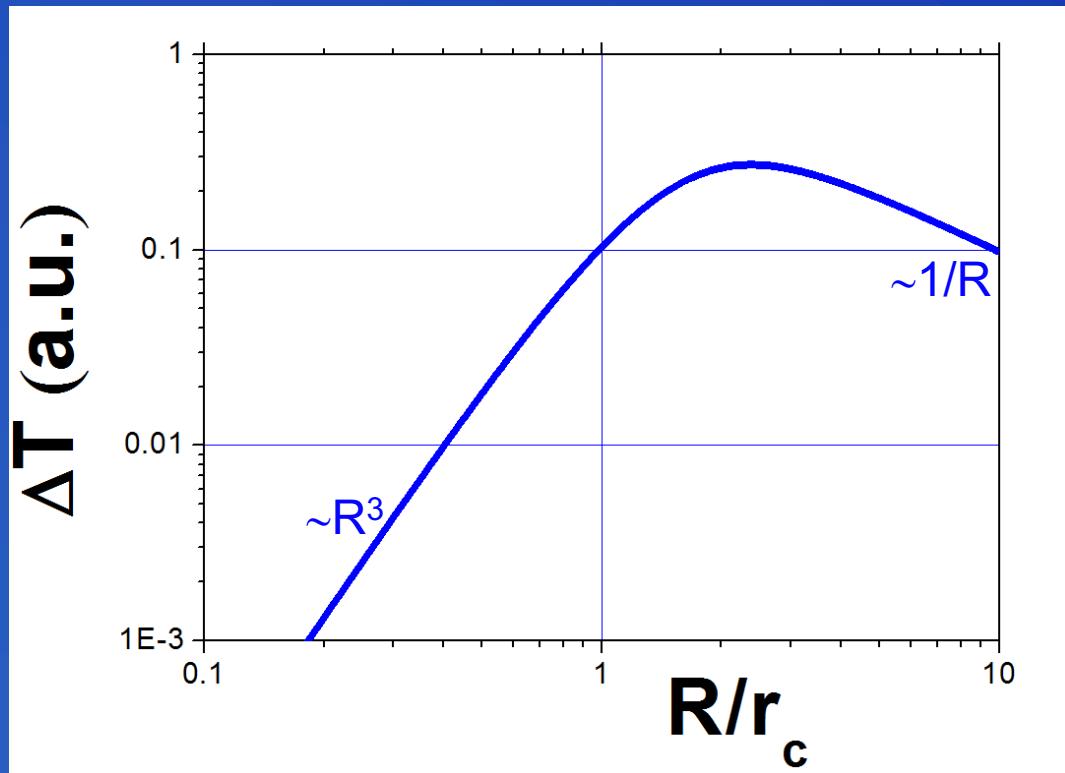
2) Thickness $L \gg r_c$
("surface" noise)

$$\eta/m \propto \rho/L$$

$$\eta \propto \rho^2 A$$

Example: CSL heating of a sphere

Exact solution for a sphere of radius R (at fixed ρ , Q and f_0)



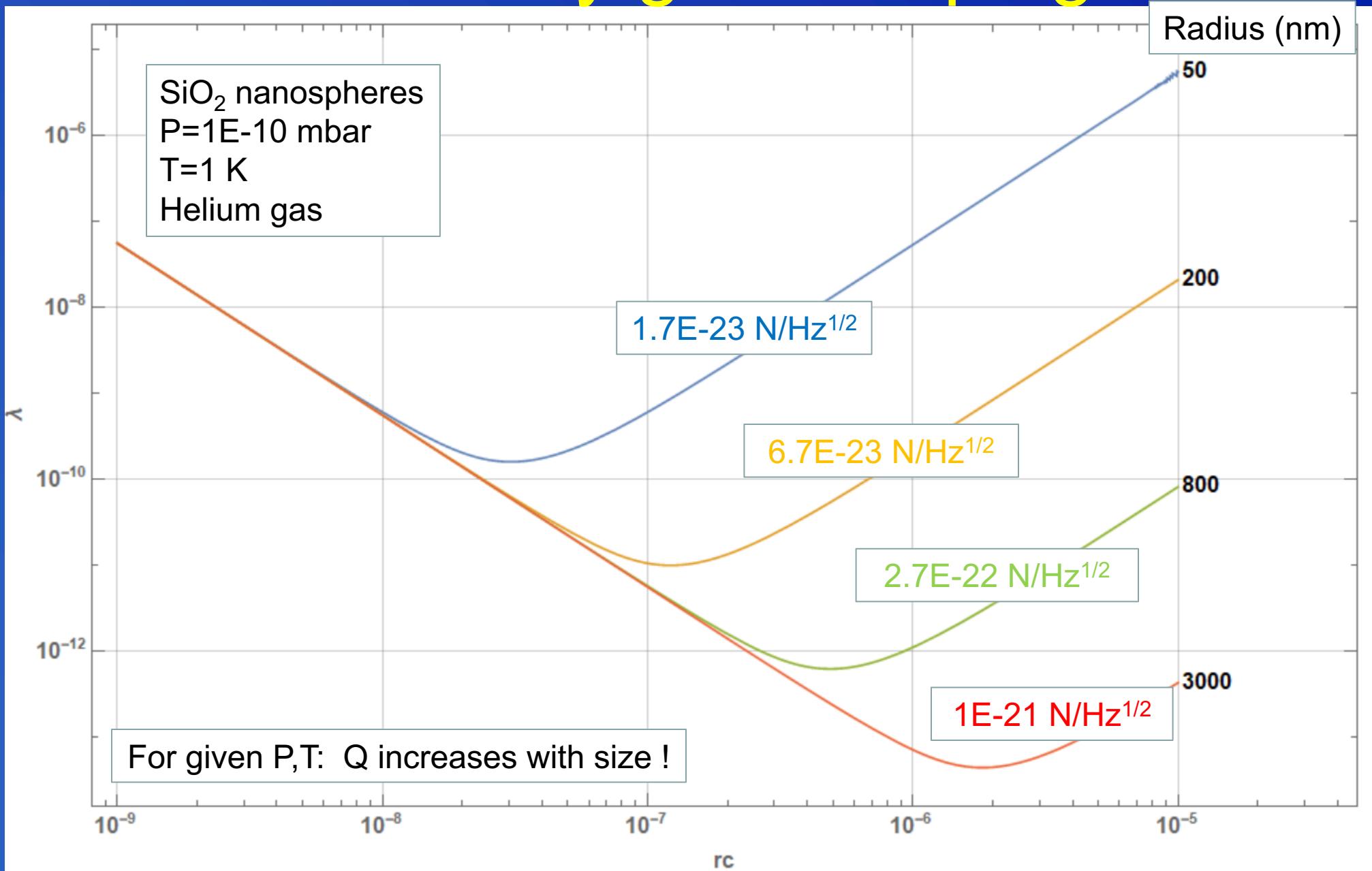
$$\eta = \frac{(4\pi)^2 \lambda r_C^2 \rho^2 R^2}{3m_0^2} \left[1 - \frac{2r_C^2}{R^2} + e^{-\frac{r_C^2}{R^2}} \left(1 + \frac{2r_C^2}{R^2} \right) \right]$$
$$\Delta T = \frac{\hbar^2 \eta}{2k_B m} \tau$$

Maximum at $R \simeq 2r_C$

NOTE:

- 1) The density is important !
- 2) Sphere is not the best geometry. For given mass, cube is slightly better !

BUT: if only gas damping



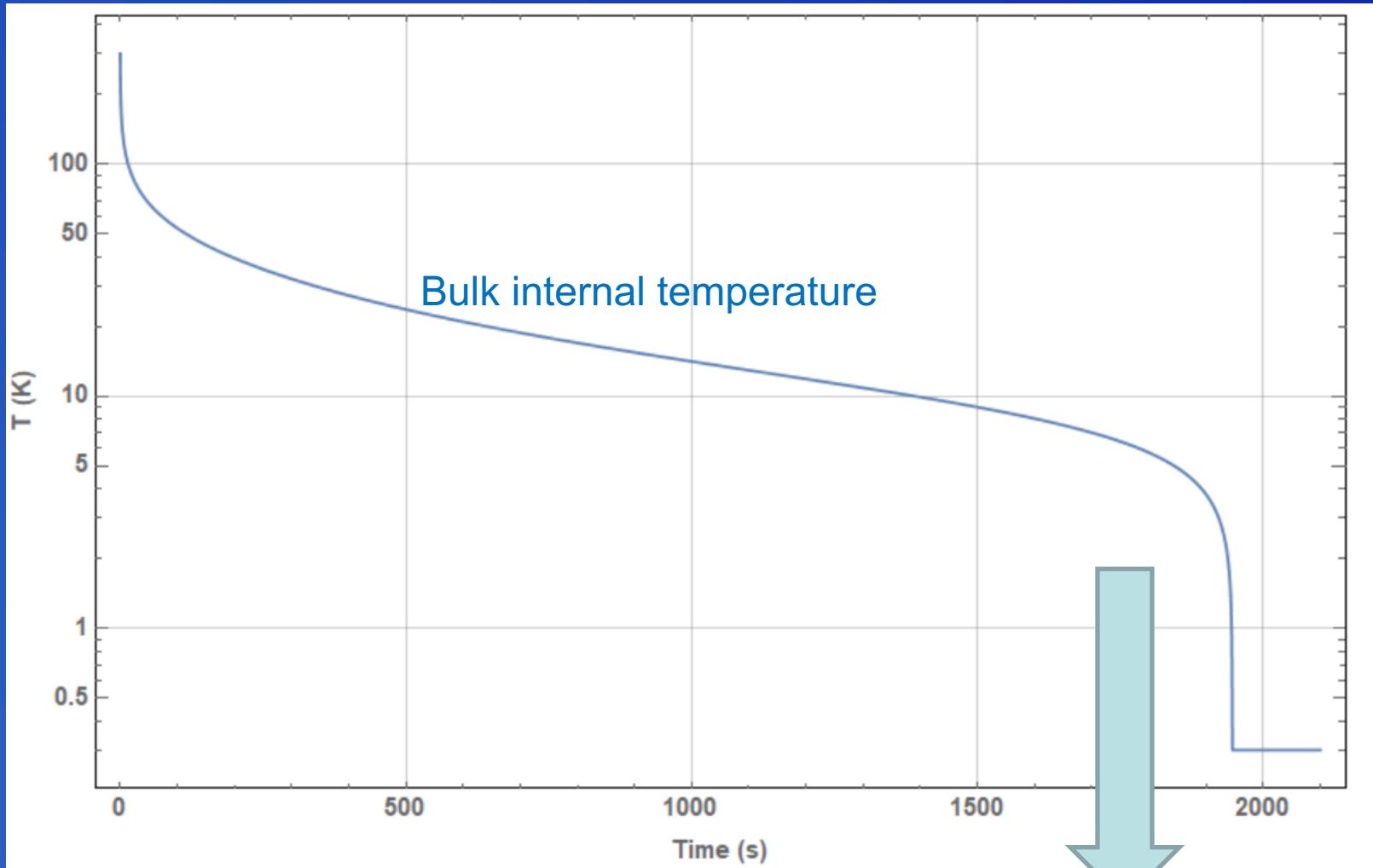
Conclusions

- Radius should not be smaller than 200 nm
Materials with density higher than SiO_2 would help
- For radius \gg 200 nm, bound @ $r_c=10^{-7}$ is almost independent of particle size for given P,T

Can we ever thermalize a micro/nanoparticle
@ $T < 1\text{K}$, $P = 1\text{E-}10 \text{ mbar}$?
(given for granted we can load & trap)

Yes, provided that external heating
(for trapping, measuring) is low enough ...

Thermalization curve



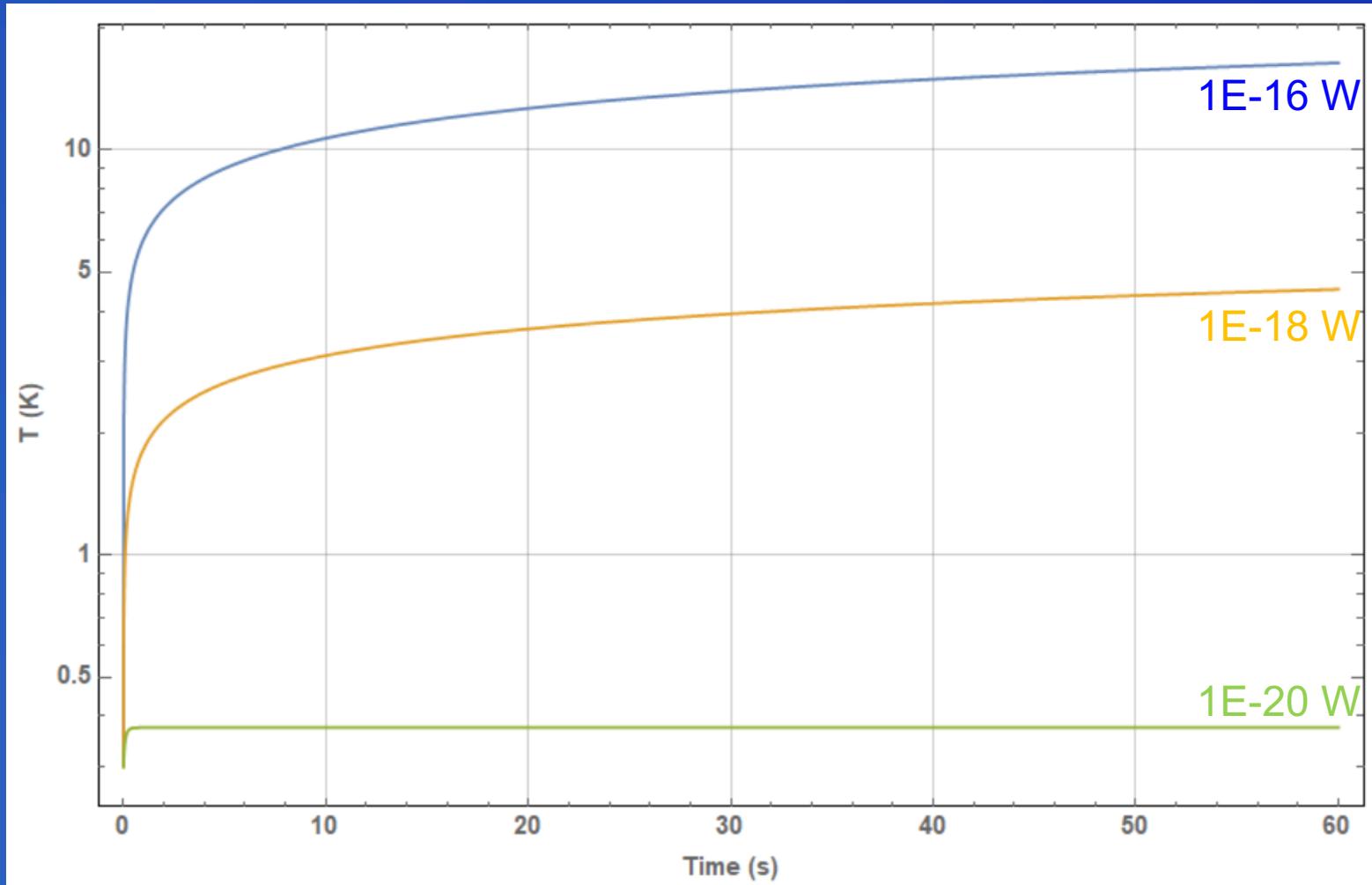
$$C(T) \frac{dT}{dt} = -\dot{Q}_{gas}(T) - \dot{Q}_{bb}(T) + \dot{Q}_{in}$$

Debye model Heat flow to gas Blackbody emission External Heat input

No need for Buffer Cooling

Key assumption: No input power !

Add a continuous power (levitating fields , measurement beam, uncontrolled heat leaks)



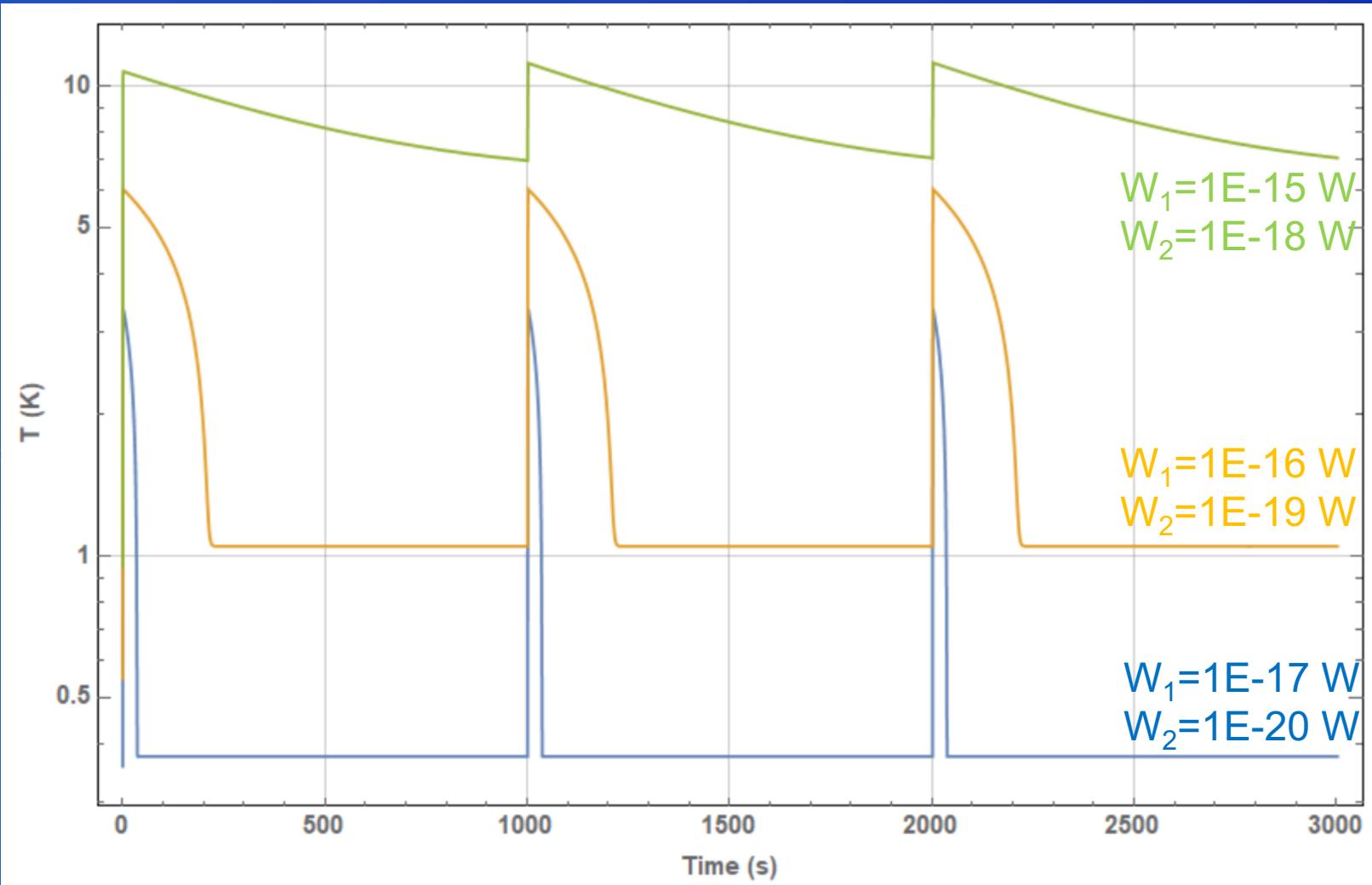
SiO_2 nanosphere
 $R=200 \text{ nm}$

Gas: helium
 $P=1\text{-}10 \text{ mbar}$
 $T_0=0.3 \text{ K}$

$T[0]=0.3 \text{ mK}$

Pulsed input power (stroboscopic measurement)

W_1 (high) for 1 s – W_2 (low) for 1000 s



SiO_2 nanosphere
 $R=200$ nm

Gas: helium
 $P=1E-10$ mbar
 $T_0=0.3$ K

$T[0]=0.3$ K

The TEQ He-3 cryostat

Initial Idea: Dry Dilution Refrigerator

Good: $T > 10 \text{ mK}$

No need for liquid helium (lower running cost)

Continuous operation

Bad: Large vibrations from precooler compressor

Expensive

Final: Wet He3-sorption Refrigerator

Bad: $T > 300 \text{ mK}$

Needs liquid helium (higher running cost)

Single shot operation ($t > 60 \text{ hours}$, rechargeable)

Good: Ultralow vibration operation mode

Cheaper (in the short term...)

The tender

Mandatory Requirements

T < 300 mK

Single shot hold-time > 60 hours

Experimental space: Diameter x Length = 15 x 25 cm

UHV compatible vacuum chamber (P<1E-10 mbar)

Ultralow vibration mode

Outcome

Four companies initially interested

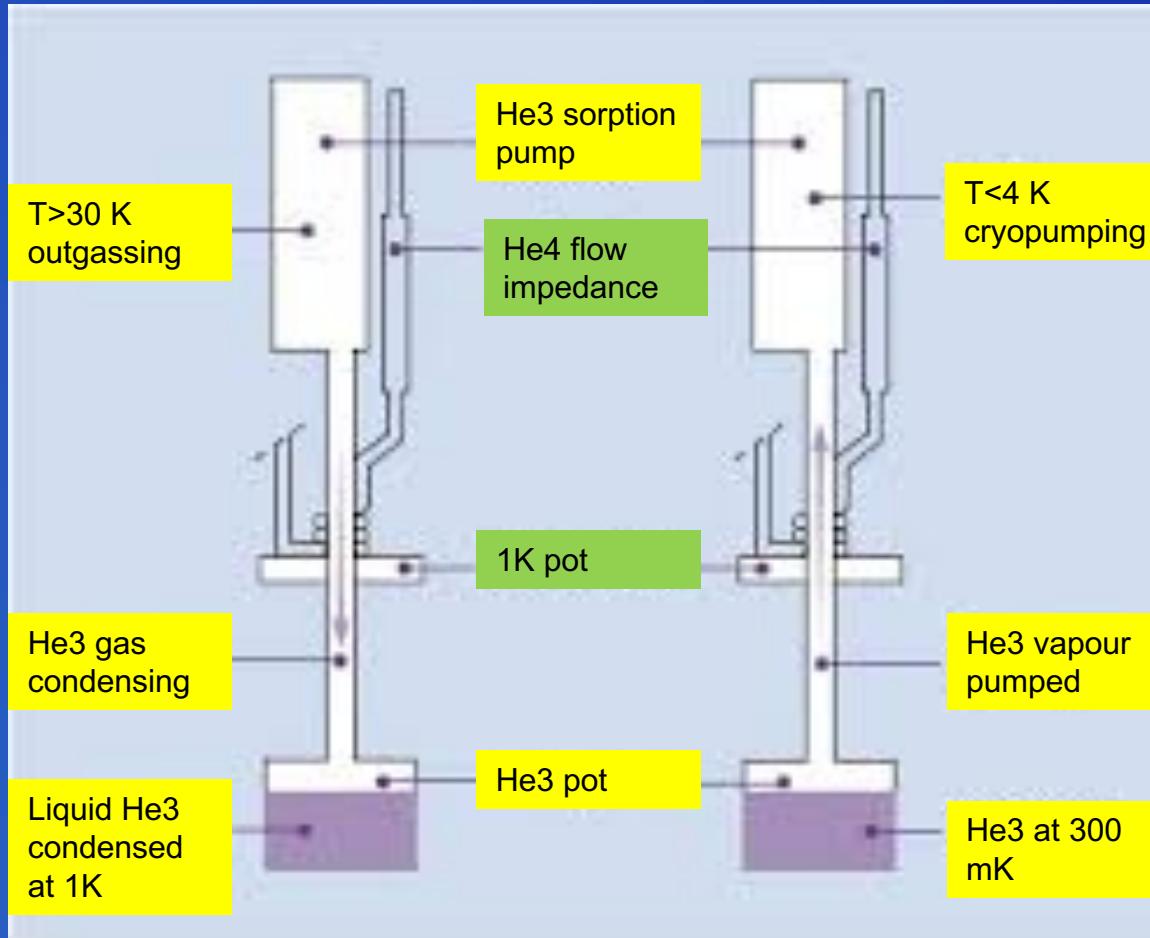
Two companies completed the bidding process

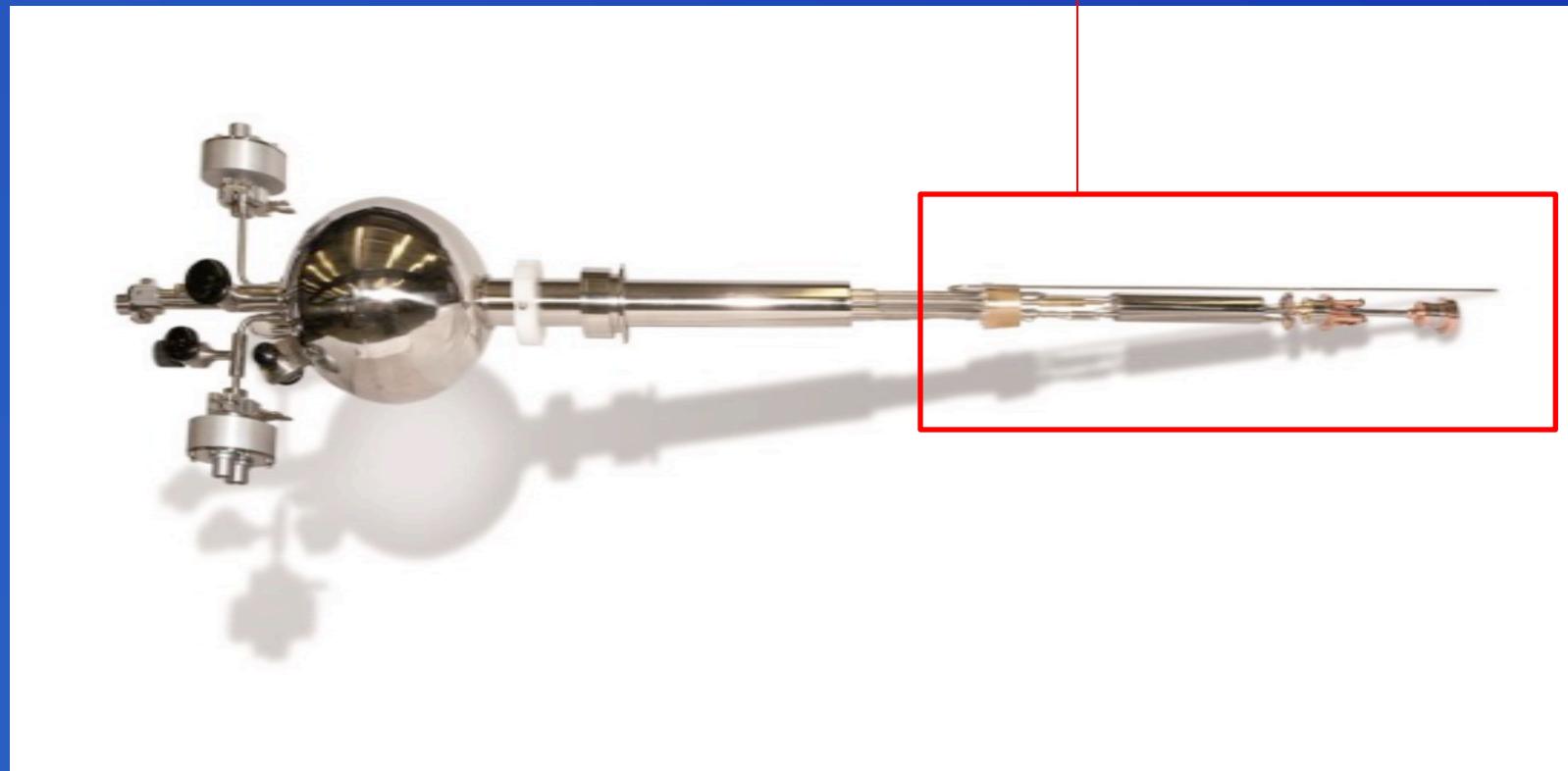
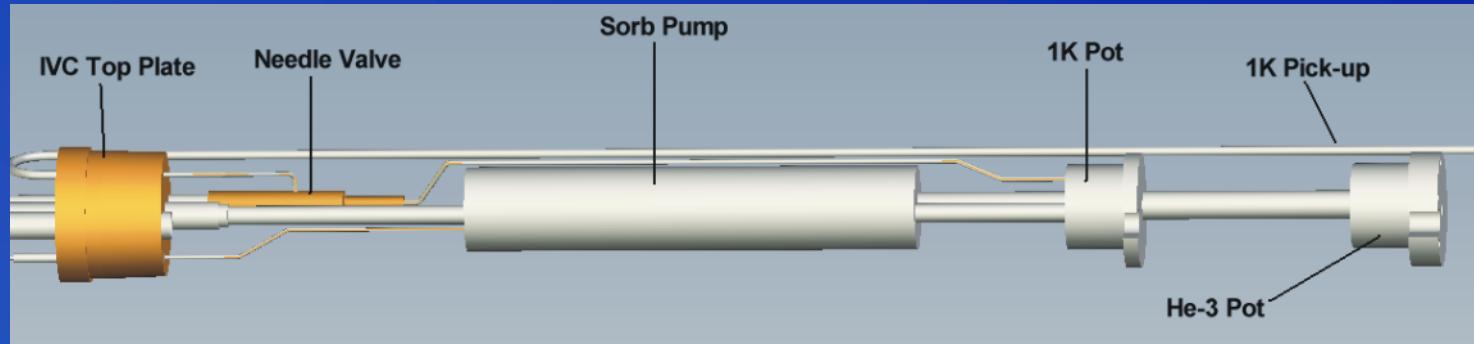
Winner: ICE Oxford (UK)

How it works

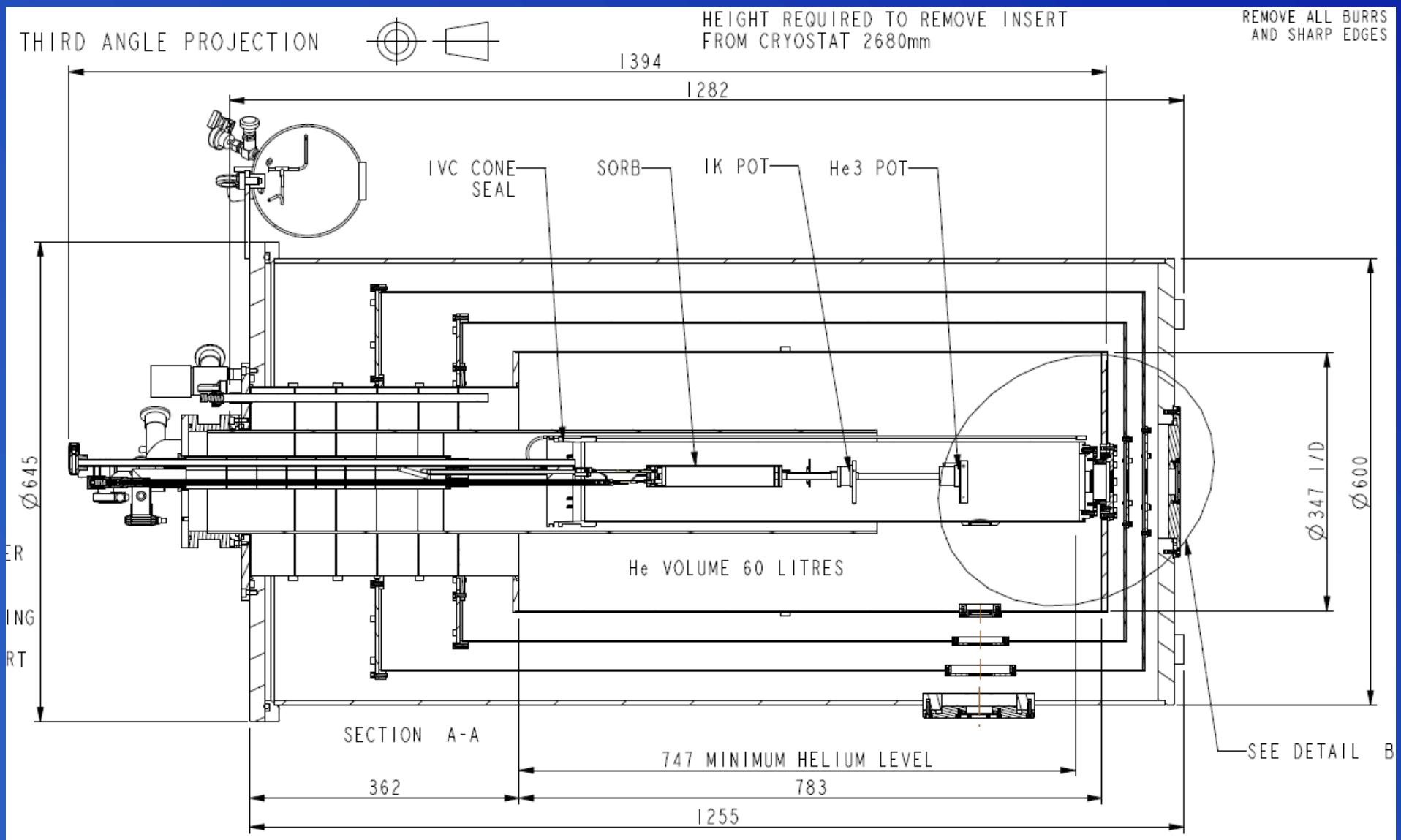
1 Condensation
(Regeneration phase $\sim 1\text{-}2$ hours)

2 Evaporation
(Cooling phase $t > 60$ hours)





A similar ICE system (Paris optomech.)



Additional features

UHV

- Low outgassing rate materials
- UHV flanges
- Residual gas pressure < 1E-10 mbar at the experiment (?)

Optical access

- Optical windows
- Optical fibers (?)

Preinstalled wiring

- 10 flexible coaxial lines
- 12 twisted pairs in one bundle

External mechanical isolation

Wiring (current design)

Coaxial lines: meant for ac signals, e.g. Paul trap “rf bias”

- Stainless steel flexible line
- Cryogenic section: switch to NbTi/CuNi matrix shielded twisted (superconducting to minimize Joule + conduction heating)
- Voltage rating 600 V
- SMA connectors on top flange
- 10x , IS IT ENOUGH ?

Twisted pairs: meant for dc or low freq signals, e.g. Paul trap “dc bias”

- Constantan, cryogenic section switch to NbTi/CuNi
- Voltage rating should be up to 200 V
- Single bundle / Single Fischer connector on top flange
- 12x, IS IT ENOUGH ?

Heat load due to Paul trap bias

1) Ohmic losses:

Heavily suppressed by superconducting wiring

2) Heat conduction through wiring

Heavily suppressed by superconducting wiring

3) Dielectric loss heating in the wiring insulation: Dominant mechanism

For N=10 lines, C≈20 pF

$$W \simeq \frac{1}{2} \delta_L \omega C V_{rf}^2$$
$$\delta_L \simeq 10^{-4}$$

$\omega/2\pi$ (kHz)	V_{rf} (V)	W (μ W)
10	100	6
20	200	50
100	1000	6000

For this cryostat W<100 μ W advisable

Mechanical Isolation

Key idea: No vibrations produced inside the cryostat
(except helium boiling noise but no mechanical pumps)



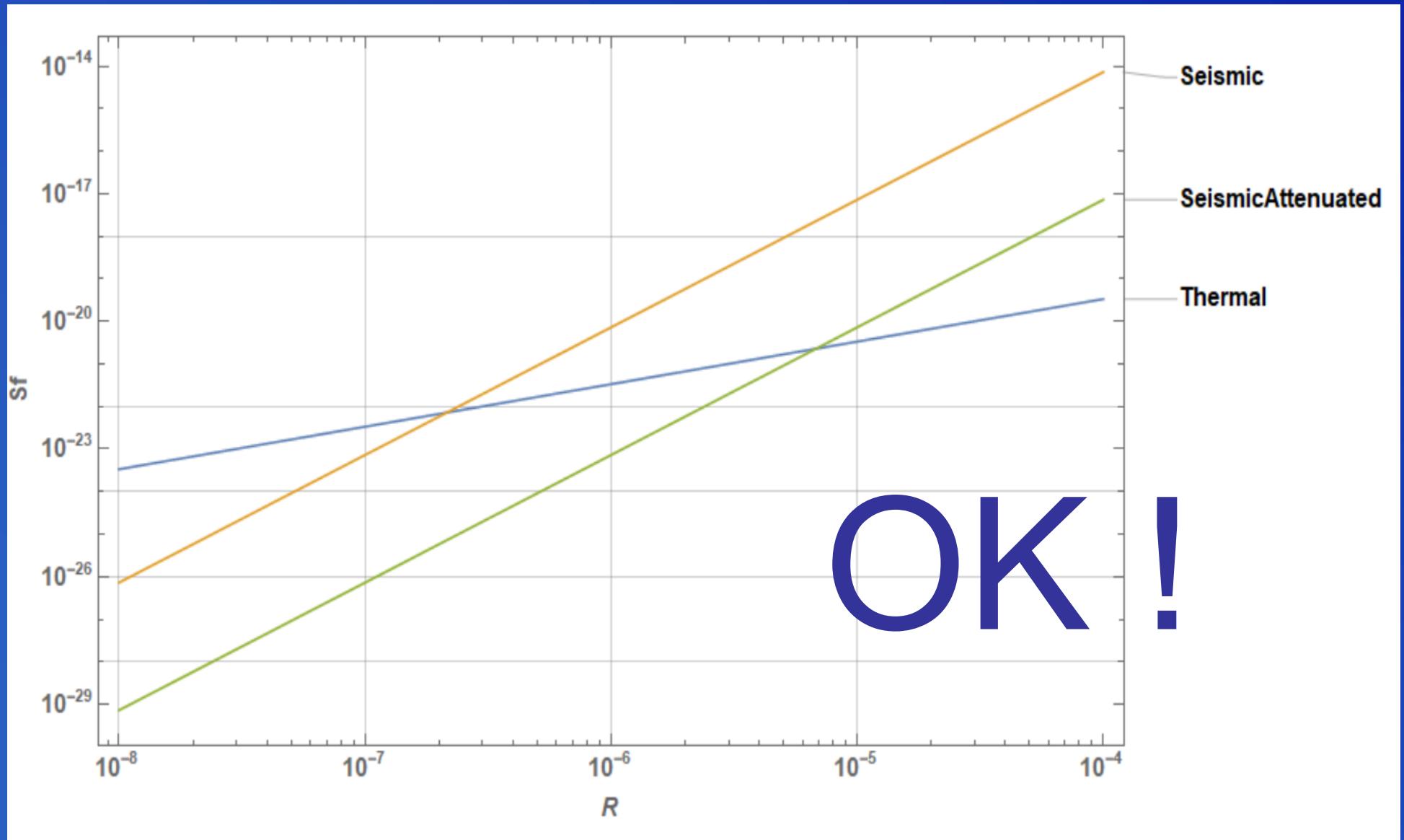
Only external noise relevant

The all cryostat will be suspended
on a pneumatic mechanical isolator (Newport)

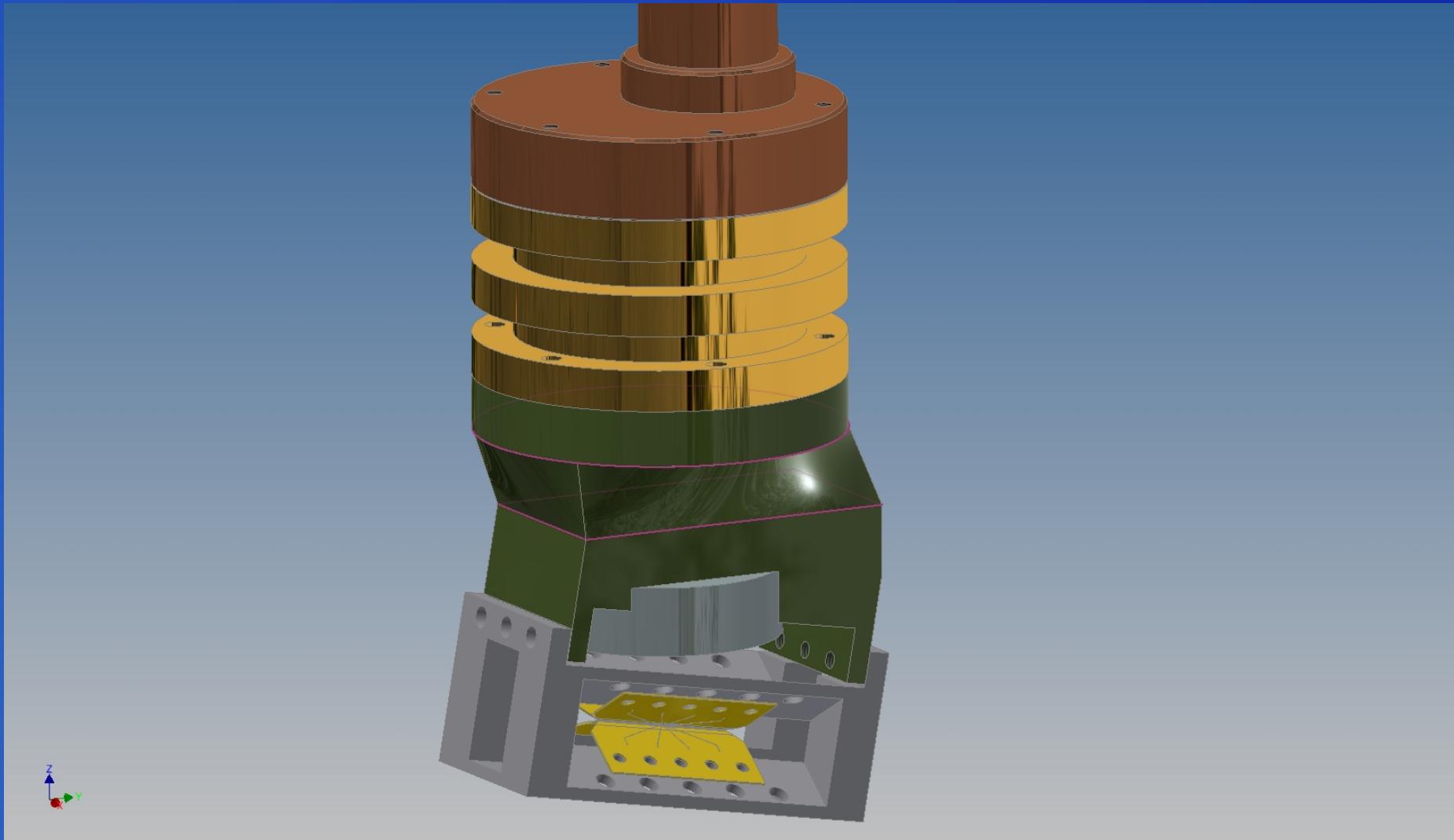
Attenuation > 60 dB @ 30 Hz

IS IT ENOUGH?

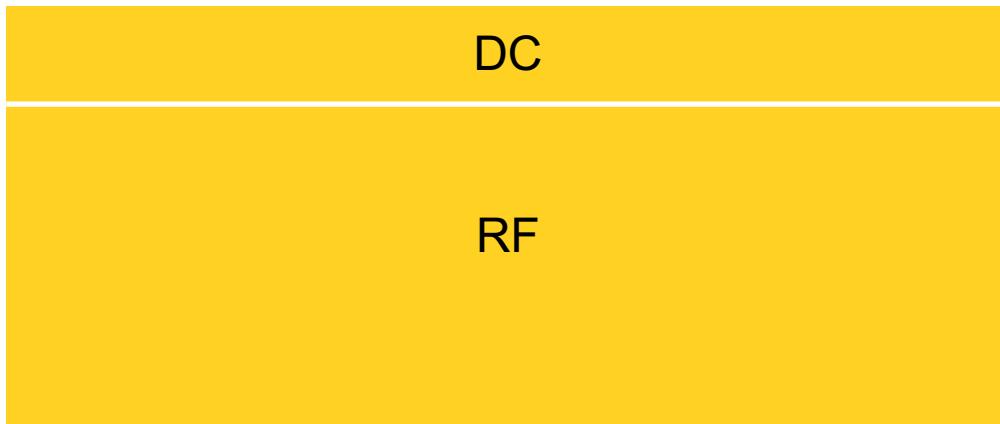
Seismic noise (using standard figures)



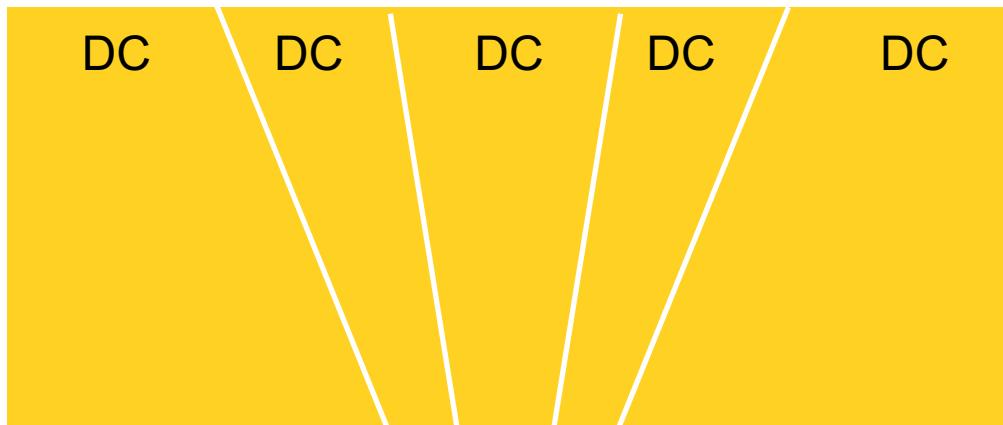
possible Paul trap assembly (parabolic mirror + optical windows)



RF blade electrode

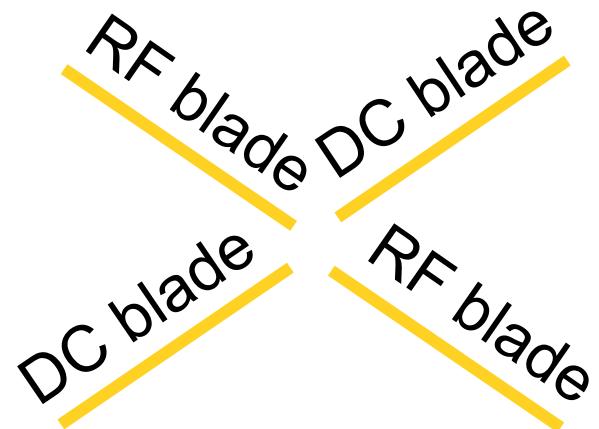


DC blade electrode



Price: 450 £/blade

Mounted electrodes
in a end view:

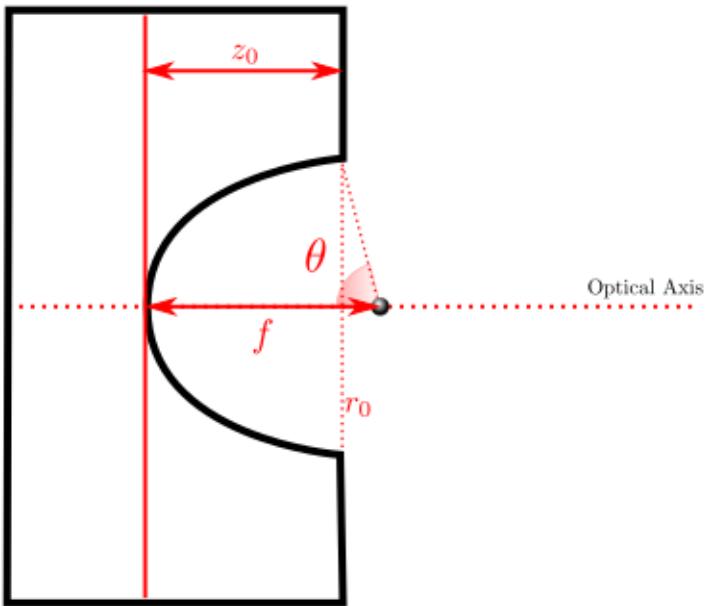


Detectio

n

with
Paraboloidal Mirror

Intro to Paraboloidal Mirror



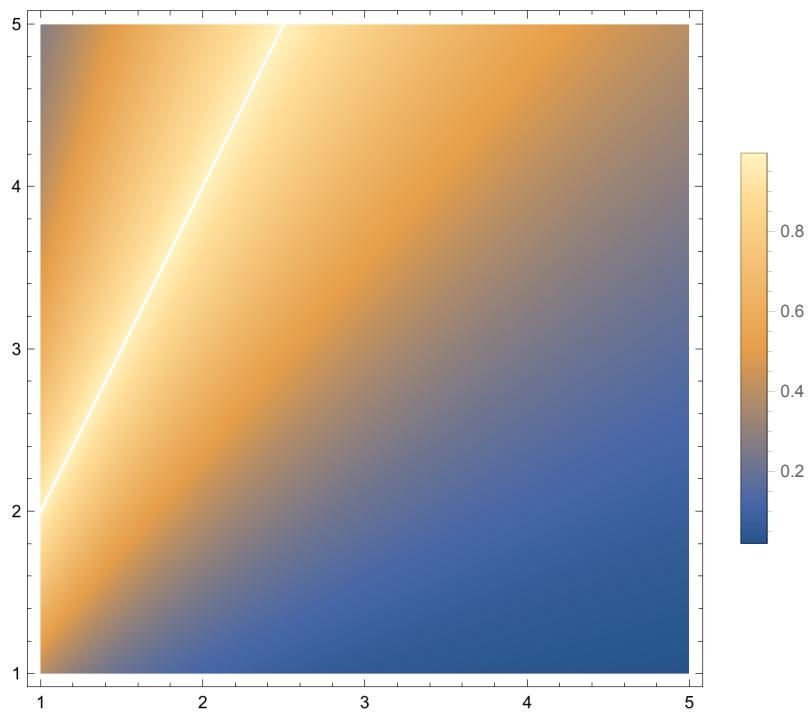
Here r_0 is the radius of curvature, z_0 depth of mirror to the apex, and f is the focal length. The numerical aperture for a lens is defined as:

$$\begin{aligned} \text{NA} &= \int_0^\theta \sin(\theta') d\theta' = 1 - \cos(\theta) \\ &= 1 - \cos\left(\tan^{-1}\left(\frac{r_0}{f - \frac{r_0^2}{4f}}\right)\right) \end{aligned}$$

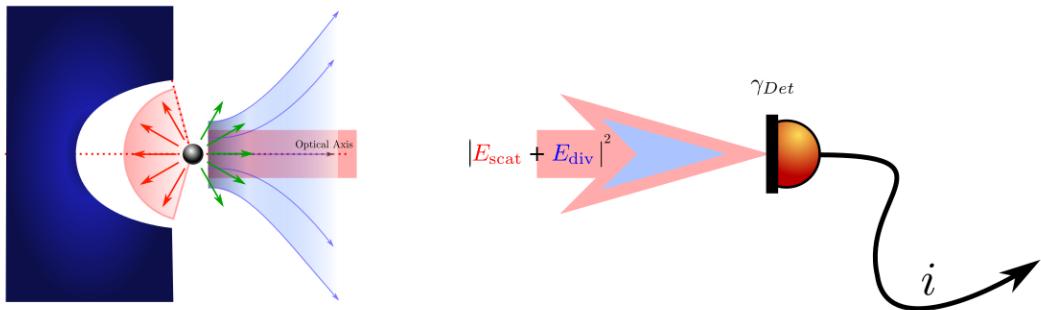
$$\text{NApara}[f_, r0_] := 1 - \text{Cos}[\text{ArcTan}[\frac{r0}{f - \frac{r0^2}{4f}}]];$$

It is worth noting that the maximum NA of 1 is achieved as $\cos(\theta) \rightarrow 0$, $\tan \theta \rightarrow \frac{\pi}{2}$, $r_0 \rightarrow 2f$

```
DensityPlot[Npara[f, r0], {f, 1, 5},  
{r0, 1, 5}, PlotPoints → 100, PlotLegends → Automatic]
```



Detection At the Detector



We can divide the problem into the following parts:

- How much power is scattered by the particle?
- How much power is collected and then detected at the detector?
- How much scattering force generated by the particle?
- And the limits of detection? i.e. What is the temperature sensitivity based on the position sensitivity?
- What is also the force sensitivity based on the above values?

I. How much power is scattered by the particle?

```

Cnst := {hbar → 1.05 × 10-34, c → 3 × 108, n → 1.45,
         ε₀ → 8.8 × 10-12, kB → 1.38 × 10-23, h → 6.626 × 10-34}

OurPara := {λ → 1550 × 10-9, Radius → 50 × 10-9, Ω → 2π1 × 103,
            γ → 2π269, f₀ → c / λ, ηc → 0.0005, ω₀ → 2πf₀, NA → 0.997,
            ρ → 1800, m → ρ 4πRadius3 / 3, k → 2π / λ, w₀ → λ / (π NA), γc → Radius / w₀}

NovotnyPara := {λ → 1064 × 10-9, Ω → 2π150 × 103, γ → 2π269,
                f₀ → c / λ, ηc → 0.0005, ω₀ → 2πf₀, Radius → 50 × 10-9,
                NA → 0.9, P₀ → 70 × 10-3, k → ω₀ / c, m → 1.14 × 10-18}

TEQpara := {λ → 1550 × 10-9, Ω → 2π1 × 103, γ → 2π269,
             f₀ → c / λ, ηc → 0.0005, ω₀ → 2πf₀, Radius → 50 × 10-9,
             NA → 0.997, k → ω₀ / c, m → ρ 4πRadius3 / 3, ρ → 1800,
             Γ → 0.619 ((9π) / Sqrt[2]) ((ηair d2) / (ρ kB T₀)) (Pgas / Radius), Pgas → 100 × 10-10,
             ηair → 18.2 × 10-6, d → 0.375 × 10-9, T₀ → 300, w₀ → λ / (π NA), γc → Radius / w₀}

(* Polarizability [1]*)
α := 4πε₀ Radius3 (n2 - 1) / (n2 + 2)

(* Rayleigh Cross Section [1]*)
σscat := α2 k4 / (6πε₀2)

(* Scatter Power
   The additional parameter γc,
   is a ratio of the beam focal waist w₀ and the particle radius.
*)

PScat := γc σscat I₀

I₀ := (2 P₀ NA2 π) / λ2

(* P₀ k2 NA2 *)
PScat // . Cnst // . TEQpara /. {P₀ → 600 × 10-3}
(*PScat//.Cnst//.NovotnyPara/.{P₀→ 100 10-3,γc→ 1}*)
PScat // . Cnst // . TEQpara /. {P₀ → 0.5 × 10-3}
4.02284 × 10-7
3.35237 × 10-10

```

Therefore, the trapped particle at the focal region will scatter **400 nW @ P₀ = 600 mW**. Whilst @ **0.5 mW** of P₀ the scattering is **0.3 nW**. For a 50 nm radius particle.

2. How much power is collected and then detected at the detector?

The photon scatter once collect reaches the detector through massive amounts of losses. These losses are:

- γ_{para} , collection of the paraboloidal mirror = NA/2
- $N_{\text{optElements}}$, Number of Optical mirrors = 4
- γ_{mirrors} , efficiency of optical silver mirrors = 0.96
- QE, detector quantum efficiency

From which we get the total detection efficiency (we add an additional loss parameter as not all the light is focussed on to the photodetector [2]):

```

QE := (S 1240) / λ (* The Quantum Efficiency[3]*)
γTotal := γpara γmirrorsNElements QE (DetectorArea / MirrorDiameter) //.
  {γpara → NA/2, γmirrors → 0.96, NEElements → 4, S → 1, λ → 1550,
   NA → 0.997, DetectorArea → 0.3 × 10-3, MirrorDiameter → 3 × 10-3}
(*Note: NEPmin refers to Minimum measured NEP,
Rmax is max responsivity, R is Gain output *)
NEP := (NEPmin Rmax) / R //.
  {Rmax → 1, NEPmin → 1.55 × 10-12, R → 105}
NEPAbs := NEP Sqrt[bandwidth] /. bandwidth → 4 × 106
OpticalInput := ((1 × 10-3) / 50) (1 / R) /. R → 105

{"Detector Efficiency",
 γTotal //.. Cnst //.. TEQpara /. {P0 → 0.5 × 10-3, Impedance → 50}}
 {"Pdet", PScat γTotal //.. Cnst //.. TEQpara /. {P0 → 0.5 × 10-3, Impedance → 50}}
 {"Pscat", PScat //.. Cnst //.. TEQpara /. {P0 → 0.5 × 10-3}}
 {"OpticalInput with oscilloscope", OpticalInput // N}
 {"NEPbnd", NEPAbs // N}
 {"Allowed S/N",
  AllowedSN = PScat γTotal //.. Cnst //.. TEQpara /. {P0 → 0.5 × 10-3, Impedance → 50}}
  {"Predicted Temp@ 300 K", PredictedTemp = 300 / AllowedSN × 103 "mK"}
  {"Predicted Temp@ 300 mK", PredictedTemp = 300 × 10-3 / AllowedSN 106 "μK"}
  {Detector Efficiency, 0.0338719}

 {"Pdet", 1.3626138112109088`*^-10}
 {Pscat, 4.02284 × 10-9}
 {OpticalInput with oscilloscope, 2. × 10-10}
 {NEPbnd, 3.1 × 10-14}
 {Allowed S/N, 4395.53}

```

{Predicted Temp@ 300 K, 68.2512 mK}

{Predicted Temp@ 300 mK, 68.2512 μ K}

The detection efficiency seems to be 0.03 compared to *Jain et al* [1] to be 0.0005.

For 500 μ W of incident Power:

Detector NEP@ λ = 0.015 fW/ $\sqrt{\text{Hz}}$

Detector Signal = 0.1 nW

Scattered Signal = 4 nW

NEP@(λ , Bandwidth) = 31 fW

If at signal of 0.1 nW is 300 K then to reach gr bound state at 1 μ K a signal drop of factor 10^8 needs to be accommodated. The available S/N is 10^4 .

If starting temp is 300 K => 68 mK

if starting temp is 300 mK => 68 μ K

NEP 10^{15}

0.0155

The question of how small a signal can our current detectors detect can be characterised by Noise Equivalent Power (NEP). For our case the NEP is 0.0155 fW/ $\sqrt{\text{Hz}}$.

$3 \times 10^{-7} / \text{Sqrt}[4 \times 10^6] // N$

1.5×10^{-10}

$\frac{300 \times 10^{-3}}{\frac{0.1 \times 10^{-9}}{31 \times 10^{-15}}} // N$

0.000093

3. Noise Power Spectral Density

```

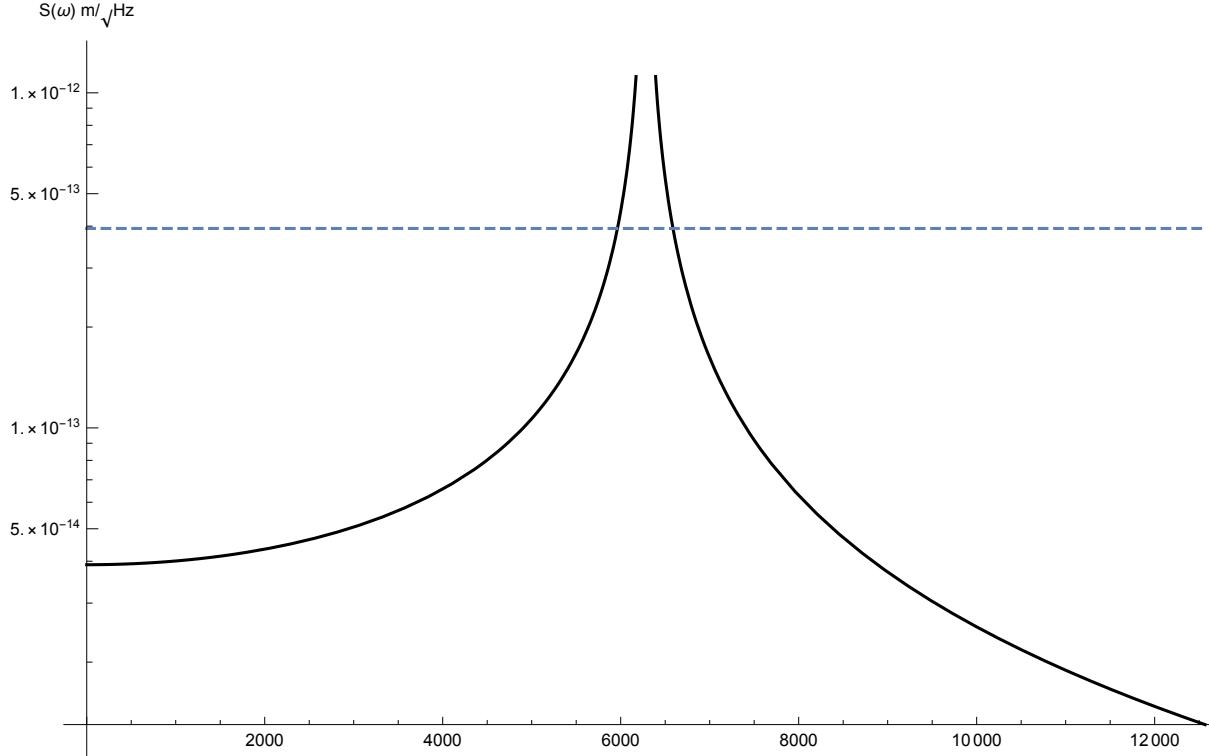
TEQpara := {λ → 1550 × 10-9, Ω → 2 π 1 × 103, γ → 2 π 1 × 10-6,
f₀ → c / λ, ηc → 0.0005, ω₀ → 2 π f₀, Radius → 50 × 10-9, NA → 0.997,
P₀ → 0.5 × 10-3, k → ω₀ / c, m → ρ 4 π Radius3 / 3, ρ → 1800,
Γ → 0.619 ((9 π) / Sqrt[2]) ((ηair d2) / (ρ kB T₀)) (Pgas / Radius),
Pgas → 100 × 10-10, ηair → 18.2 × 10-6, d → 0.375 × 10-9, T₀ → 300} //.
Cnst
Γ / (2 π) //.
TEQpara //.
Cnst
1.35294 × 10-7

```

```

Syzp := hbar / (2 π m γ Ω) // . Cnst // . TEQpara // . Cnst;
(* Zero Point Spectral Density *)
S0sci := ((2 kB T) / (π m)) (Γ / ((Ω² - ω²)² + (ω Γ)²)) // . Cnst // . TEQpara // . Cnst // .
{Τ → 300 × 10⁻³} ; (* Mechanical Motion *)
Sysn := NEP / (10⁴)² (* Detector Noise *)
Sy0scN := 1 × 10⁻¹² / (10⁴)² (* Oscilloscope Noise *)
SyShotNoise :=
  (*Stotal:= SBrown + S0sci + Sthermal;*)
  ScaleFactor = 1;
PlotZP = LogPlot[Sqrt[Syzp] ScaleFactor, {ω, 0, 2 π .2 × 10⁴}, PlotStyle → Red];
Plot0sc = LogPlot[Sqrt[S0sci] ScaleFactor, {ω, 0, 2 π .2 × 10⁴}, PlotStyle → Black];
(* PlotTotal=
  LogPlot[Sqrt[Stotal]ScaleFactor,{ω,0,2 π 1 10⁴}, PlotStyle→Dashed]; *)
PlotSN = LogPlot[Sqrt[Sysn] ScaleFactor, {ω, 0, 2 π .2 × 10⁴}, PlotStyle → Dashed];
Show[Plot0sc, PlotZP, PlotSN,
  PlotRange → All,
  PlotPoints → 150, PlotStyle → Medium,
  AxesLabel → {"ω (Hz)", "S(ω) m/√Hz"}, PlotRange → All]

```



Sqrt[Sysn]

3.937×10^{-13}

```

Sqrt[S0sci //. Cnst //. TEQpara //. Cnst]
0.0154182  $\sqrt{\frac{1}{7.22634 \times 10^{-13} \omega^2 + (4000000 \pi^2 - \omega^2)^2}}$ 

(* PlotRange-
{{2 π 50 103, 2 π 150 103}, {Log[Sqrt[1 10-30]], Log[Sqrt[1 10-15]])}},*)

xvar = 1 × 10-12;
Ekbt = 0.5 kB T //. Cnst //. SotonPara //. T → 300
Eke = 0.5 mΩ2 xvar2 //. Cnst //. SotonPara
Tmp =  $\frac{m\Omega^2}{kB} xvar^2 //. Cnst //. SotonPara$ 
xv = Sqrt[  $\frac{kB T}{m\Omega^2}$  ] //. Cnst //. SotonPara //. T → 3 × 10-3

(*SBrown := S0/ω2 //.{gfactor → 105, S0 → 10-12/gfactor} ;(* Brownian Noise *)
*) (*Sthermal := ( 2 kB Tnoise r )/π //.{Tnoise → 300} //. Cnst //. TEQpara ;
(* Thermal Noise *)*)
(*PlotBrown =
LogPlot[Sqrt[SBrown ]ScaleFactor,{ω,0,2 π .2 104}, PlotStyle→Brown];
PlotThermal= LogPlot[Sqrt[Sthermal]ScaleFactor,
{ω,0,2 π .2 104}, PlotStyle→Orange];*)

```

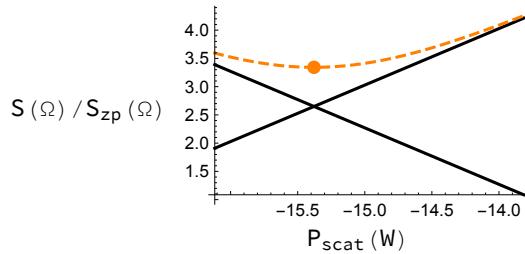
How much power at Backaction and Photon Recoil Limit?

The criteria required for the minimum amount of scattered power required to resolve the system (i.e. overcoming measurement noise/imprecision) whilst limiting the backaction is [1]:

```

Syzp := hbar / (2 π m γ Ω) (* Zero Point Spectral Density *)
Syimprecision := (Syzp/2) (1 / ηc) ((m c² γ Ω) / (2 ω₀ Pscat))
(* Measurement Imprecision *)
Sybackaction := (Syzp/2) (2/5) ((2 ω₀ Pscat) / (m c² γ Ω))
(* Measurement Backaction *)
Syy := Syimprecision + Sybackaction
PScatmin := Sqrt[5 / (8 ηc)] (Ω / ω₀) m c² γ (* *)
TEQpara := {λ → 1550 × 10⁻⁹, Ω → 2 π 1 × 10³, γ → 2 π 269 ,
f₀ → c / λ, ηc → 0.0005, ω₀ → 2 π f₀, Radius → 100 × 10⁻⁹,
NA → 0.997, P₀ → 0.5 × 10⁻³, k → ω₀ / c, m → ρ 4 π Radius³ / 3, ρ → 1800}
TEQPointX = PScatmin // . TEQpara // . Cnst;
TEQPoint = Log[Syy / Syzp // . TEQpara // . Cnst /. {Pscat → TEQPointX}];
plotImp = LogLogPlot[Syimprecision / Syzp // . TEQpara // . Cnst,
{Pscat, 1 × 10⁻⁷, 1 × 10⁻⁶}, PlotStyle → Black];
PlotBack = LogLogPlot[Sybackaction / Syzp // . TEQpara // . Cnst,
{Pscat, 1 × 10⁻⁷, 1 × 10⁻⁶}, PlotStyle → Black];
PlotSyyTEQ = LogLogPlot[Syy / Syzp // . TEQpara // . Cnst,
{Pscat, 1 × 10⁻⁷, 1 × 10⁻⁶}, PlotStyle → {Dashed, Orange}];
teqP = Graphics[{PointSize[Large], Orange, Point[{Log[TEQPointX], TEQPoint}]}];
Labeled[Show[plotImp, PlotBack, PlotSyyTEQ, teqP, PlotRange → All],
{"Pscat (W)", "S(Ω) / Szp(Ω)"}, {Bottom, Left}]

```



Whilst noting that the scattering power is also dependant upon the incident laser power given by:

```
(*JainPointX = PScatmin//.NovotnyPara//.Cnst;
SotonPointX = PScatmin//.SotonPara//.Cnst;*)
(*JainPoint = Log[ $\frac{Syv}{Syzp}$ //.NovotnyPara//.Cnst/.{Pscat→ JainPointX}];
SotonPoint = Log[ $\frac{Syv}{Syzp}$ //.SotonPara//.Cnst/.{Pscat→ SotonPointX}];*)
(*PlotSyy=
LogLogPlot[ $\frac{Syv}{Syzp}$ //.NovotnyPara//.Cnst, {Pscat,1 10-7,1 10-4},PlotStyle→Red];
PlotSyySoton=LogLogPlot[ $\frac{Syv}{Syzp}$ //.SotonPara//.Cnst,
{Pscat,1 10-7,1 10-4},PlotStyle→Dashed];*)
(*PlotSyy=LogLogPlot[ $\frac{Syv}{Syzp}$ //.NovotnyPara//.Cnst,
{Pscat,1 10-7,1 10-4},PlotStyle→Red];
g=Graphics[{PointSize[Large],Red,Point[{Log[JainPointX],JainPoint}]}];
s=Graphics[{PointSize[Large],Blue,Point[{Log[SotonPointX],SotonPoint}]}];*)
```

Power absorbed/Scattered

```

 $\epsilon = 2;$ 
 $(*(*\epsilon i*) = 2 \epsilon ; (* \text{ for } 1550\text{nm } *))$ 
 $\epsilon i = 2 \epsilon 2.5 \times 10^{-8}; (*n=2+i 2.5 10^{-8} *)$ 
 $\epsilon r = \epsilon - i \epsilon i;$ 

 $I_0 := \frac{P_0 k^2 NA^2}{2 \pi}$ 
 $PScat := \sigma_{scat} I_0$ 
 $\sigma_{scat} := \frac{\alpha^2 k^4}{6 \pi \epsilon_0^2}$ 
 $\alpha := (4 \pi \epsilon_0 \text{Radius}^3 (n^2 - 1) / (n^2 + 2))$ 
 $Pabs := 12 \pi \frac{I_0}{\lambda} \left( \frac{4 \pi \text{Radius}^3}{3} \right) \text{Im} \left[ \frac{\epsilon + i \epsilon i - 1}{\epsilon + i \epsilon i + 2} \right]$ 

SotonPara :=
 $\{\lambda \rightarrow 1550 \times 10^{-9}, f_0 \rightarrow c / \lambda, \omega_0 \rightarrow 2 \pi f_0, NA \rightarrow 0.997, P_0 \rightarrow 0.1 \times 10^{-3}, k \rightarrow \omega_0 / c\}$ 
CavityPara :=
 $\{\lambda \rightarrow 1064 \times 10^{-9}, f_0 \rightarrow c / \lambda,$ 
 $\omega_0 \rightarrow 2 \pi f_0, NA \rightarrow 0.997, P_0 \rightarrow 0.5 \times 10^{-3}, k \rightarrow \omega_0 / c\}$ 
PScat
Pabs
 $\frac{4 k^6 (-1 + n^2)^2 NA^2 P_0 \text{Radius}^6}{3 (2 + n^2)^2}$ 
 $\frac{4.71239 \times 10^{-7} k^2 NA^2 P_0 \text{Radius}^3}{\lambda}$ 
 $\frac{4 k^6 (-1 + n^2)^2 NA^2 P_0 \text{Radius}^6}{3 (2 + n^2)^2}$ 
 $\frac{4 k^6 (-1 + n^2)^2 NA^2 P_0 \text{Radius}^6}{3 (2 + n^2)^2}$ 

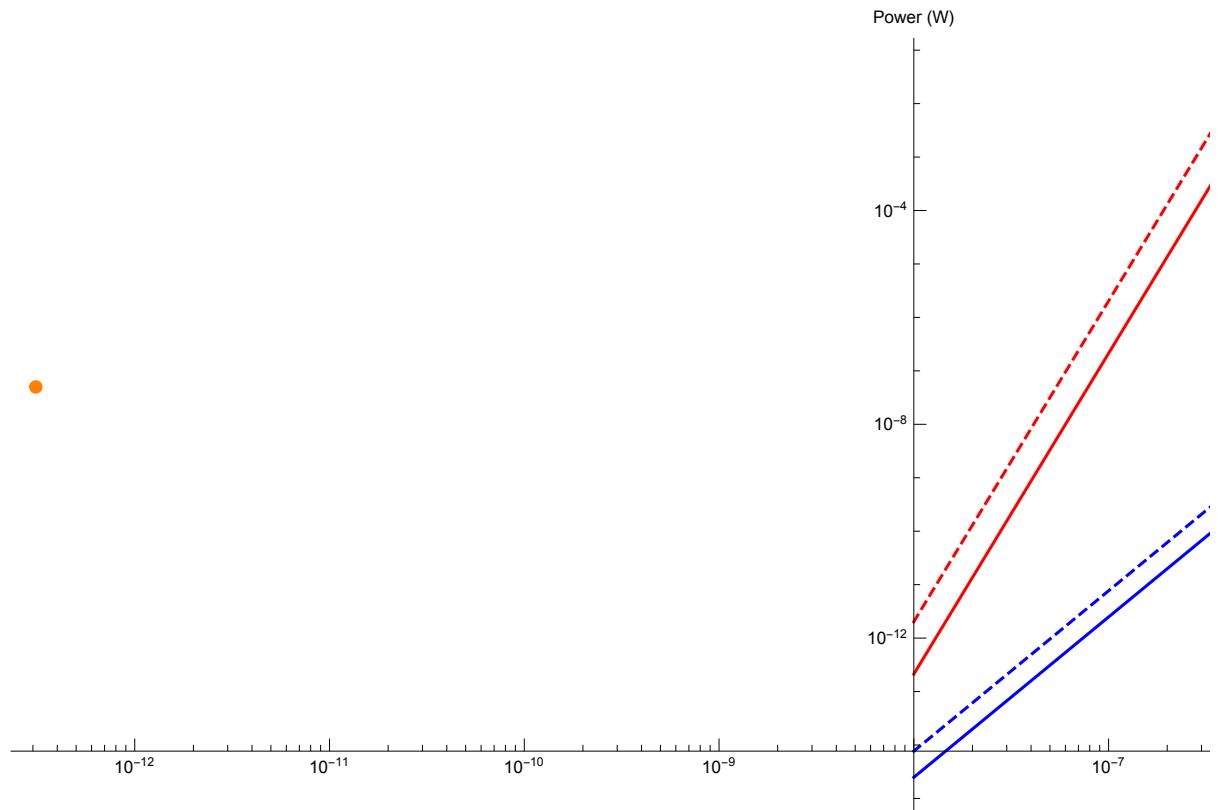
Pabs // Cnst // SotonPara /. {Radius → 50 × 10-9}
6.20735 × 10-14

```

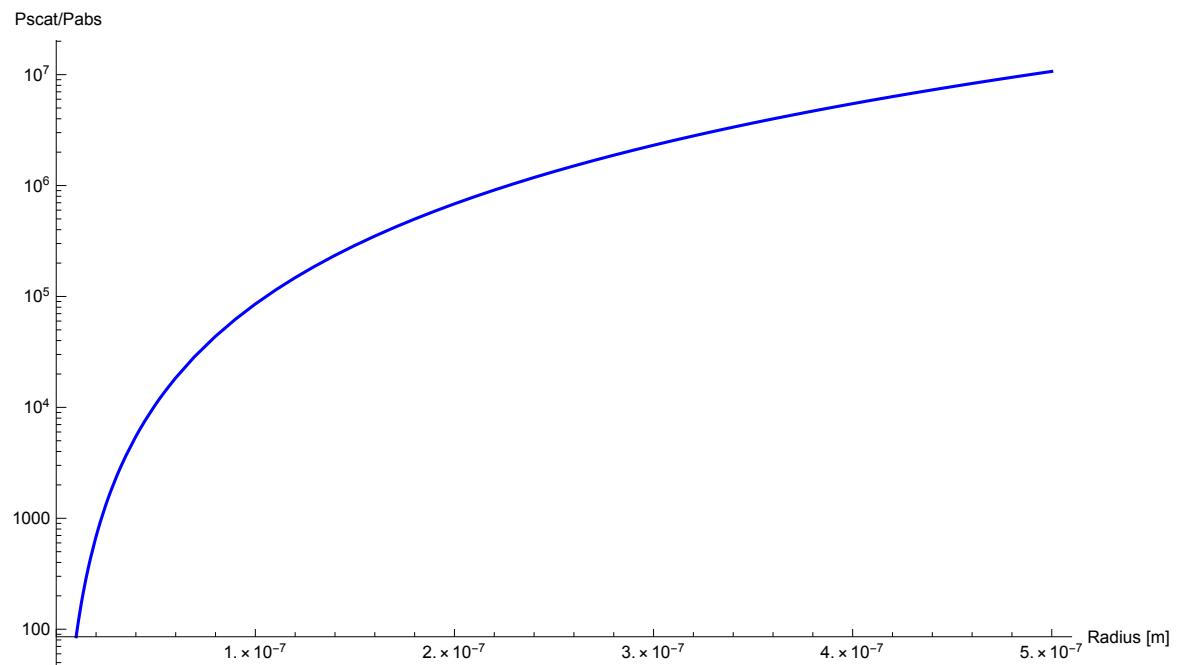
```

CavityAbs = LogLogPlot[Pabs //. Cnst //. CavityPara,
    {Radius, 10 × 10-9, 500 × 10-9}, PlotStyle → {Dashed, Blue}];
CavityScat = LogLogPlot[PScat //. Cnst //. CavityPara,
    {Radius, 10 × 10-9, 500 × 10-9}, PlotStyle → {Dashed, Red}];
ParaAbs = LogLogPlot[Pabs //. Cnst //. SotonPara,
    {Radius, 10 × 10-9, 500 × 10-9}, PlotStyle → {Blue}];
ParaScat = LogLogPlot[PScat //. Cnst //. SotonPara,
    {Radius, 10 × 10-9, 500 × 10-9}, PlotStyle → {Red}];
teqP = Graphics[{PointSize[Large], Orange, Point[
    {Log[Pabs //. Cnst //. SotonPara /. {Radius → 50 × 10-9}], Log[50 × 10-9]}}]}];
Show[CavityAbs, CavityScat, ParaAbs, ParaScat, teqP, PlotRange → All,
    AxesLabel → {"Radius (m)", "Power (W)"}, PlotStyle → Large]

```



```
LogPlot[PScat/Pabs /. Cnst //. SotonPara, {Radius, 10×10-9, 500×10-9},  
PlotStyle -> {Blue}, AxesLabel -> {"Radius [m]", " Pscat/Pabs"}]
```



Thermal Force Noise

```

Fnoise := Sqrt[ $\frac{4 \text{kB} T m \Omega}{Q}$ ]

TEQpara := { $\lambda \rightarrow 1550 \times 10^{-9}$ ,  $\Omega \rightarrow 2\pi 1 \times 10^3$ ,  $f_0 \rightarrow c/\lambda$ ,  $\eta c \rightarrow 0.0005$ ,  $\omega_0 \rightarrow 2\pi f_0$ ,
Radius  $\rightarrow 50 \times 10^{-9}$ , NA  $\rightarrow 0.997$ , k  $\rightarrow \omega_0/c$ , m  $\rightarrow \rho 4\pi \text{Radius}^3/3$ ,
 $\rho \rightarrow 1800$ ,  $\Gamma \rightarrow 0.619 ((9\pi)/\text{Sqrt}[2]) ((\eta \text{air} d^2)/(\rho \text{kB} T_0)) (\text{Pgas}/\text{Radius})$ ,
Pgas  $\rightarrow 100 \times 10^{-10}$ ,  $\eta \text{air} \rightarrow 18.2 \times 10^{-6}$ , d  $\rightarrow 0.375 \times 10^{-9}$ ,
 $T_0 \rightarrow 300$ , w0  $\rightarrow \frac{\lambda}{\pi \text{NA}}$ ,  $\gamma c \rightarrow \frac{\text{Radius}}{\omega_0}$ } // . Cnst

Fnoise // . {T  $\rightarrow 300 \times 10^{-3}$ , Q  $\rightarrow \frac{\Omega}{\Gamma}$ } // . TEQpara // . Cnst
3.64246  $\times 10^{-24}$ 

```

Incident Power

The σ_{scat} is the scattering cross - section due to Rayleigh scatter and I_0 the incident laser intensity determined by P_0 the incident laser power and numerical aperture (NA).

The equation that tells us the detection laser power required to satisfy the condition of being able to reach ground state can be described by:

$$P_{\text{inc}} = ((3 \times \sqrt{10 \pi \gamma m c^2 \epsilon_0^2}) / (k^6 N A^2 \alpha^2)) \frac{\Omega}{\omega_0} \sqrt{\frac{1}{\eta_c}}$$

where α is the polarizability of the particle, Ω the oscillator frequency and ω_0 the frequency of light, and η_c is the detector efficiency. γ is the total damping due to feedback + radiation pressure + gas collision.

Key Parameters

```

Cnst := {hbar → 1.05 × 10-34, c → 3 × 108, n → 1.45, ε0 → 8.8 × 10-12, kB → 1.38 × 10-23}
NovotnyPara := {λ → 1064 × 10-9, Ω → 2 π 150 × 103, γ → 2 π 269, f0 → c / λ, ηc → 1,
ω0 → 2 π f0, Radius → 50 × 10-9, NA → 0.9, P0 → 70 × 10-3, k → ω0/c, m → 1.14 × 10-18}
OurPara := {λ → 1550 × 10-9, Radius → 100 × 10-9, Ω → 2 π 1 × 103,
γ → 2 π 269, f0 → c / λ, ηc → 0.0005, ω0 → 2 π f0,
NA → 0.997, ρ → 1800, m → ρ 4 π Radius3/3, k → ω0/c}

Pinc := 
$$\frac{3 \sqrt{\frac{5}{2}} c^2 m (2 + n^2)^2 \gamma \sqrt{\frac{1}{\eta c}} \Omega}{8 k^6 (-1 + n^2)^2 N A^2 R a d i u s^6 \omega_0}$$


Pinc 1 × 103 mW // . NovotnyPara // . Cnst
Pinc 1 × 103 mW // . OurPara // . Cnst
1.41123 mW
0.493314 mW

```

From the above it is apparent that for Novotny's case he requires roughly 70 mW to reach this regime, whilst changing the NA and wavelength of light allows you to use greater power of 117 mW of laser power.

Ratio of Scatter Force and Photon Recoil

If you have a particle in a trap that scatters a certain amount of power, evidently the incident light will impart a Photon pressure on the particle. What is the strength of this force acting on the particle.

```

OpticalParameters := {wθ → λ / (π NA), zR → π wθ² / λ, Iθ → 2 Pθ / (π wθ²)}
w[z_] := wθ Sqrt[1 + (z/zR)²]
R[z_] := z [1 + (zR/z)²]
Intensity := Iθ (wθ / w[z])² Exp[-2 r² / w[z]²]
(*The use of n2 is dependant on the material. Change
this if you change the particle or the wavelength of light*)
Fscat := (128 π⁵ n1 a⁶ / (3 c λ⁴)) (m² - 1)² / (m² + 2)² Intensity //.
{z → 0, r → 0, a → Radius, n1 → 1} //.
OpticalParameters // Cnst

```

The final form of the scattering force can be written as:

$$F_{\text{scat}} = 2.7 \times 10^{-4} n_1 \frac{(m^2 - 1)^2}{(m^2 + 1)^2} \frac{\text{NA}^2 P_0}{\lambda^6} \text{Radius}^6$$

where $m = \frac{n_2}{n_1}$ with n_1 and n_2 are the refractive indices of the environment (air) and the particle (silica). NA is the numerical aperture, λ is the wavelength of light and P_0 is the incident power.

In this case, if we consider the incident $P_0 = P_{\text{inc}}$ then we can work out the scattering force imparted on the particle:

$10 \times 10^{-9} \text{ nm}$	$25 \times 10^{-9} \text{ nm}$	$50 \times 10^{-9} \text{ nm}$	$100 \times 10^{-9} \text{ nm}$	$200 \times 10^{-9} \text{ nm}$
0	0	0	0	0
$4.90046 \times 10^{-6} \text{ fN}$	0.0011964 fN	0.0765697 fN	4.90046 fN	313.629 fN
0.000490046 fN	0.11964 fN	7.65697 fN	490.046 fN	31362.9 fN
0.00245023 fN	0.598201 fN	38.2848 fN	2450.23 fN	$156815. \text{ fN}$

The rows refer to the power P_0 at 0, 1 mW, 100 mW, 500 mW and the numbers in the table refer to

```
TEQpara := { $\lambda \rightarrow 1550 \times 10^{-9}$ ,  $\Omega \rightarrow 2\pi 1 \times 10^3$ ,  $\gamma \rightarrow 2\pi 269$  ,
 $f_0 \rightarrow c/\lambda$ ,  $\eta c \rightarrow 0.0005$ ,  $\omega_0 \rightarrow 2\pi f_0$ ,  $\text{Radius} \rightarrow 50 \times 10^{-9}$ ,  $\text{NA} \rightarrow 0.997$ ,
 $P_0 \rightarrow 0.5 \times 10^{-3}$ ,  $k \rightarrow \omega_0/c$ ,  $m \rightarrow \rho 4\pi \text{Radius}^3/3$ ,  $\rho \rightarrow 1800$ ,
 $r \rightarrow 0.619 ((9\pi)/\text{Sqrt}[2]) ((\eta \text{air} d^2)/(\rho k_B T_0)) (P_{\text{gas}}/\text{Radius})$ ,
 $P_{\text{gas}} \rightarrow 100 \times 10^{-10}$ ,  $\eta \text{air} \rightarrow 18.2 \times 10^{-6}$ ,  $d \rightarrow 0.375 \times 10^{-9}$ ,  $T_0 \rightarrow 300$ }
```

```
Grid[Table[Fscat  $1 \times 10^{15}$  FN // . TEQpara,
{P0, { $1 \times 10^{-6}$ ,  $500 \times 10^{-6}$ ,  $1 \times 10^{-3}$ }}, {Radius, { $50 \times 10^{-9}$ ,  $200 \times 10^{-9}$ }}], Frame -> All]
```

0.0000765697 FN	0.313629 FN
0.0382848 FN	156.815 FN
0.0765697 FN	313.629 FN

```
Insert[ReplacePart[Grid[{{0.0000765697 FN, 0.313629 FN},
{0.0382848 FN, 156.815 FN}, {0.0765697 FN, 313.629 FN}}], Frame -> All],
1 -> Prepend[First[Grid[{{"1  $\mu$ W", 0.0000765697 FN, 0.313629 FN},
{"500  $\mu$ W", 0.0382848 FN, 156.815 FN}, {"1 mW", 0.0765697 FN, 313.629 FN}},
Frame -> All]], {"P0", "50 nm", "200 nm"}]],
{Background -> {None, {GrayLevel[0.7], {White}}}},
Dividers -> {Black, {2 -> Black}}, Frame -> True,
Spacings -> {2, {2, {0.7}, 2}}], 2]
```

P0	50 nm	200 nm
1 μ W	0.0000765697 FN	0.313629 FN
500 μ W	0.0382848 FN	156.815 FN
1 mW	0.0765697 FN	313.629 FN

Paul Trap

The **Paul trap** potential can be given by the following equation:

$$U_{\text{ion}} = \frac{1}{2} m \omega_{\text{ion}}^2 r_e^2$$

where m is the mass of the particle, ω_{ion} the angular frequency of oscillation, r_e the distance between the electrodes. Alternatively the force for a quadrupole ion trap is given by:

$$F_{\text{ion}} = -\frac{2e}{d_0} (V_{\text{dc}} + V_{\text{rf}} \cos(\omega_{\text{ion}} t)) x$$

where e , is the electric charge, d_0 a size parameter constant, V_{dc} and V_{rf} are the voltages of the applied DC and RF fields, whilst ω_{ion} is the driving frequency of the RF applied along the x direction of the system.

```

IonPara := {re → 500 × 10-6, ωion → 2 π 1 × 103}
U := 1/2 m ωion2 re2
Fion := - 2 e / d0 (Vdc + Vrf Cos[ωIon t])
U / kB T // . IonPara // . OurPara // . Cnst /. T → 300 // N
3.41238 × 108

```

References

- [1] Jain, V., Gieseler, J., Moritz, C., Dellago, C., Quidant, R. and Novotny, L., 2016. Direct measurement of photon recoil from a levitated nanoparticle. *Physical review letters*, 116 (24), p .243601.
- [2] PDB450C(-AC) https://www.thorlabs.com/newgroupage9.cfm?objectgroup_id=5201
- [3] https://www.hamamatsu.com/resources/pdf/ssd/ingaas_kird0005e.pdf

Status of the LNF activities on electronics

TEQ MEETING
Southampton, June 22 2018

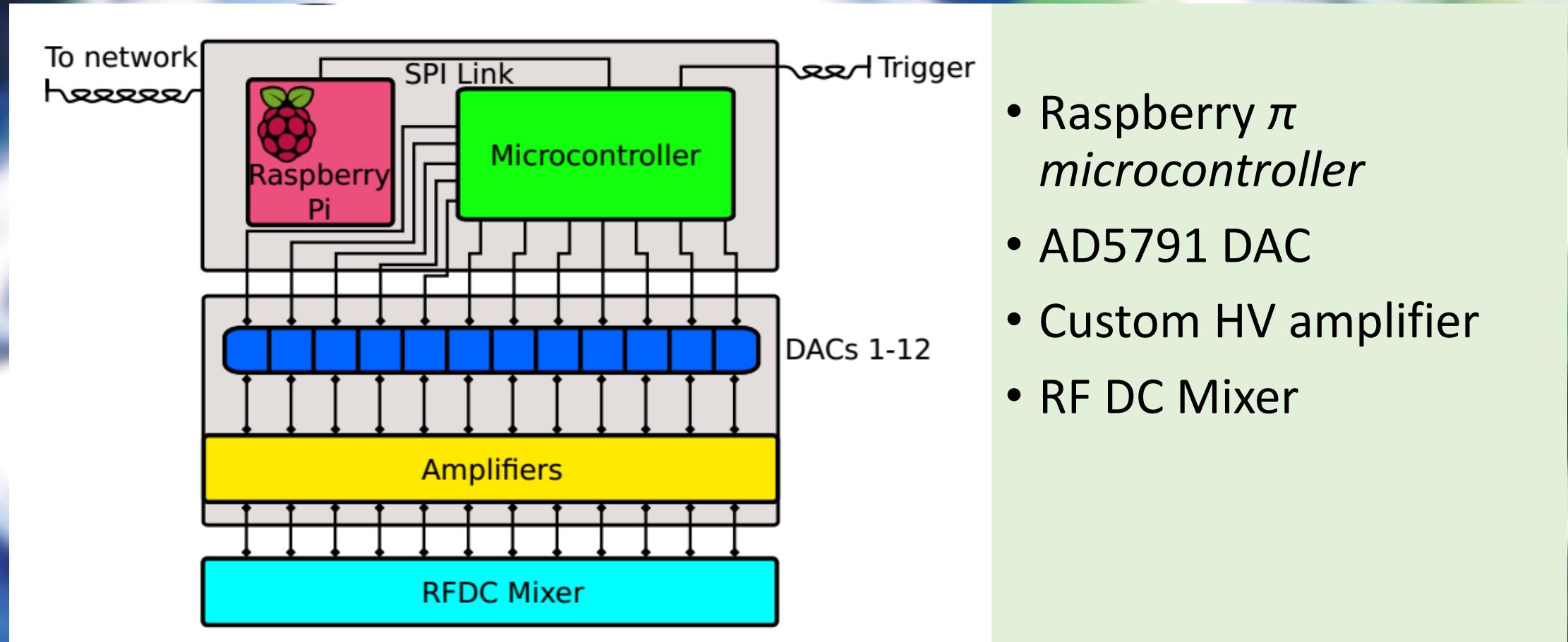
Power Supply Requirements

Due to its ambitious finality, the Particle Trap Power Supply must respond to the following specifics:

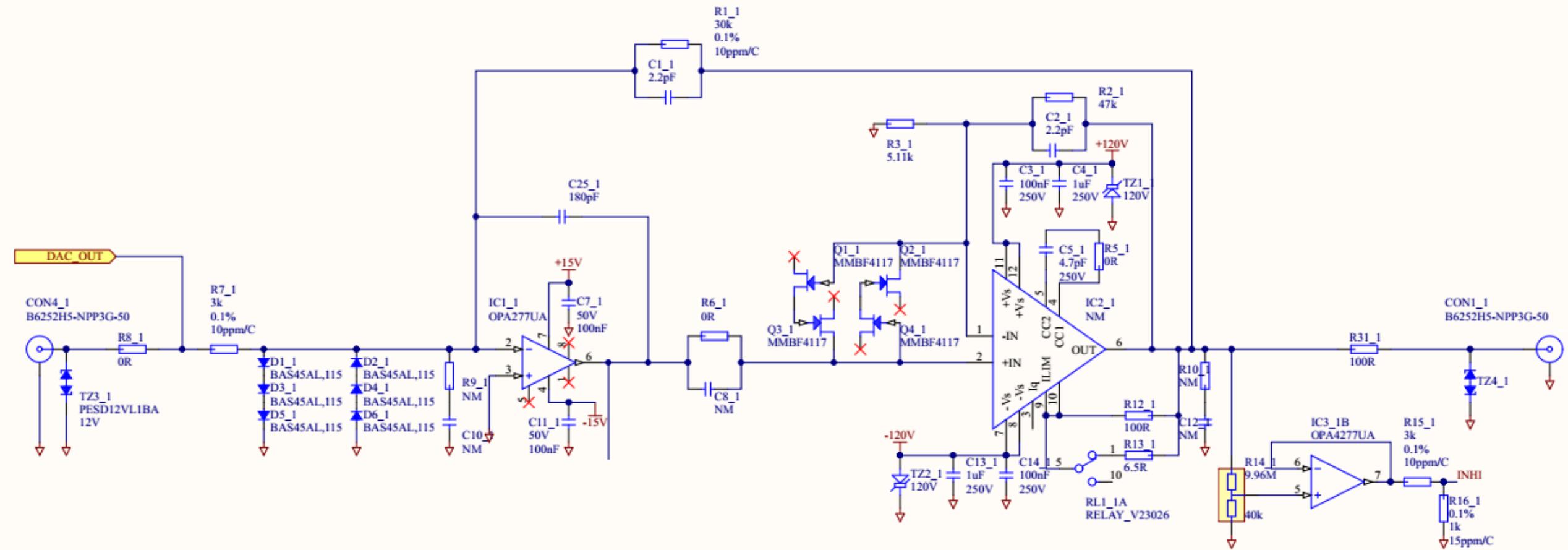
- Max amplitude 50V
- Typical Bandwidth 10kHz
- Maximum output Noise $22\text{nV}/\sqrt{\text{Hz}}$

$$(2) \quad S_V^{\text{DC}}(\omega) \leq 5 \cdot 10^{-16} \text{ V}^2/\text{Hz} \quad @ \begin{array}{l} \omega = 100 - 1000 \text{ Hz} \\ \text{and } V_{\text{DC}} = 50 \text{ V} \end{array}$$

Current Power Supply Apparatus



Amplifier Schematic



Power Supply Requirements

Current design has been thoroughly reviewed to check if specifics were respected.

DC GAIN = 10 OK

Bandwidth = 300kHz OK

NOISE...

Among all specifics, noise is indeed the most critical.

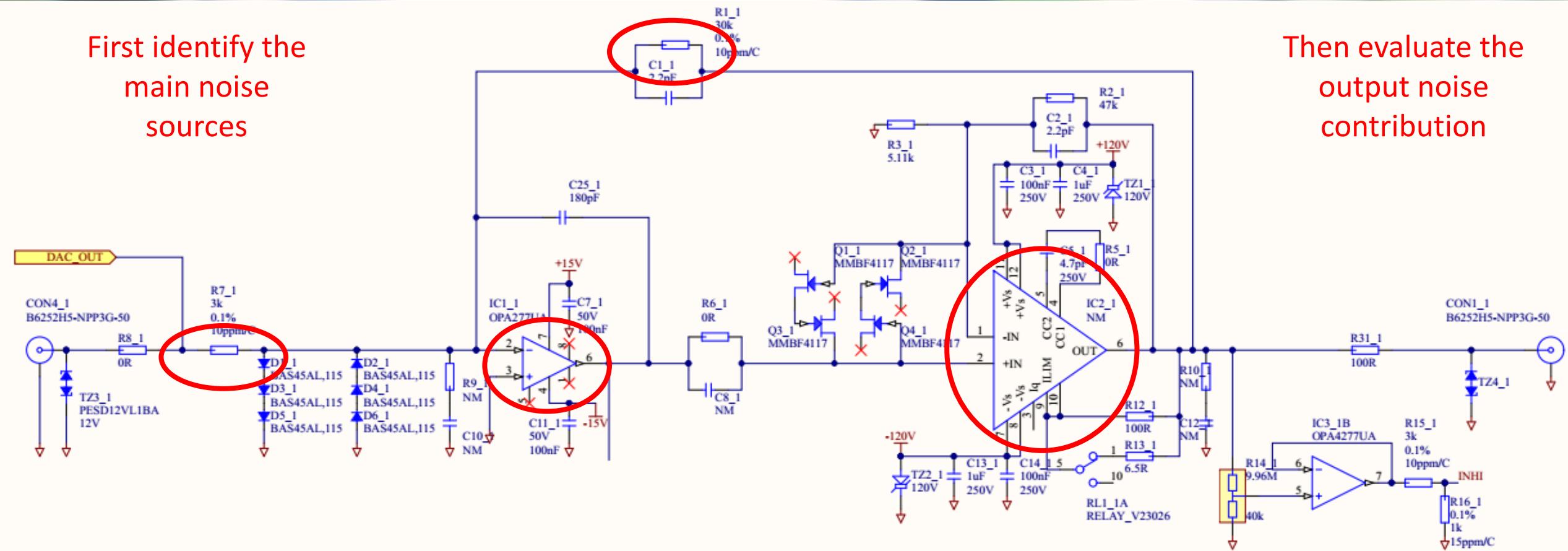
Amplifier NOISE analysis

NOISE analysis include:

- Identify the main sources of noise
- Calculate Noise GAIN for each source
- Output Noise Estimation for each source
- Quadratic Sum of all Noise contribution

Amplifier NOISE analysis

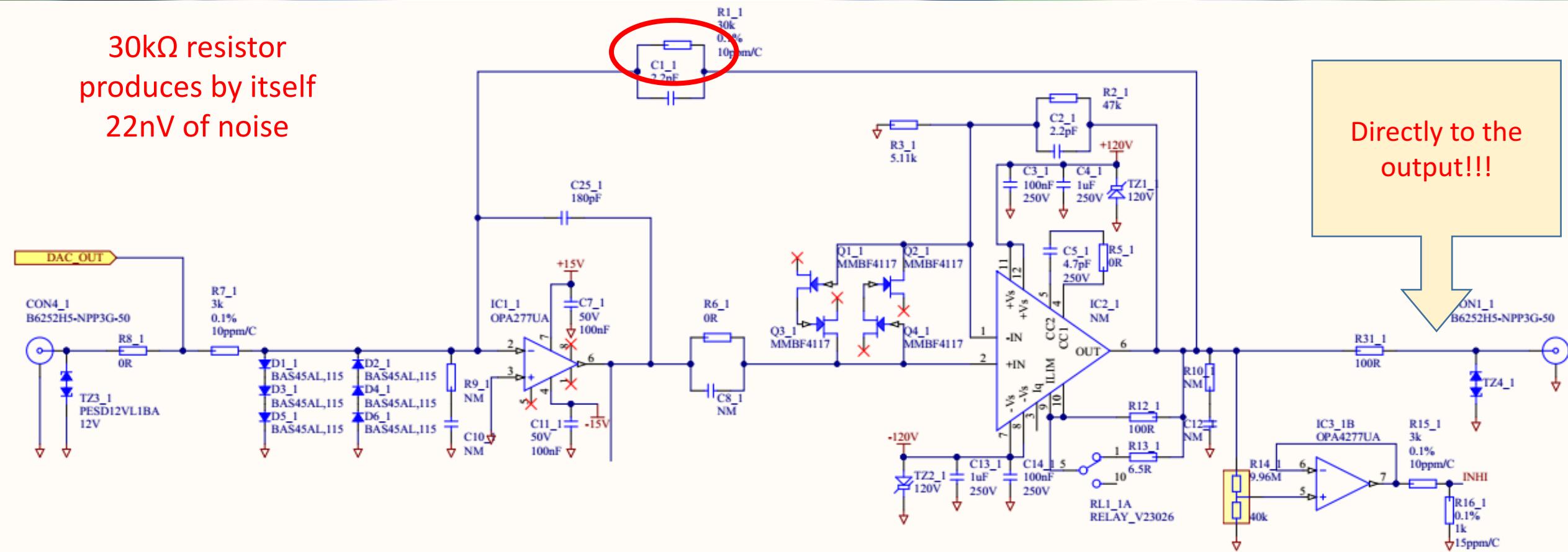
First identify the main noise sources



Then evaluate the output noise contribution

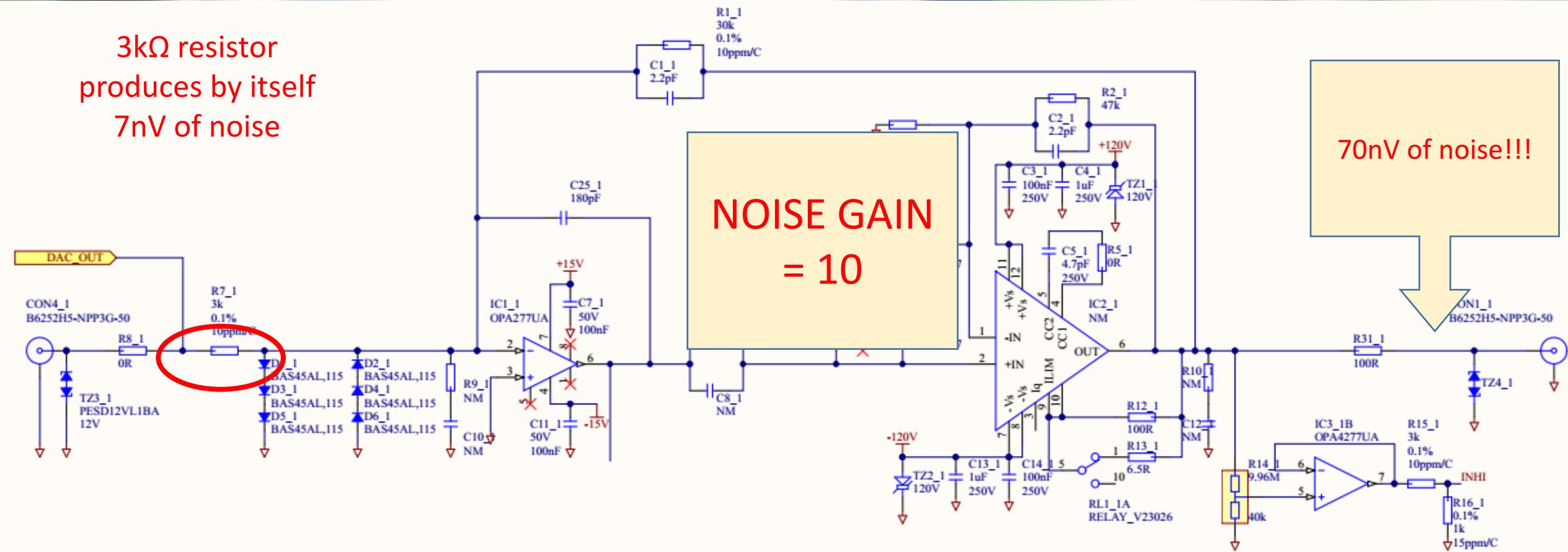
Amplifier NOISE analysis

30k Ω resistor
produces by itself
22nV of noise

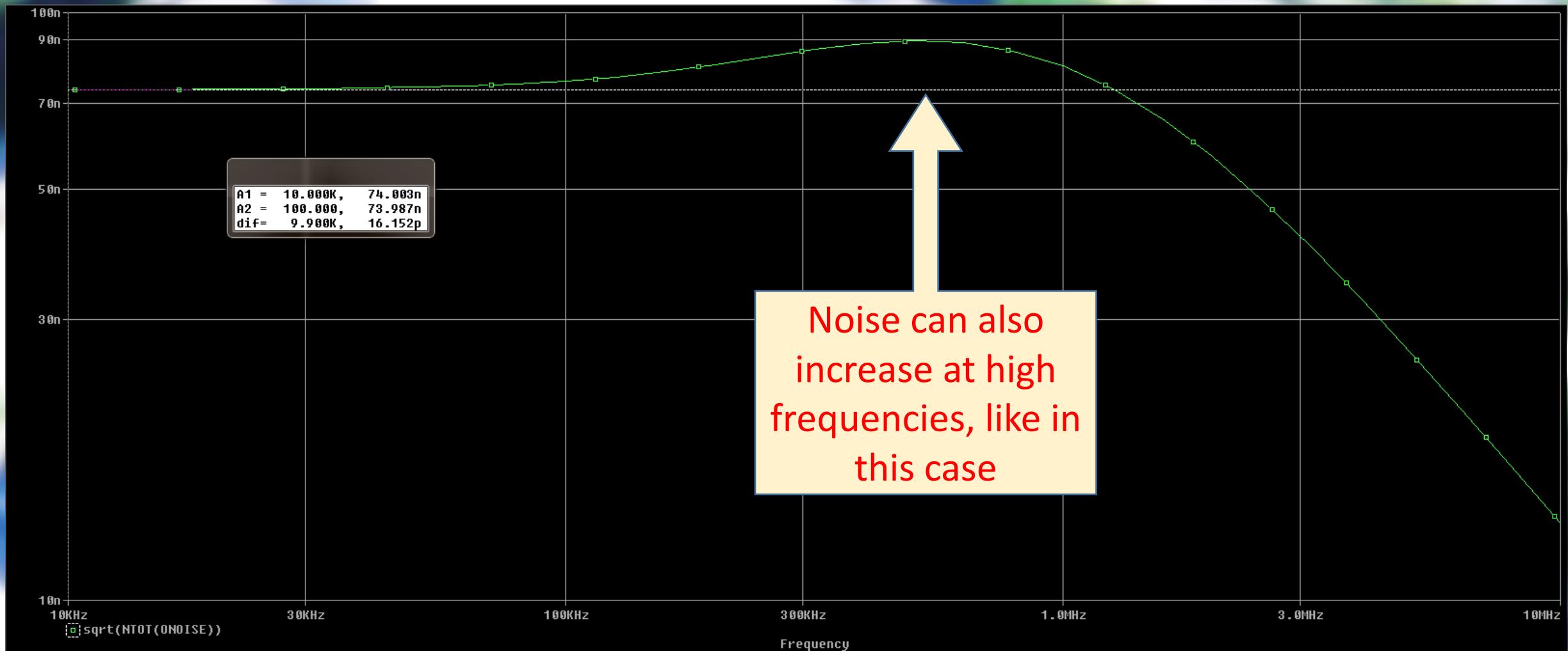


Amplifier NOISE analysis

3kΩ resistor
produces by itself
7nV of noise

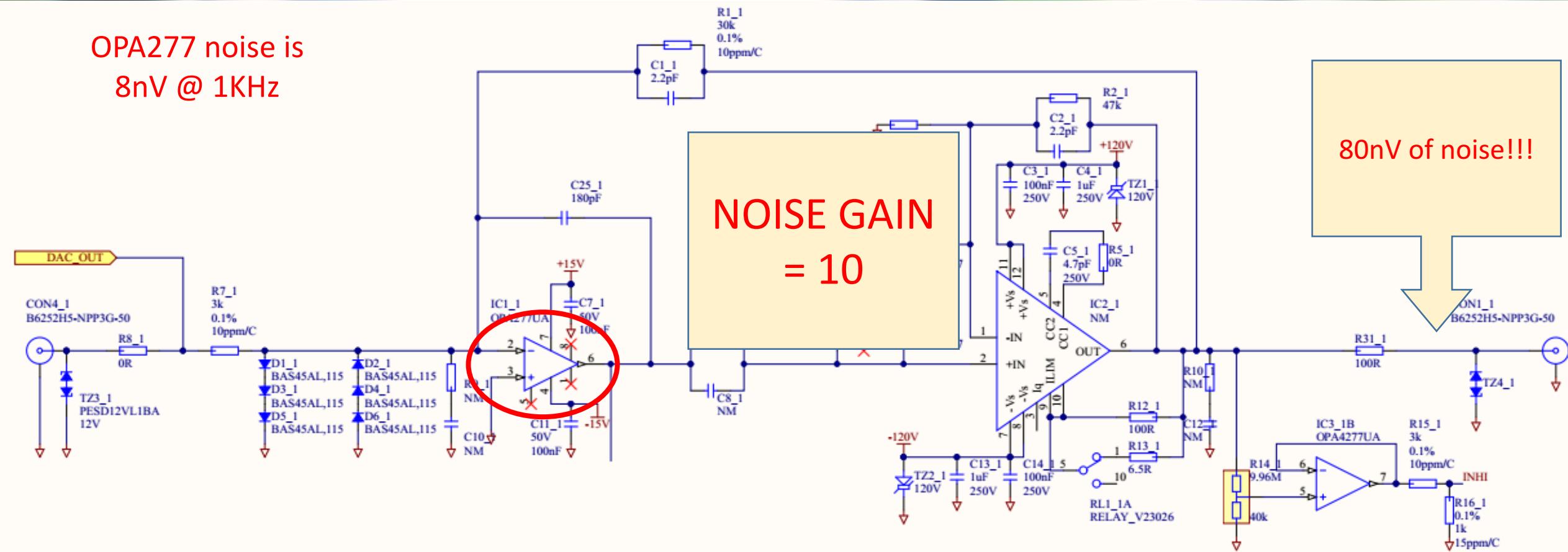


Amplifier NOISE analysis



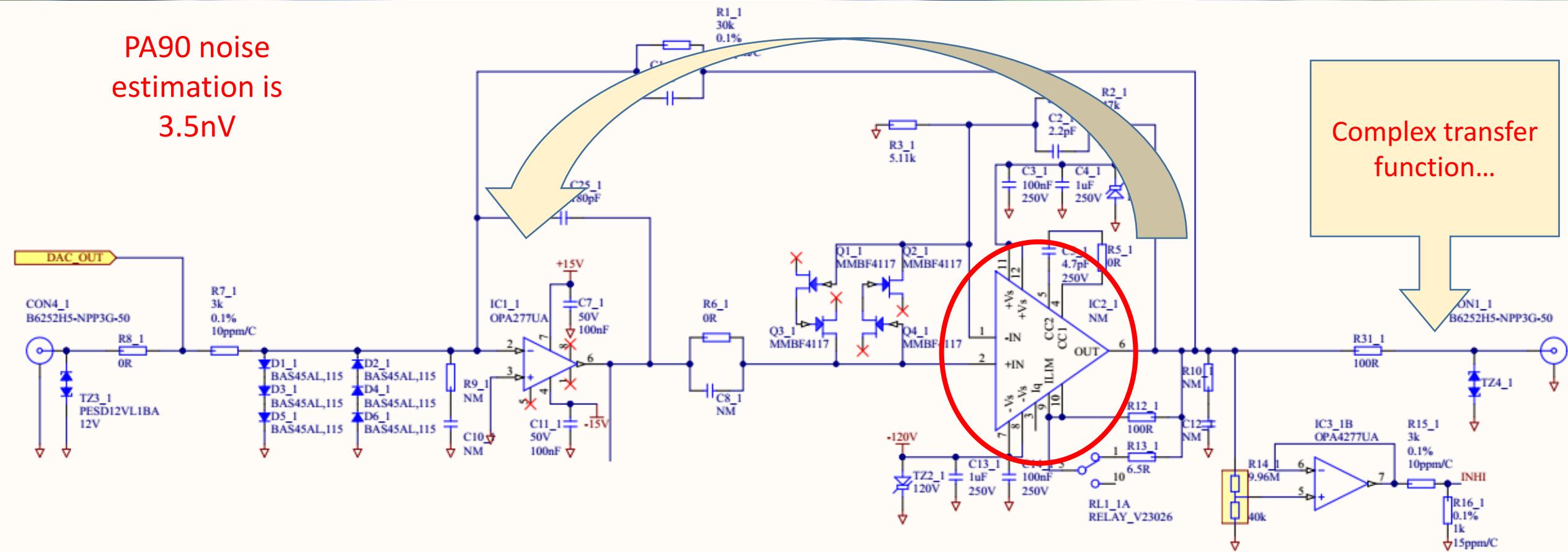
Amplifier NOISE analysis

OPA277 noise is
8nV @ 1KHz

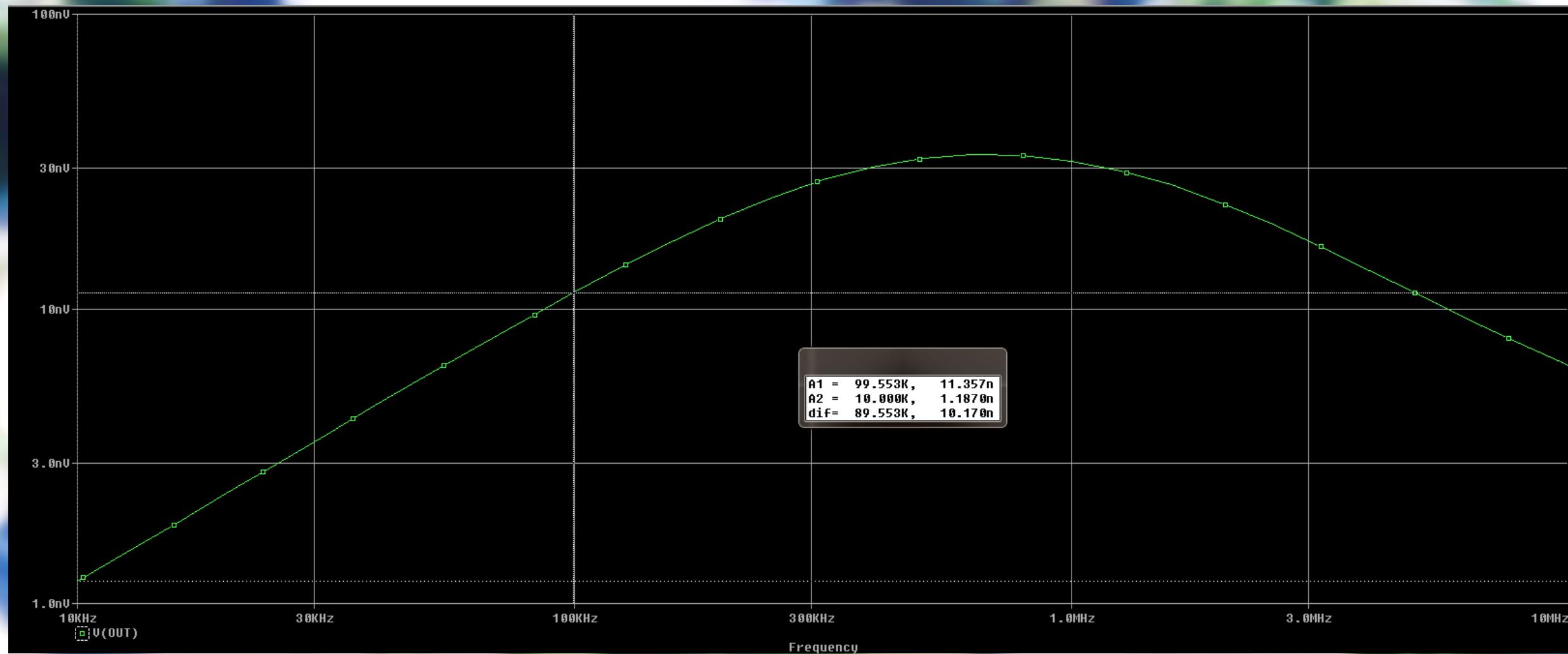


Amplifier NOISE analysis

PA90 noise
estimation is
3.5nV



Amplifier NOISE analysis



Power Supply Requirements

Current design has been thoroughly reviewed to check if specifics were respected.

DC GAIN = 10 OK

Bandwidth = 300kHz OK

TOTAL NOISE MORE THAN 100nV/ $\sqrt{\text{Hz}}$!

BUT WE CAN SOLVE!

Power Supply Adjustements

Current design can be salvaged with a few expedients:

- Reduce resistor values, maintaining DC Gain
- Increase capacitor values, maintaining time constants
- Replace OPA277 with a low noise amplifier
- Place on the output an additional Low Pass Filter at desired BW

Power Supply Adjustements

Possible solution is to replace:

- $R_1=1K$ $R_7=100R$ $R_2=10K$ $R_2=1K$ $C_1=68pF$ $C_2=10pF$
- OPA277 with LT6018 (same package, 1nV of noise)
- Add 100kHz low pass filter

Result is...

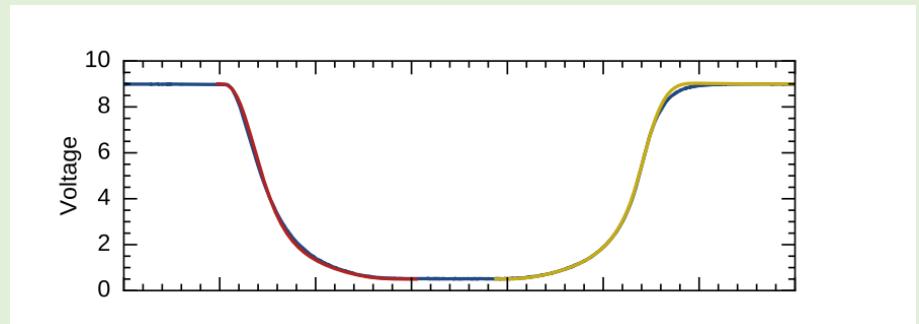
15nV/VHz of noise!

But still we are not considering the signal source...

SIGNAL SOURCE (DAC)

In the current application a "bath curve" dynamics is required

- Signal source is AD5791 DAC
- From datasheet its noise is $7.5\text{nV}/\sqrt{\text{Hz}}$
- By using this source the output noise would be $75\text{nV}/\sqrt{\text{Hz}}$ at least!
- The maximum source noise allowed is $1.5\text{nV}/\sqrt{\text{Hz}}$



SIGNAL SOURCE (DAC)

Signal generator must be replaced for noise and other issues.

A better candidate is AD9106 waveform generator.

- Current mode DAC
- High accuracy and stability
- From datasheet noise is $0,999\text{nV}/\sqrt{\text{Hz}}$
- SPI Programmable device
- 4 channels
- Low cost (20€ per chip)
- Evaluation board with labview interface
- USB connection

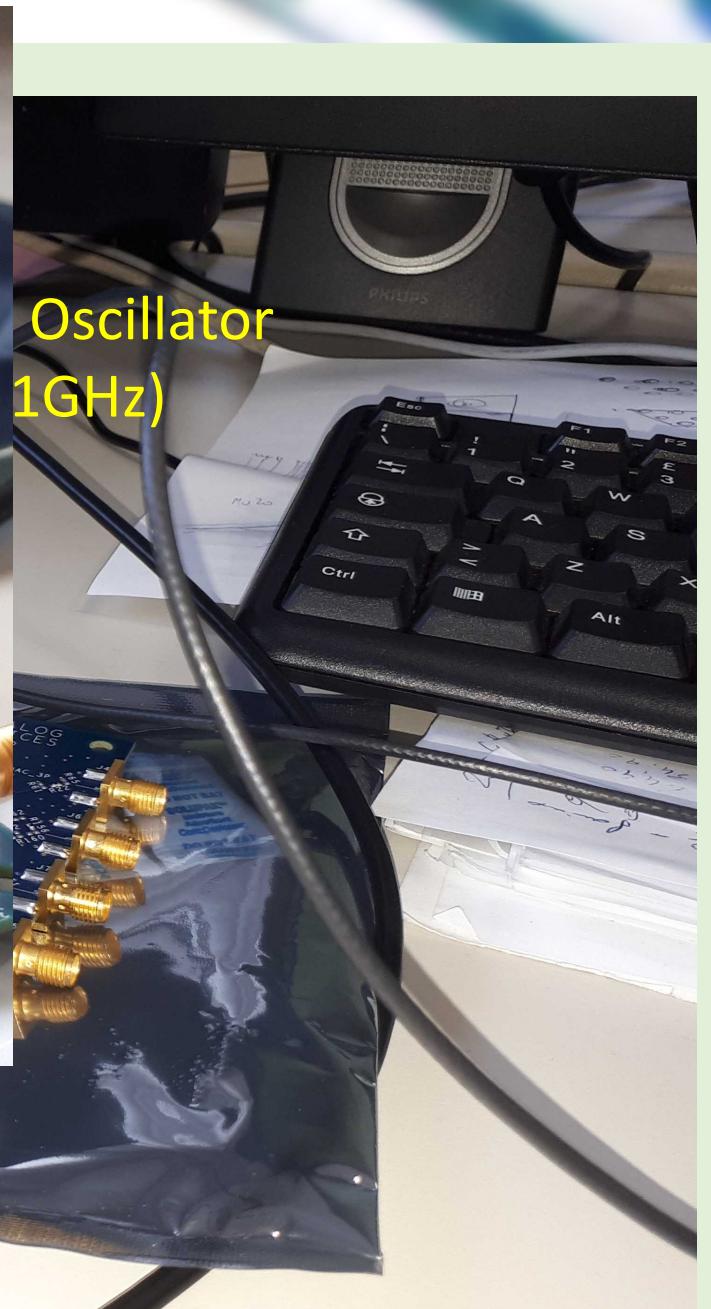
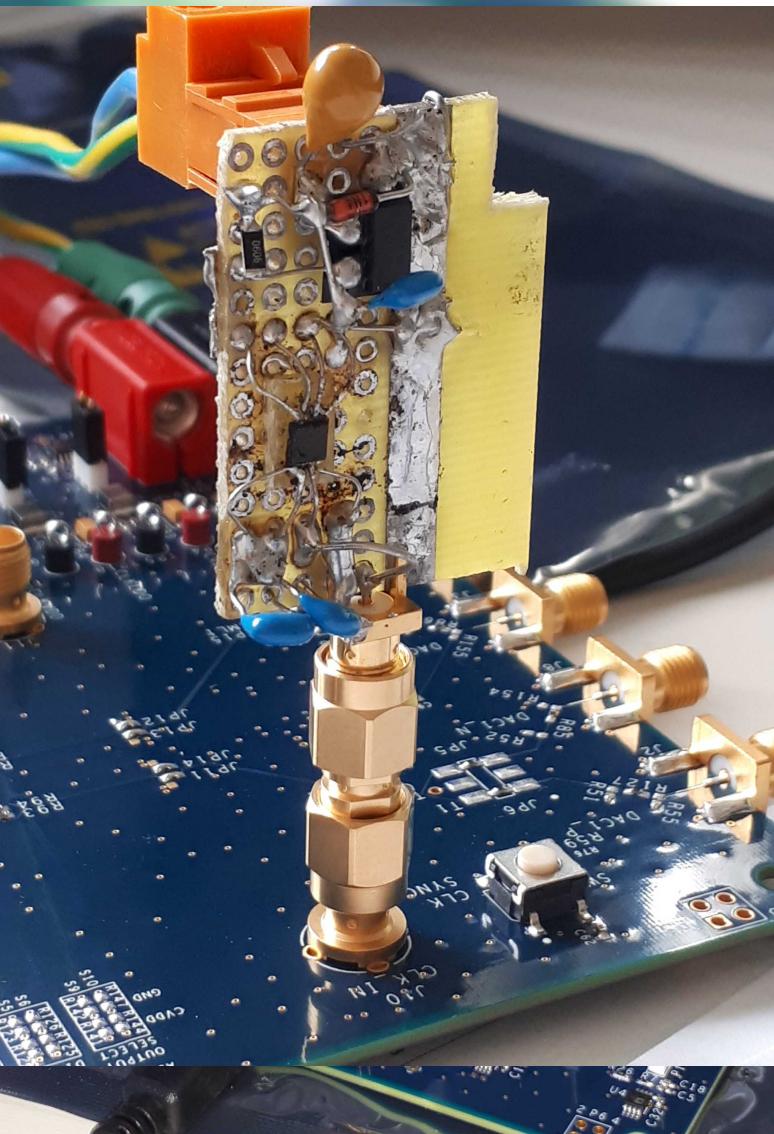
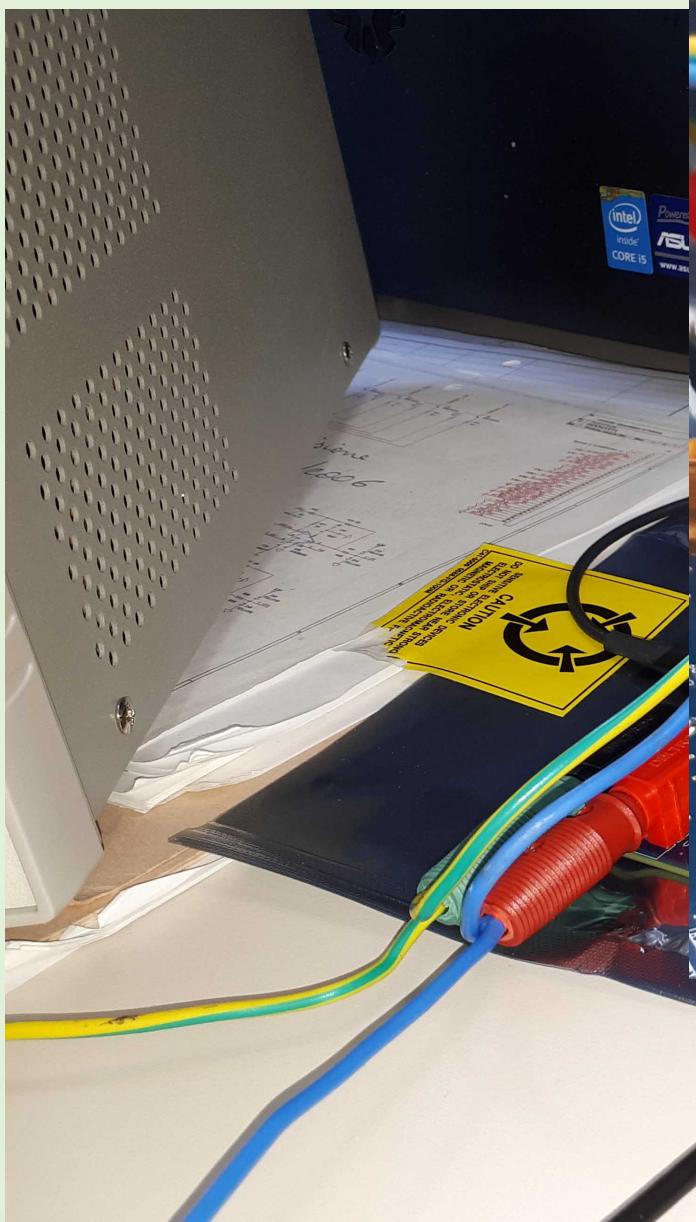
SIGNAL SOURCE (DAC)



Evaluation board has already been purchased and currently under test.

DRAWBACKS:

- Evaluation board costly (500€)
- External Clock reference (1Ghz typ.)
- Labview interface not user friendly!
- No manual included!

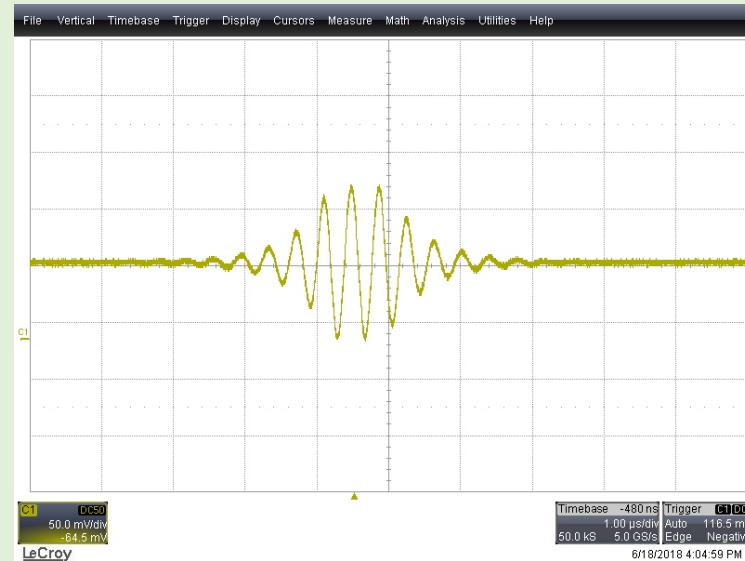
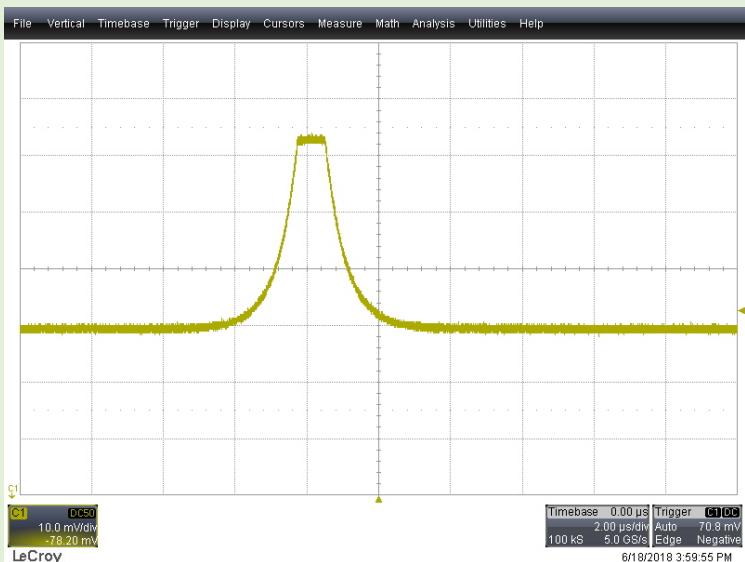
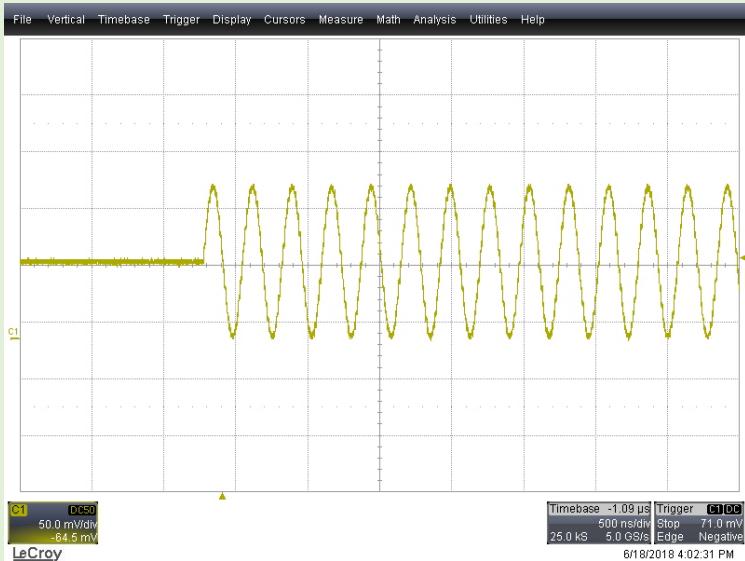


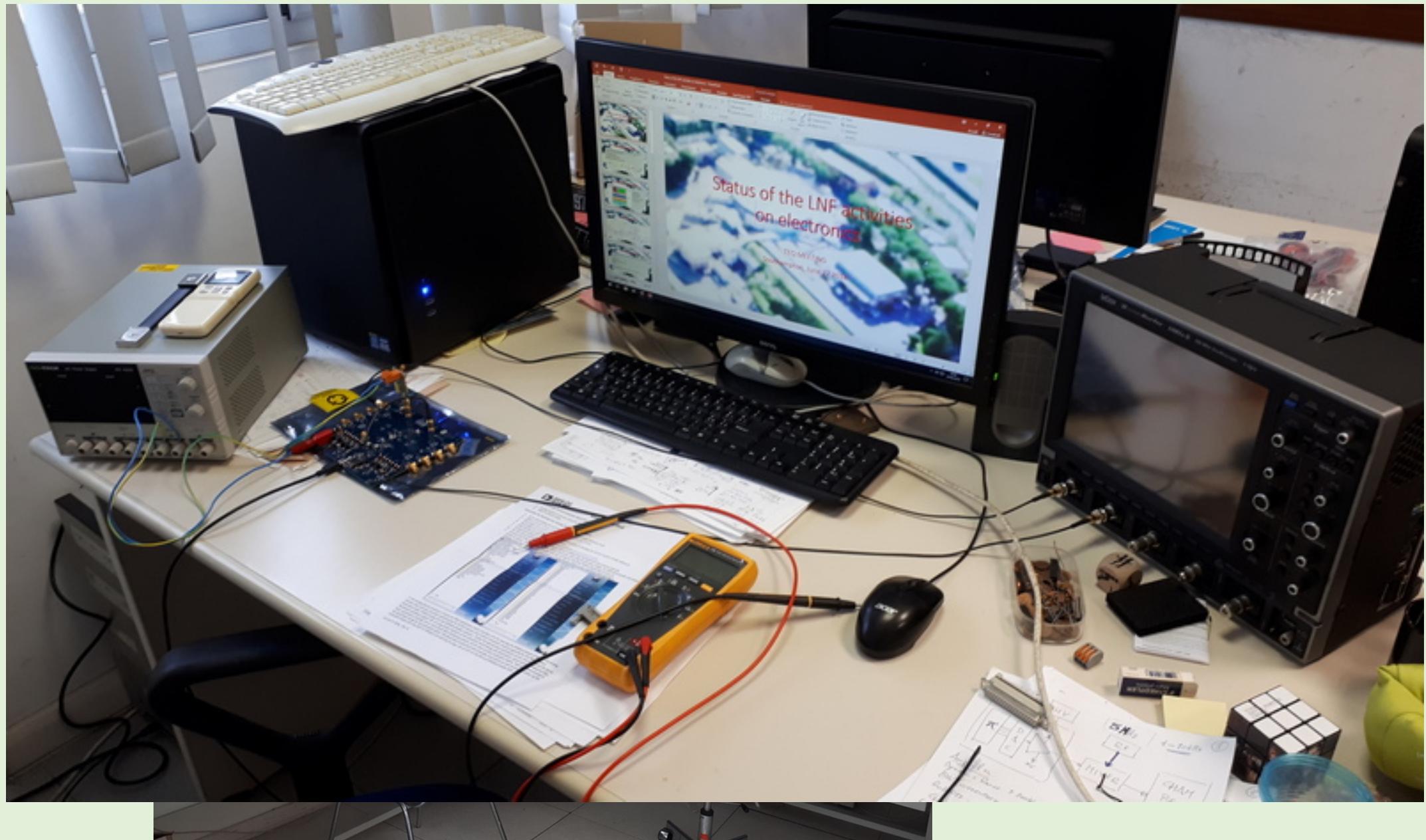
SIGNAL SOURCE (DAC)

NEXT STEPS ARE:

- Signal pattern generation
- Noise tests
- Output filter design
- Integration in current set-up
 - Using current board
 - Developing new layout with specific features

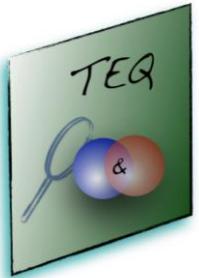
WAVEFORM SAMPLES





Grazie per l'attenzione!

TEQ MEETING
Southampton, June 22 2018



Testing the Large-Scale Limit of Quantum Mechanics (TEQ)



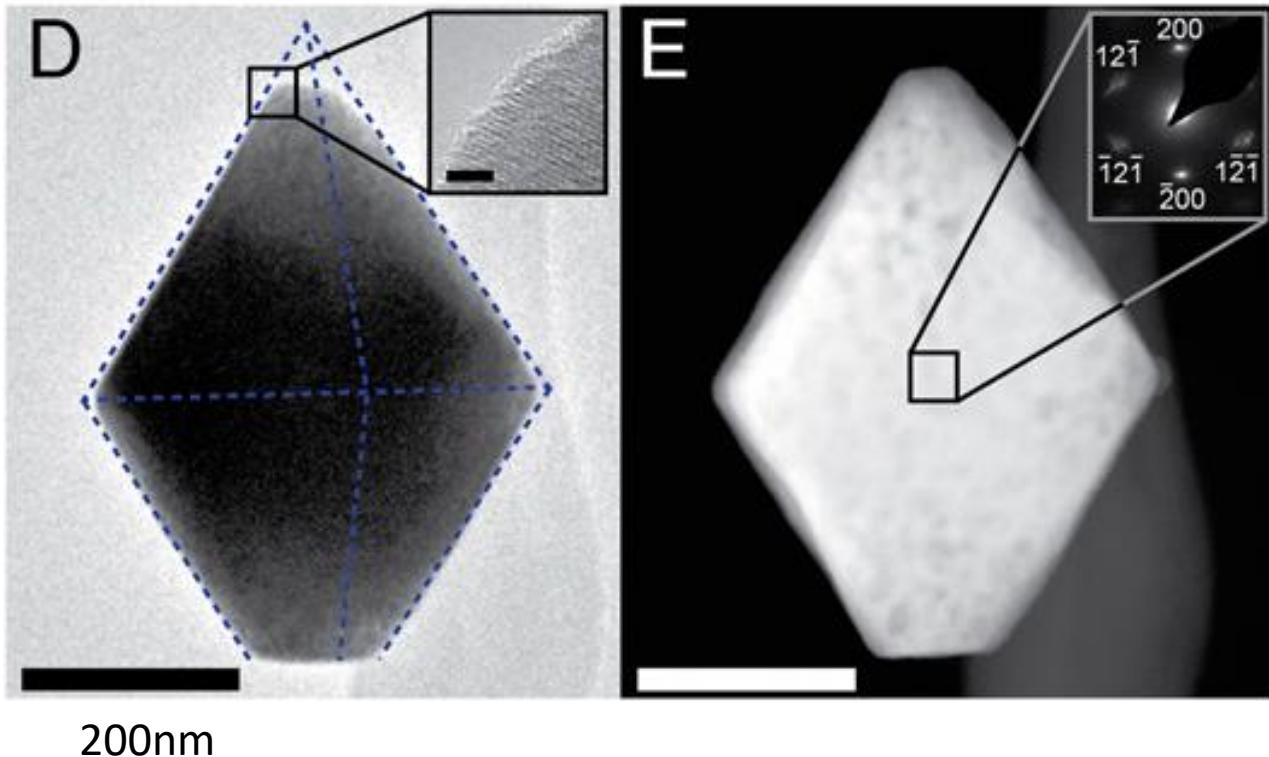
Synthesis of **Yb-doped LiYF₄** Colloidal Nanocrystals

Liberato Manna
Luca De Trizio
Francesco De Donato

Southampton – 22nd of June

Work Progress: 2nd of February 2018

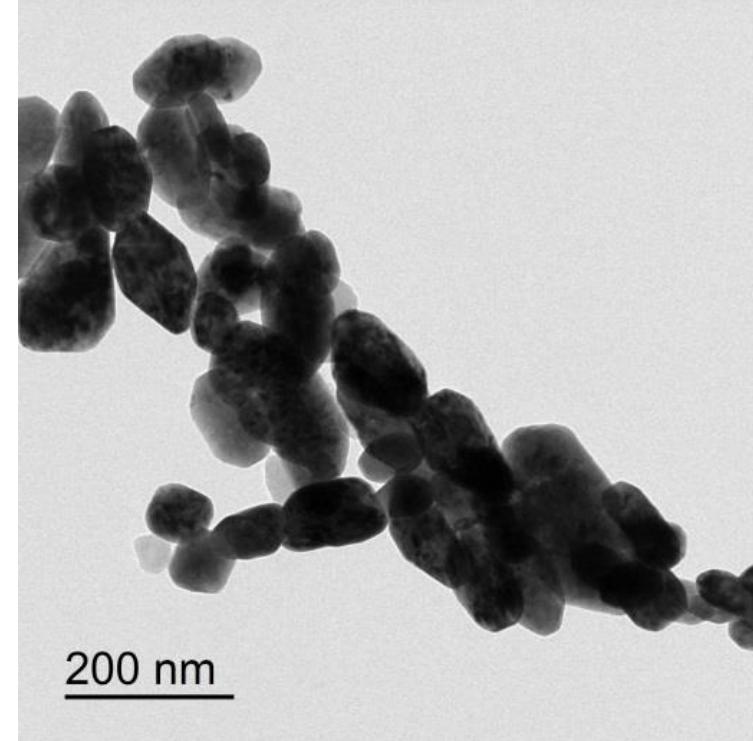
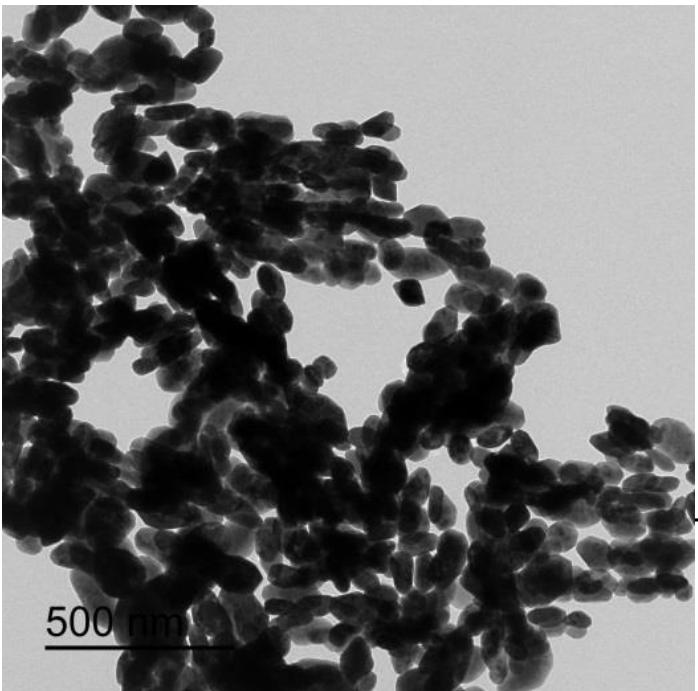
Reference synthesis protocol: Solvothermal Approach



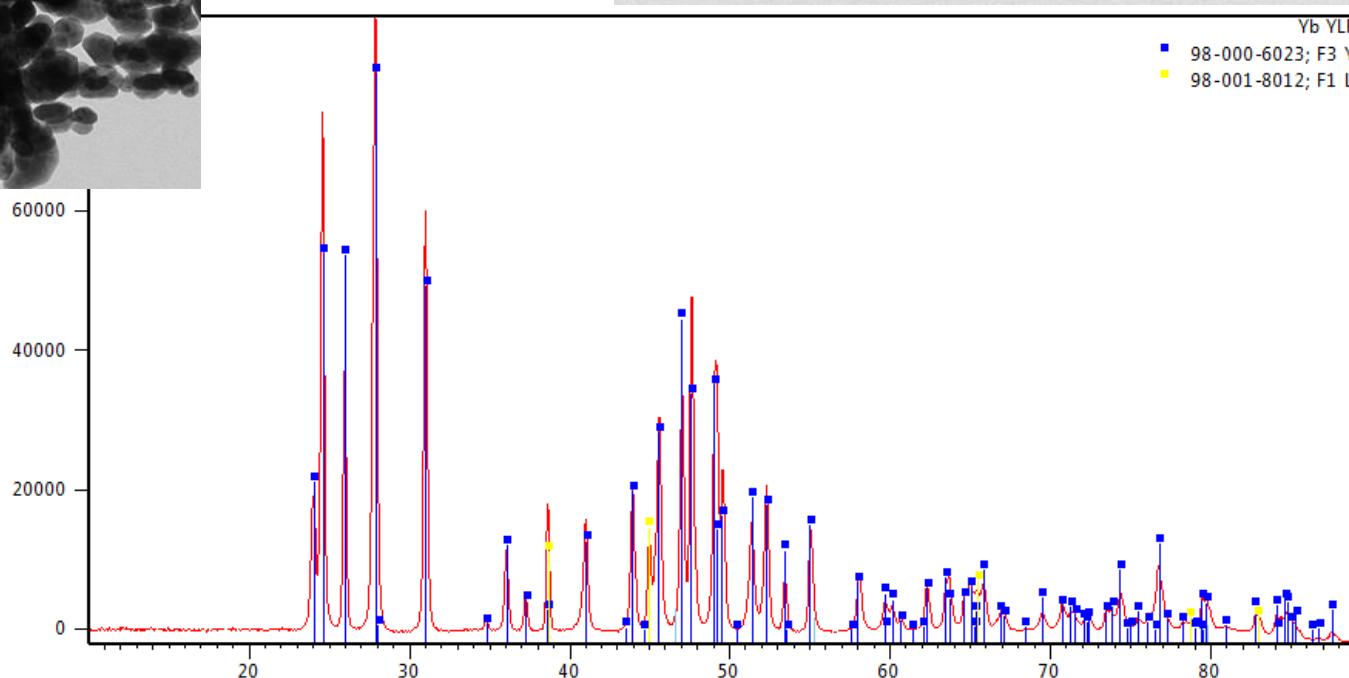
2% Er^{3+} , 10% Yb^{3+} : LiYF_4
10% Yb^{3+} : LiYF_4

Work Progress: 2nd of February 2018

Our Results: Solvothermal Approach

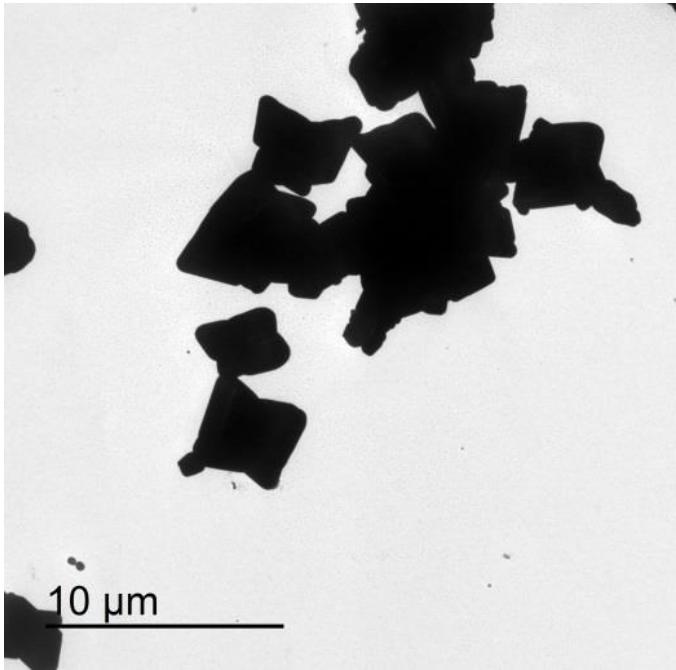


Yb:YLF Sample 2

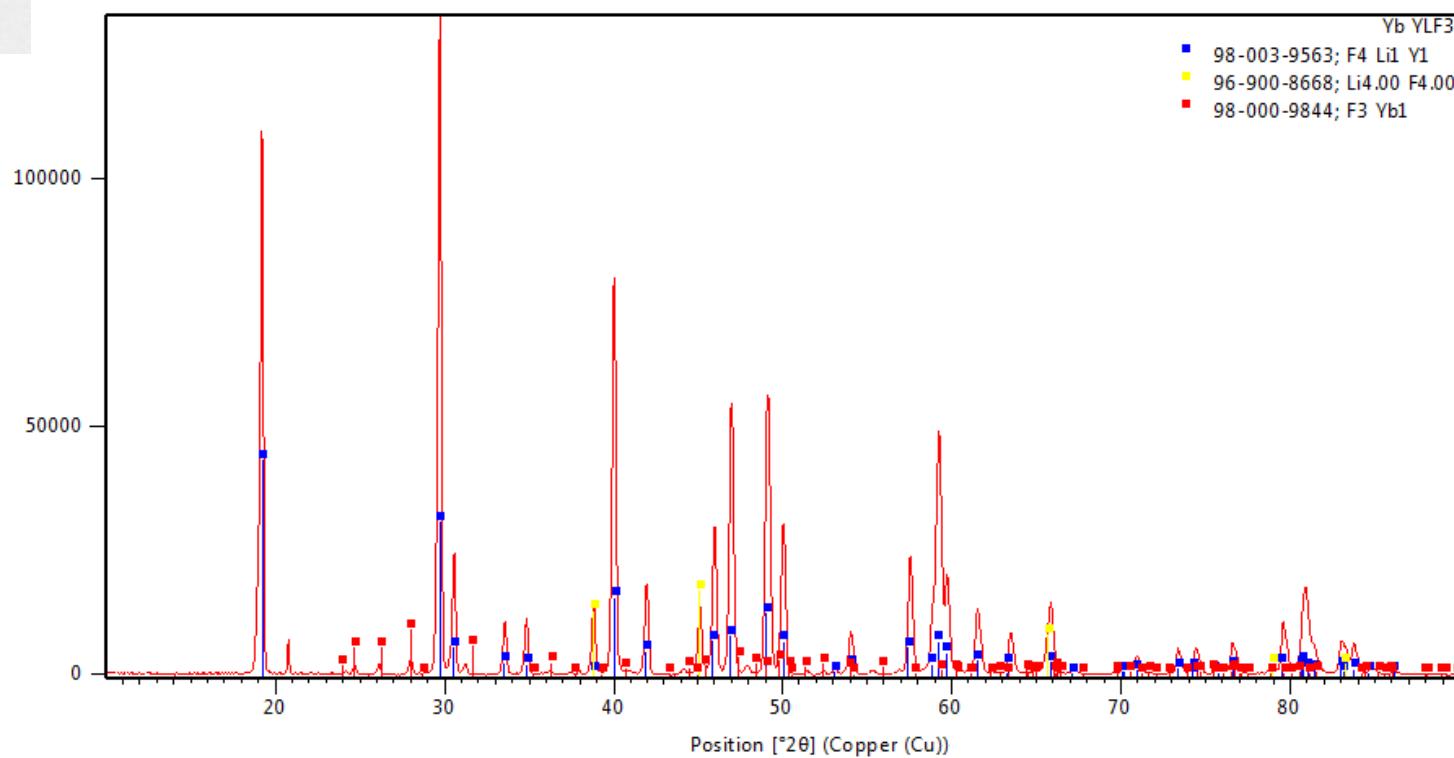
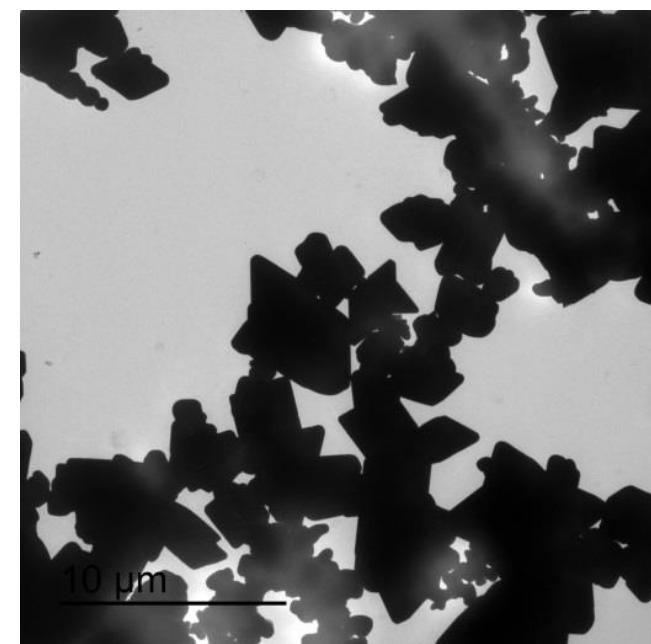


Our Results

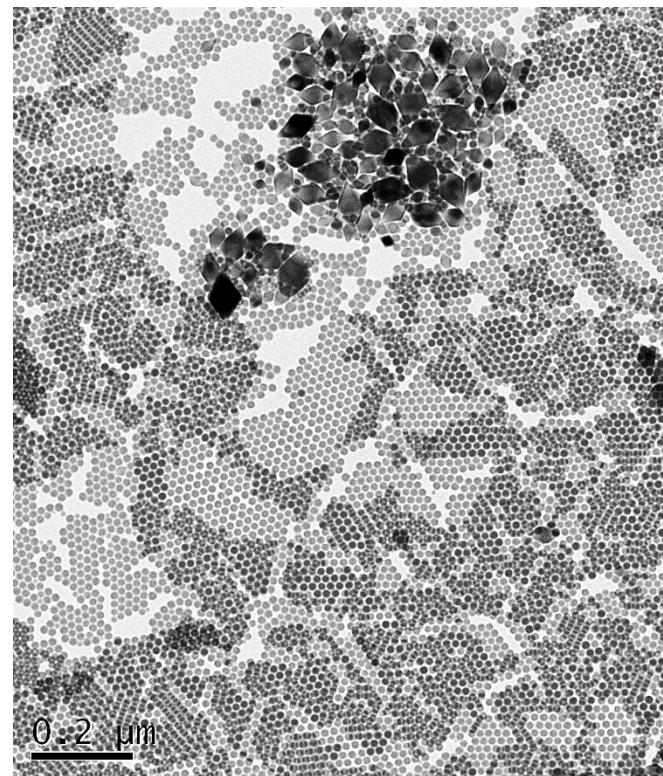
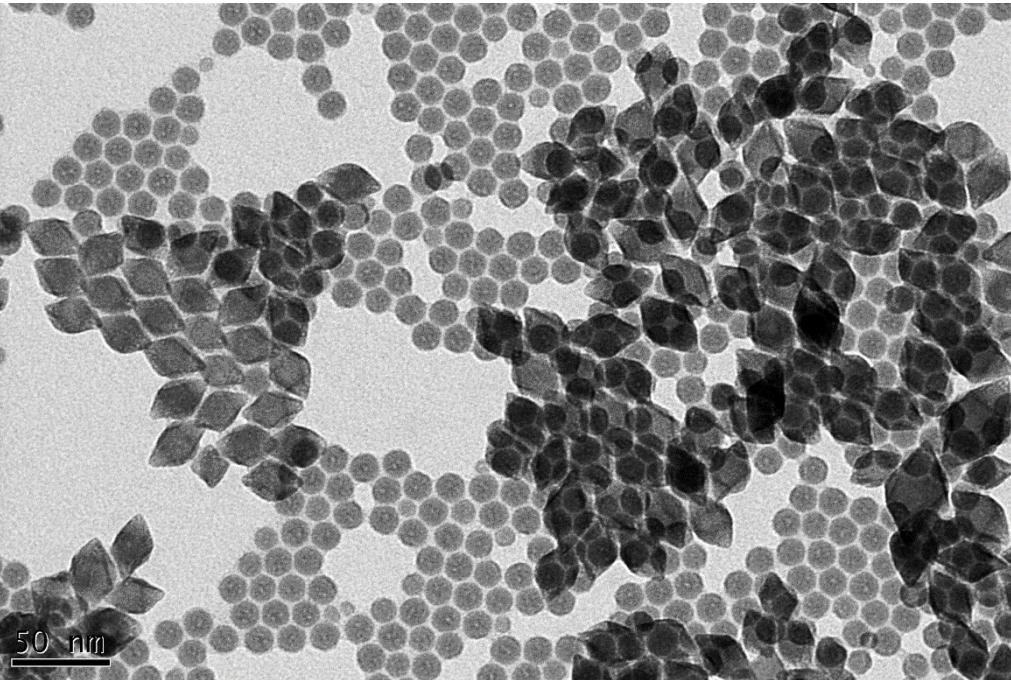
Solvothermal Approach



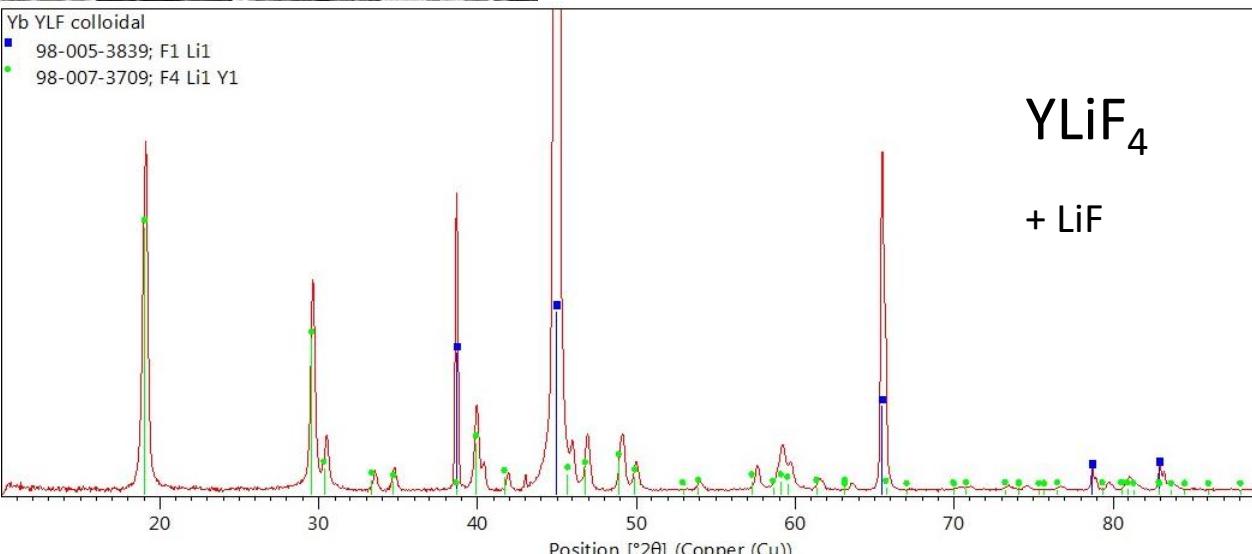
Yb:YLF Sample 3



Work Progress: 2nd of February 2018



Colloidal Approach



Roberts et al. *J. Am. Chem. Soc.*, 1961, 83 (5), pp 1087–1088

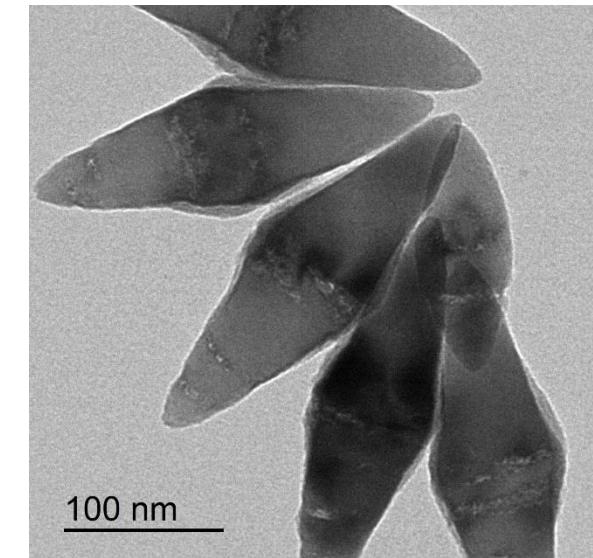
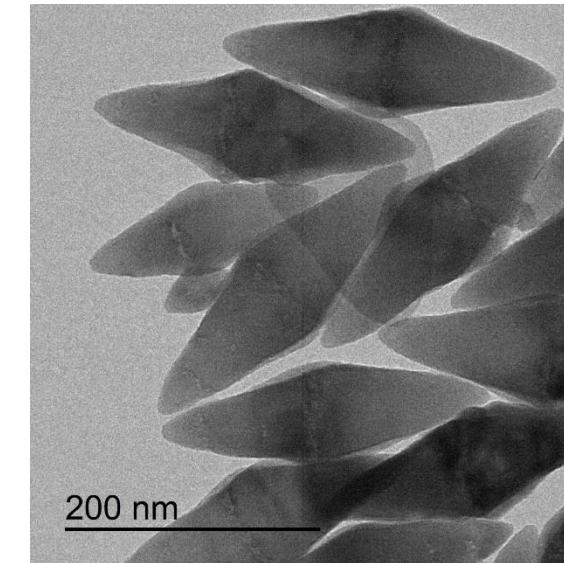
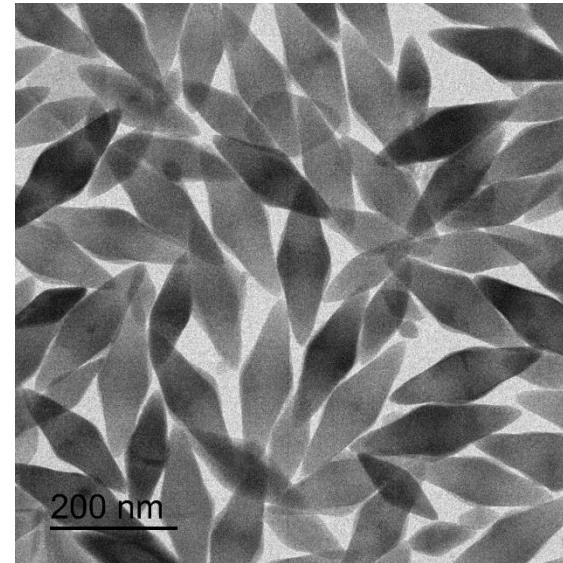
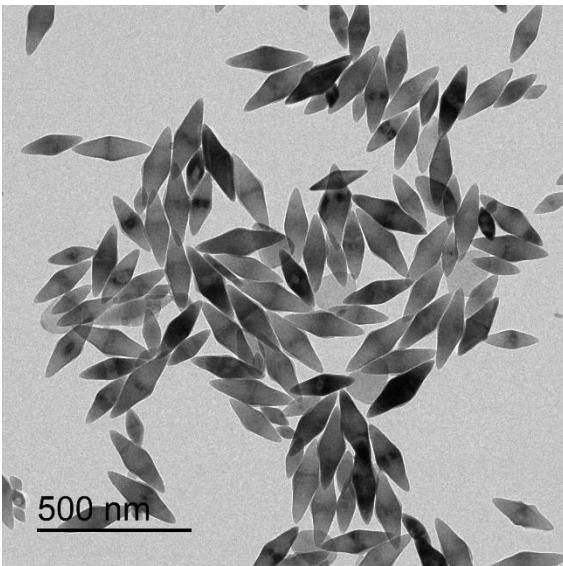
Du et al. *Dalton Trans.*, 2009, 0, 8574-8581

Work Progress: Today

«non doped» LiYF₄ NCs

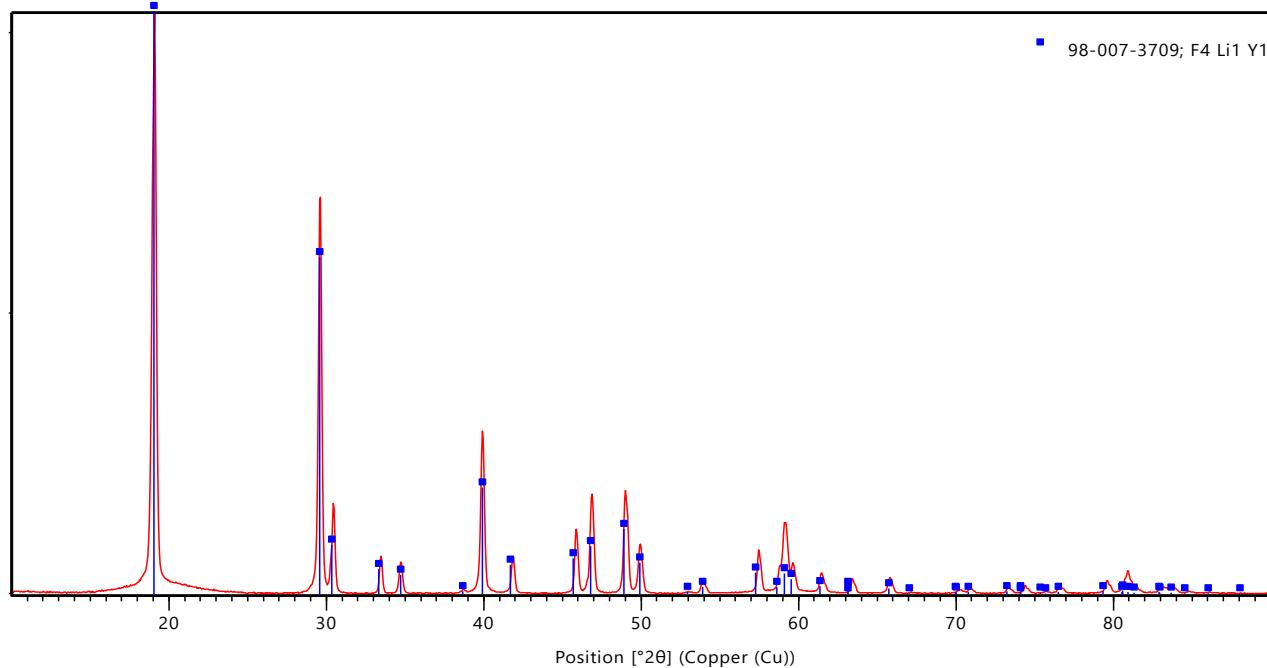
LiCO₃ 1 mmol
Y₂O₃ 1 mmol
TFA 5 mL
H₂O 5 mL

- The aqueous solution was heated up to 100°C under N₂ flow to get a clear solution
 - The solution was dried under vacuum to remove the excess of TFA and water
 - The resulting powder was solubilized in 12 mL of a mixture of Oleic Acid and Octadecene and degassing at 120°C for 1 hour
 - 330 °C (10°C/min) – Growth 15 min



«non doped» LiYF₄ NCs

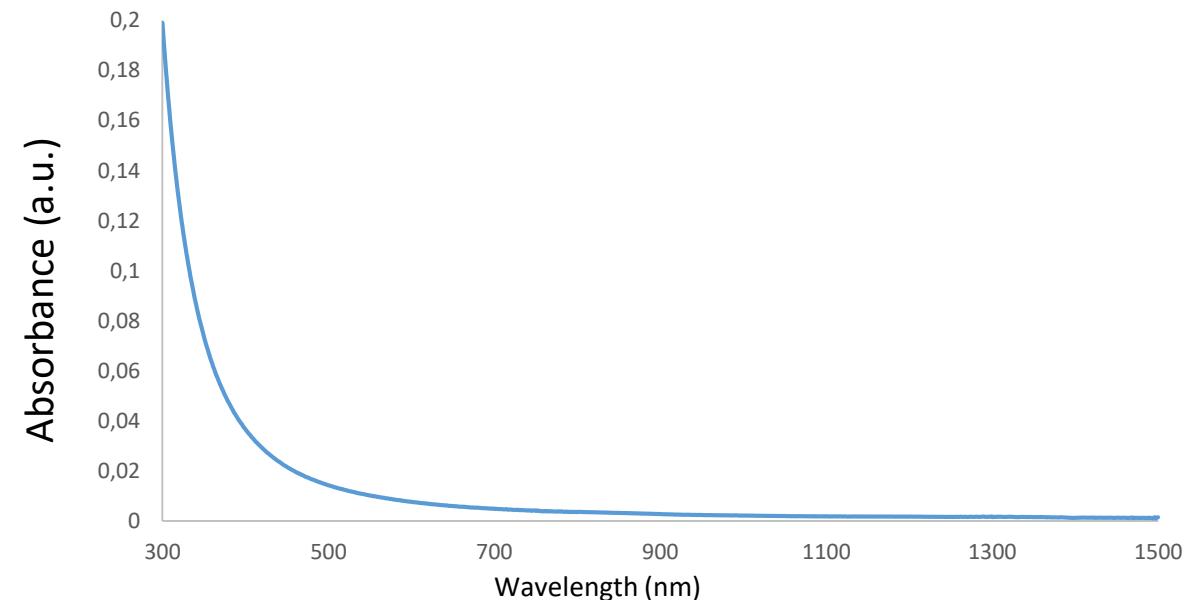
XRD analysis



Lithium yttrium fluoride

Tetragonal structure

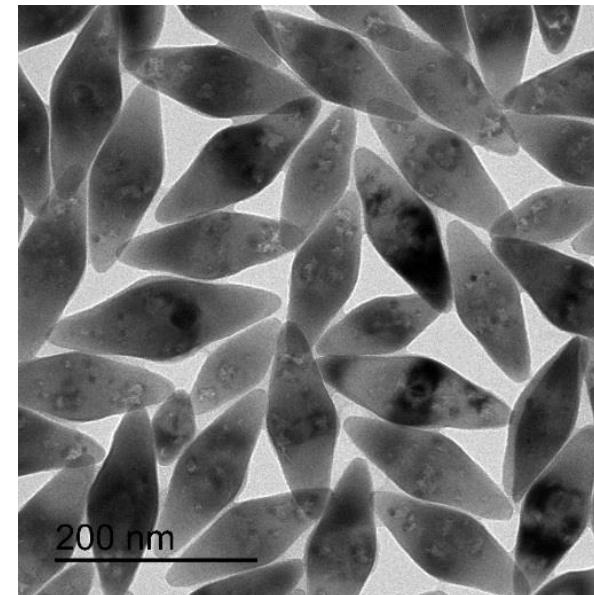
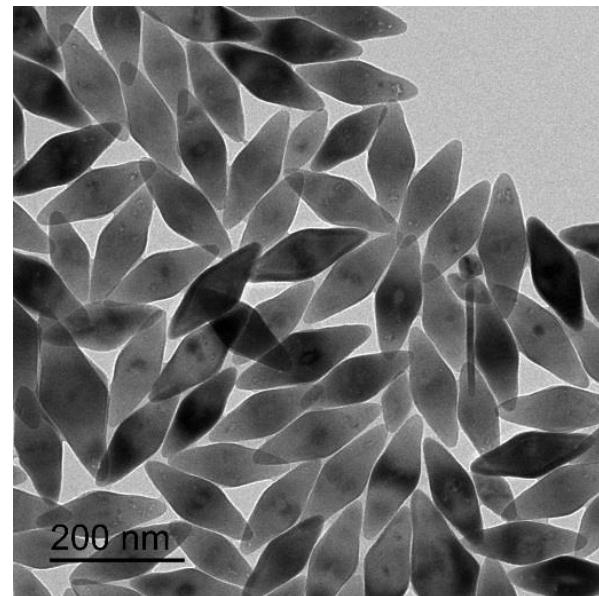
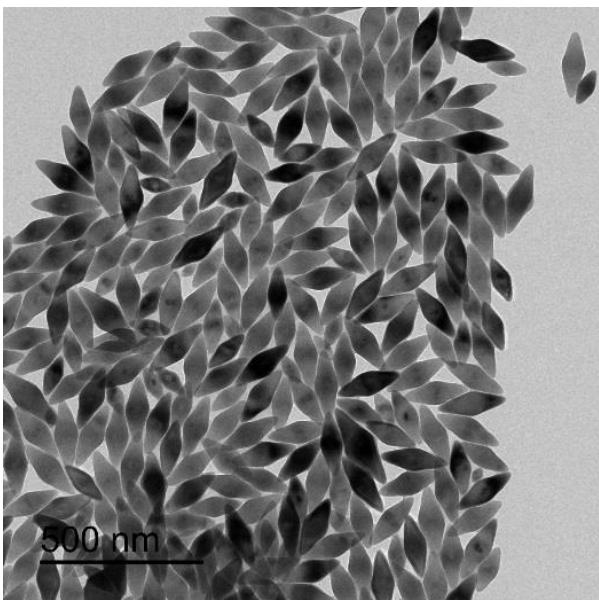
Optical Properties
dispersion of nanocrystals in tetrachloroethylene (TCE)



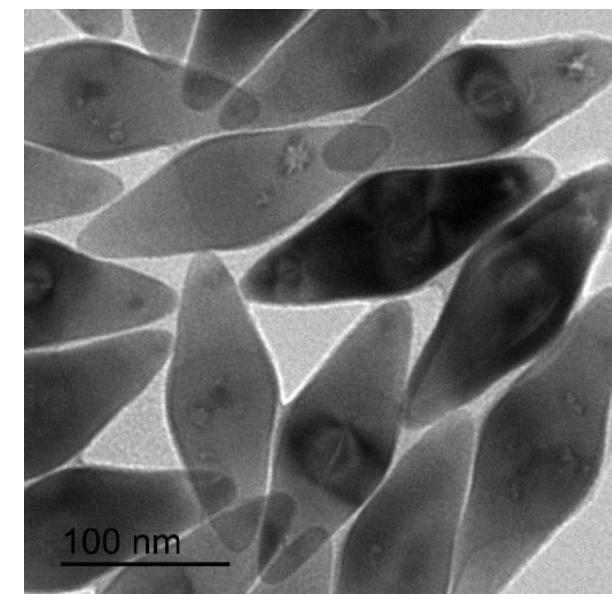
Yb-doped LiYF₄ NCs

Different Yb:LiYF₄ NC samples were synthesized following the same protocol, adding also Yb₂O₃, as Yb precursor, from the very beginning.

30% Yb:LiYF₄ NCs



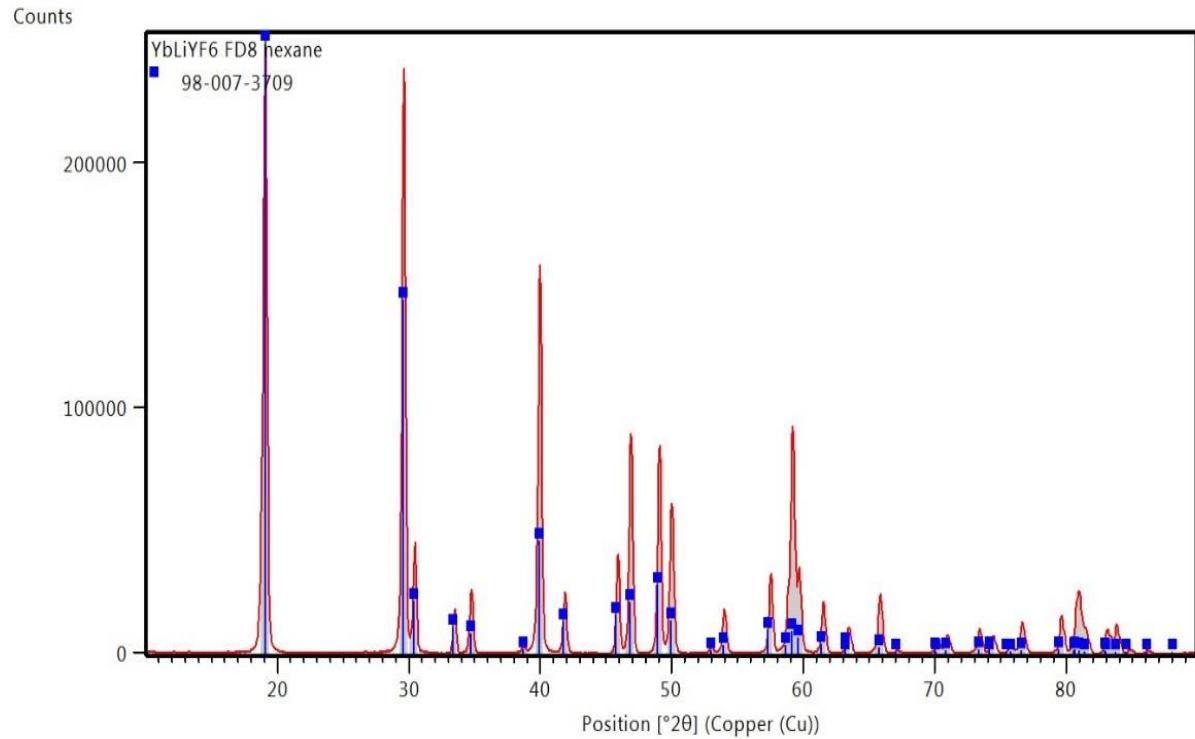
ICP elemental analysis
Yb/Y=0.30



Yb-doped LiYF₄ NCs

30% Yb:LiYF₄ NCs

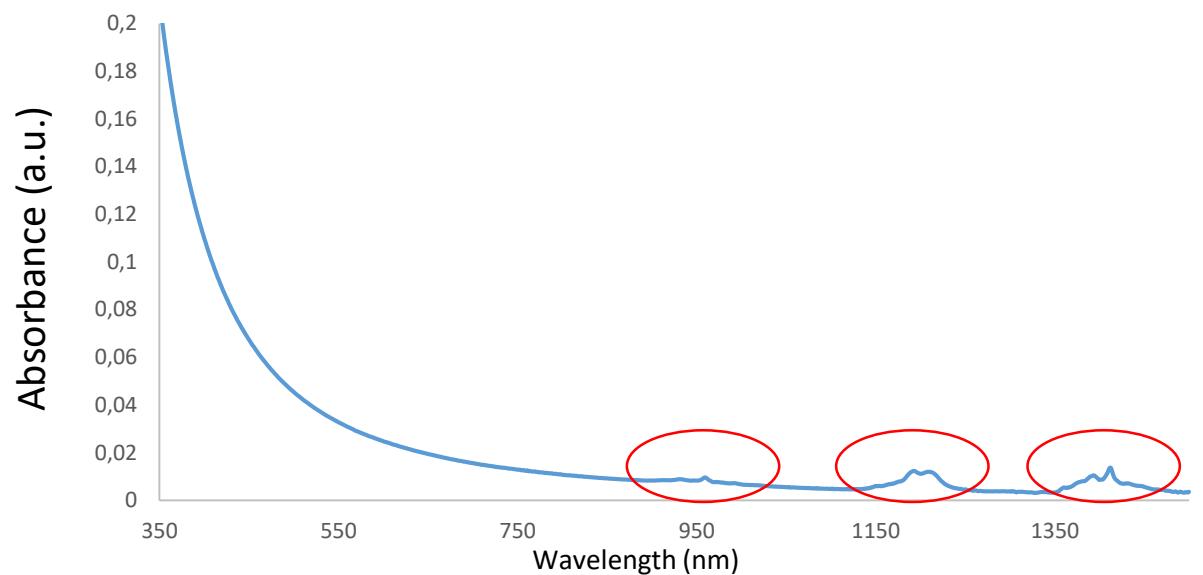
XRD analysis



Lithium yttrium fluoride

Tetragonal structure

Optical Properties

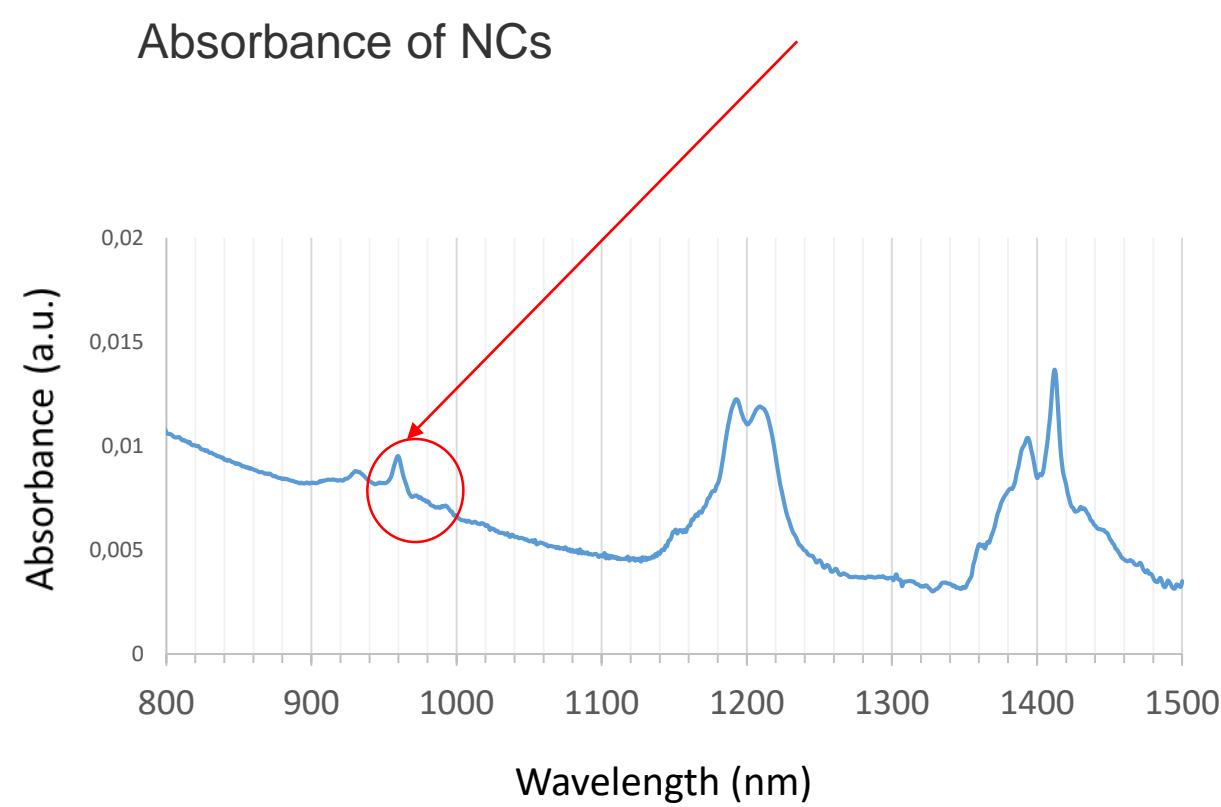


Yb-doped LiYF₄ NCs

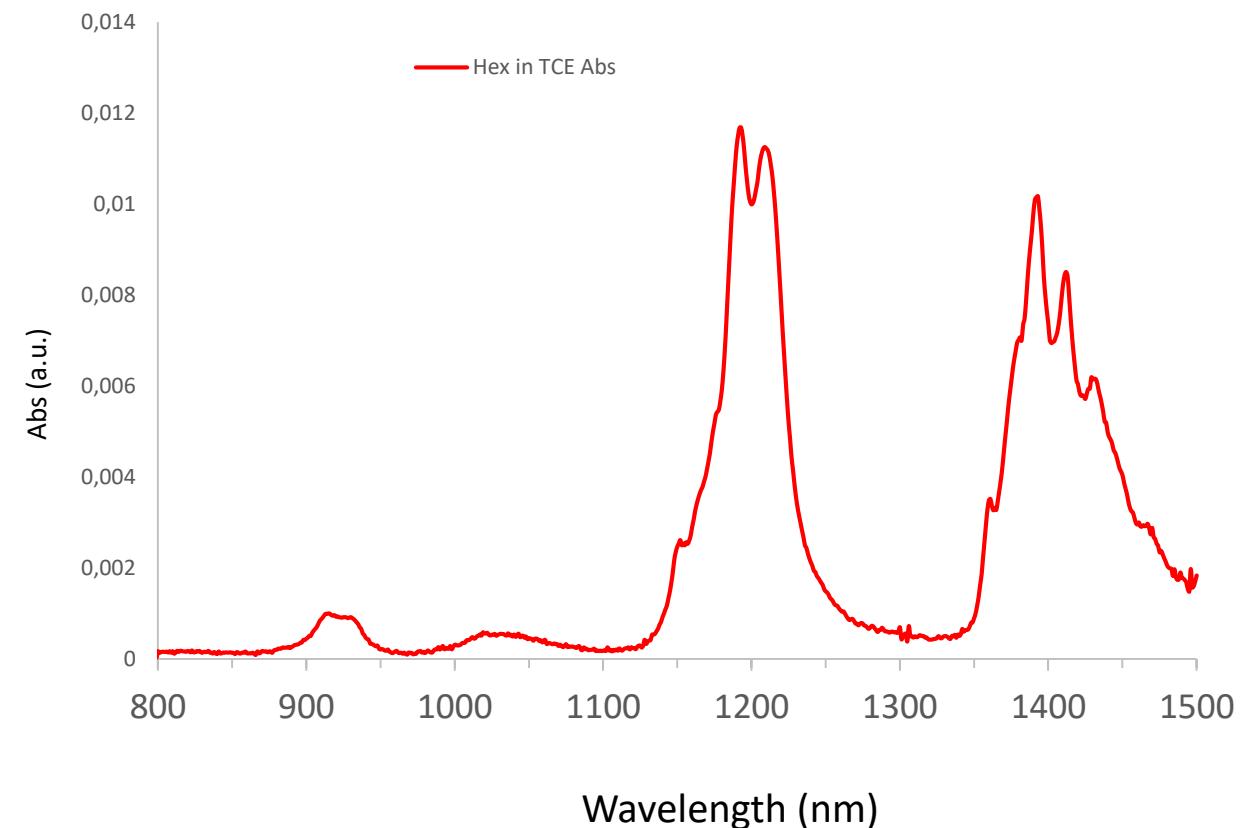
30% Yb:LiYF₄ NCs

Absorbance of NCs

Yb³⁺ Optical transitions

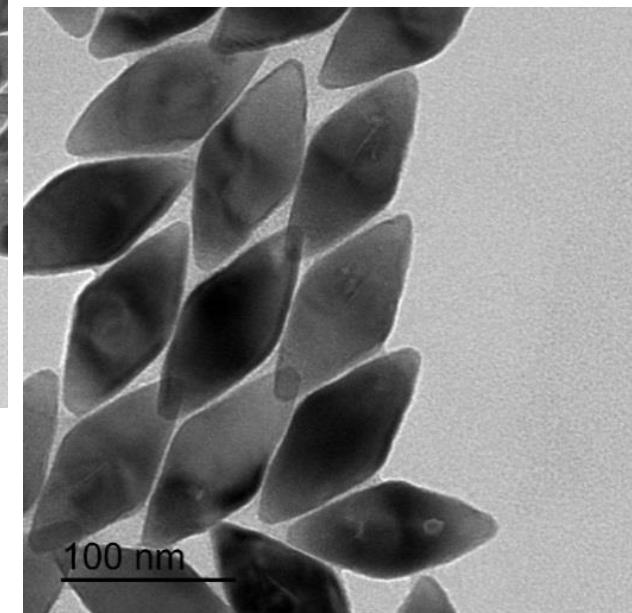
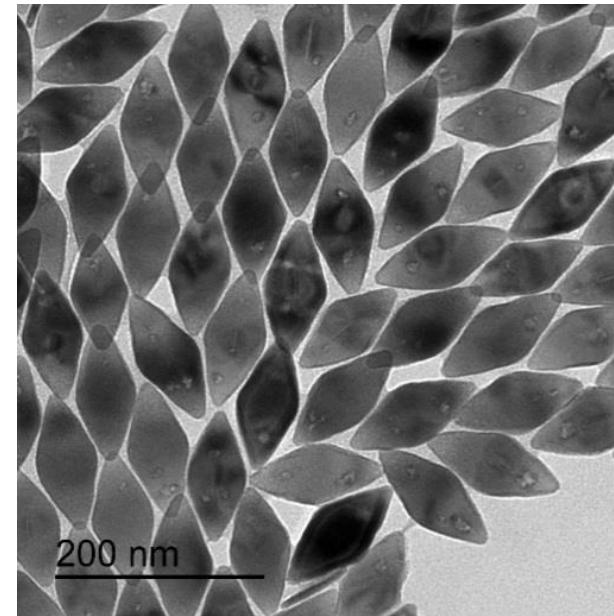
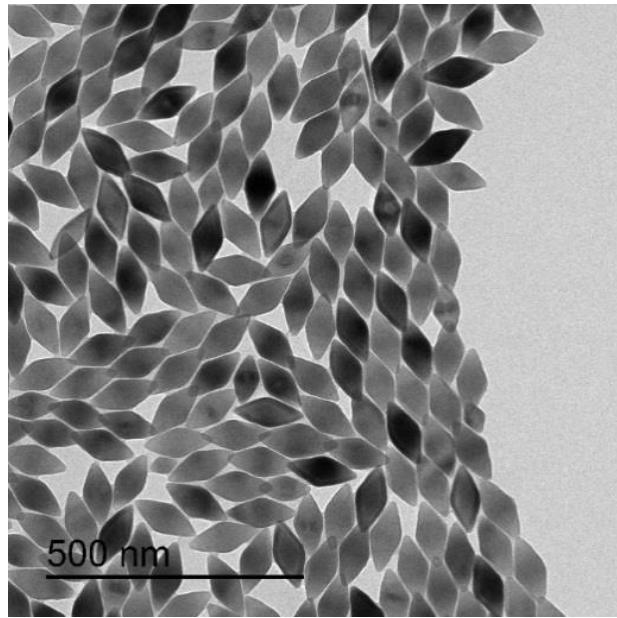
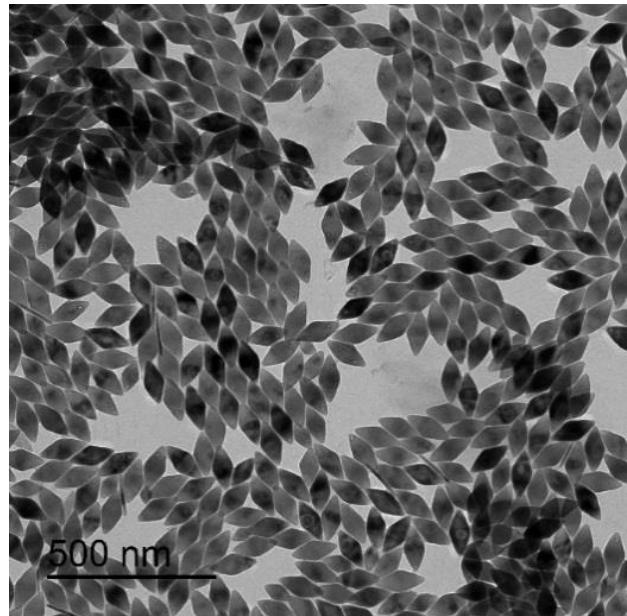


Absorbance of hexane (in TCE)



Yb-doped LiYF₄ NCs

38% Yb:LiYF₄ NCs

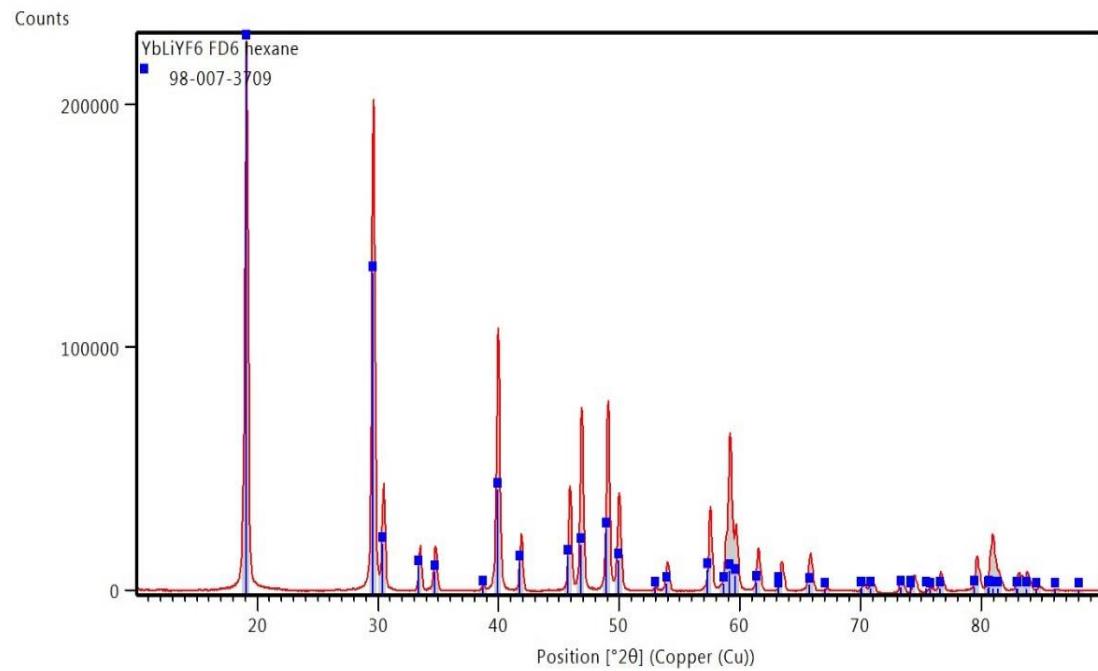


ICP elemental analysis
Yb/Y=0.38

Yb-doped LiYF₄ NCs

38% Yb:LiYF₄ NCs

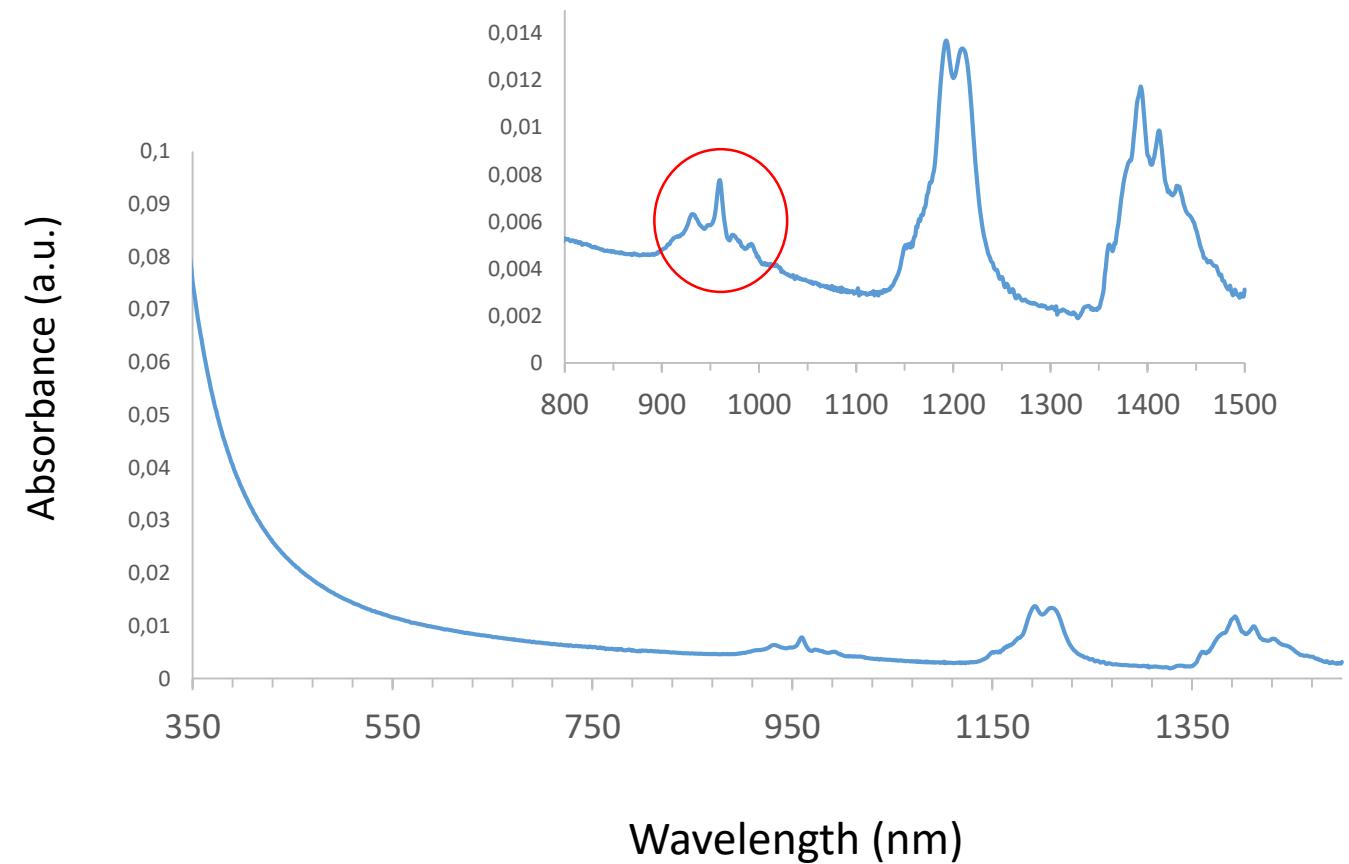
XRD analysis



Lithium yttrium fluoride

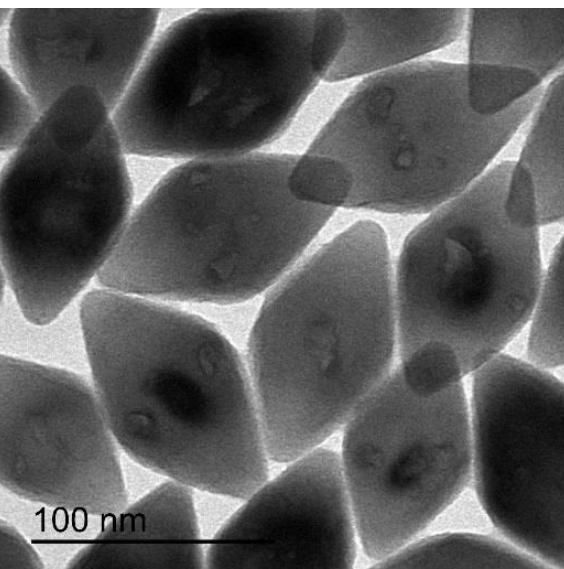
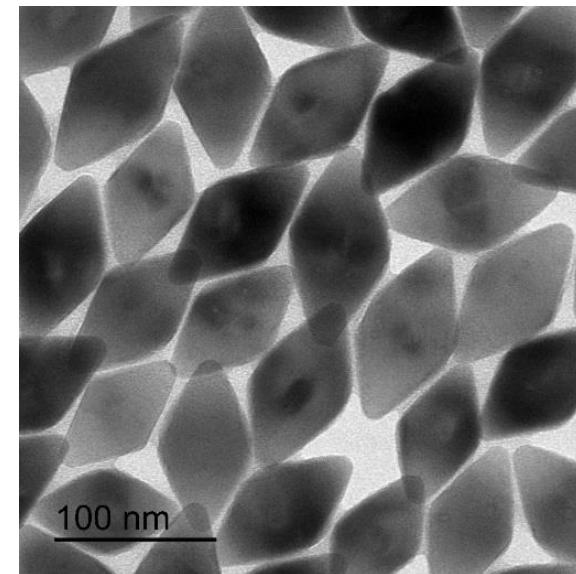
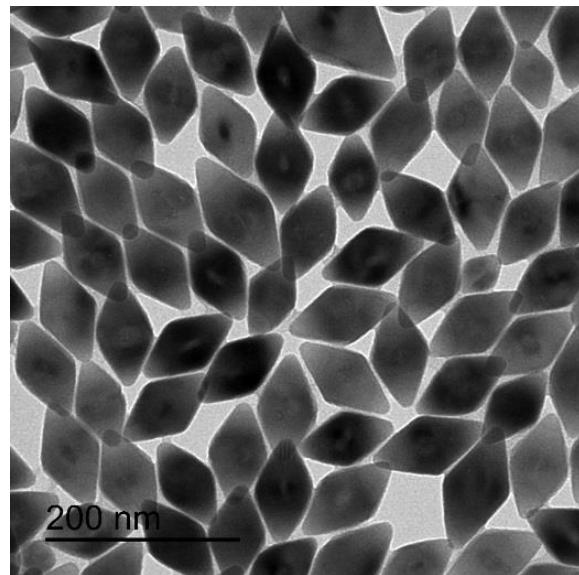
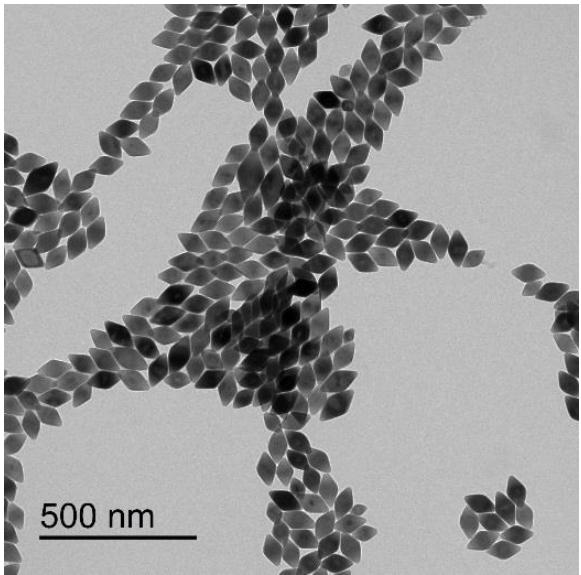
Tetragonal structure

Optical Properties



Yb-doped LiYF₄ NCs

127% Yb:LiYF₄ NCs



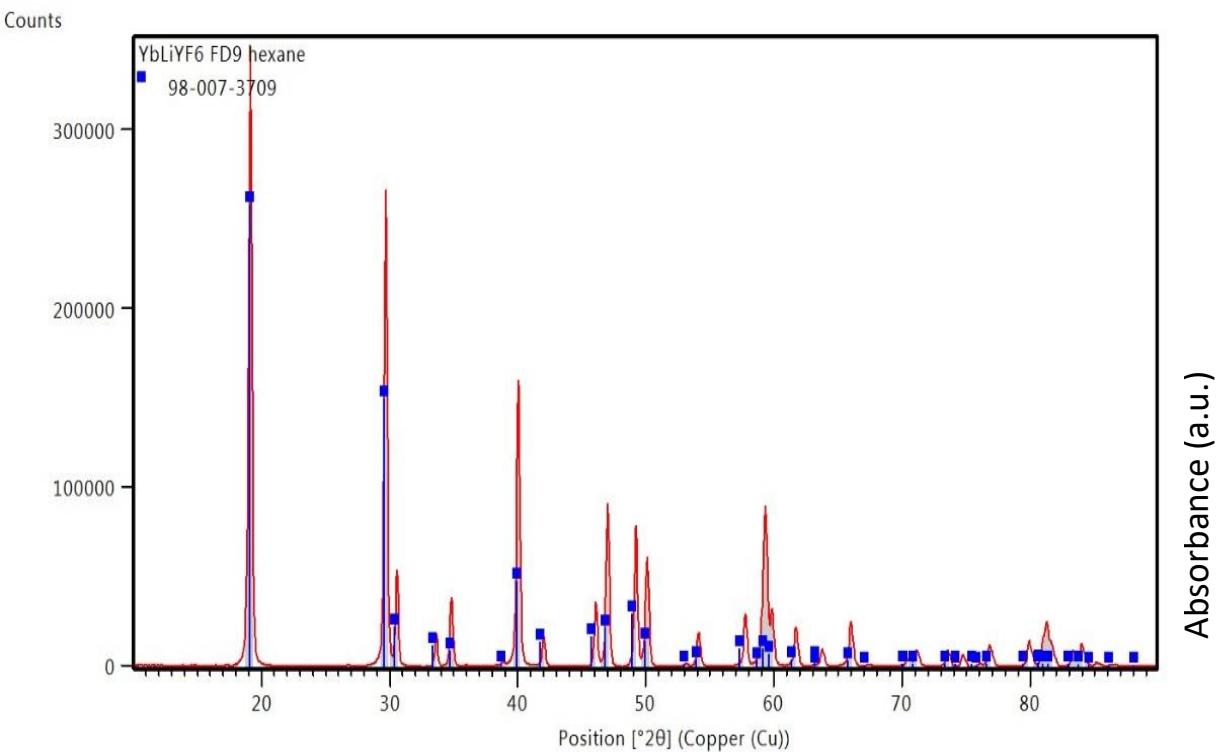
ICP elemental analysis

Yb/Y=1.27

Yb-doped LiYF₄ NCs

127% Yb:LiYF₄ NCs

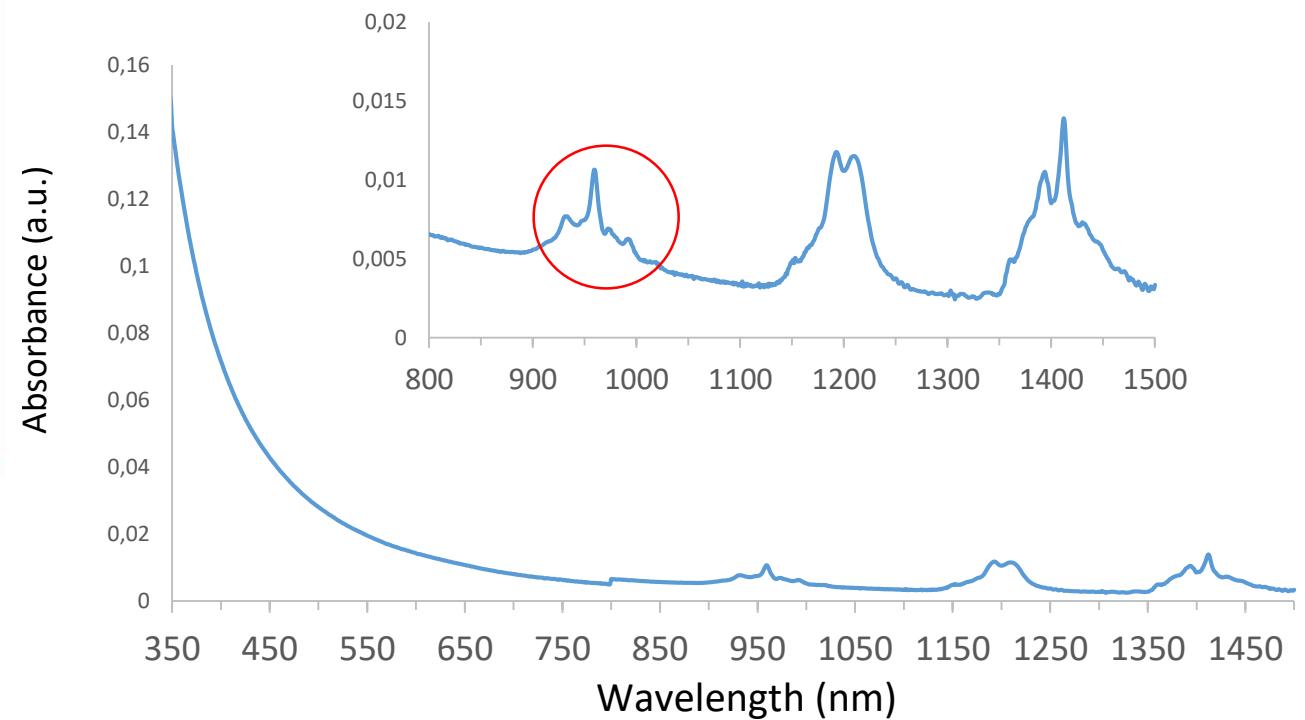
XRD analysis



Lithium yttrium fluoride

Tetragonal structure

Optical Properties

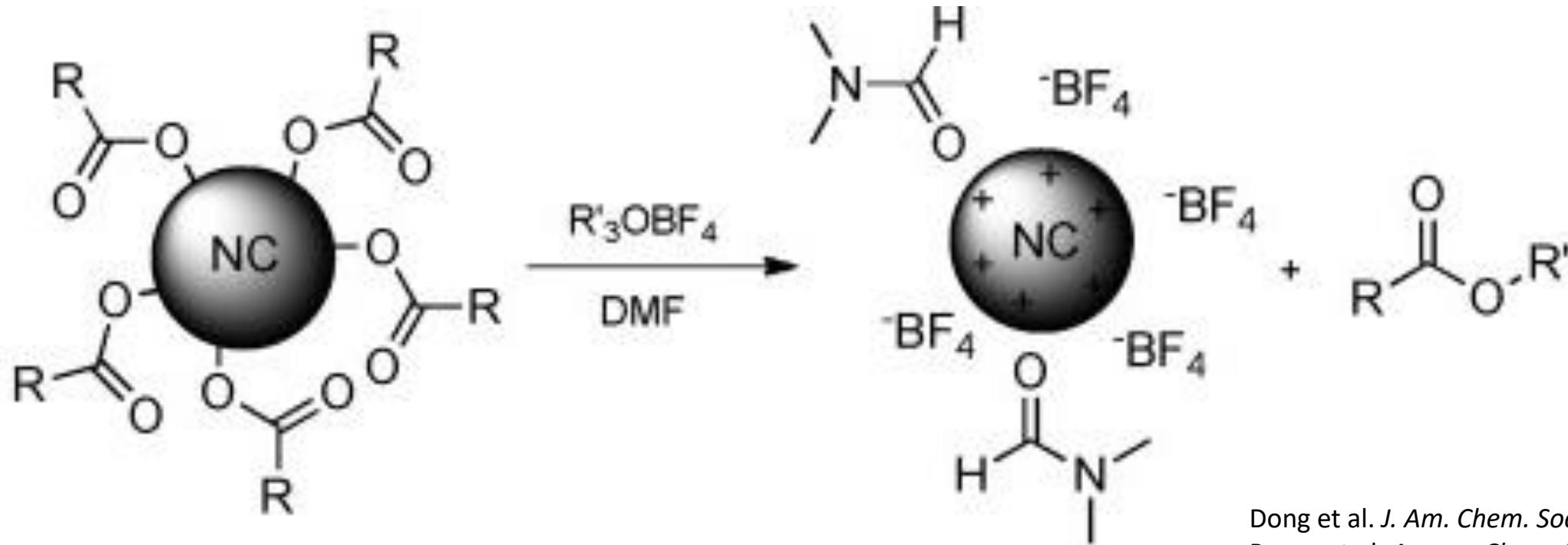


Ligand Stripping

Making the NCs dispersible in Methanol

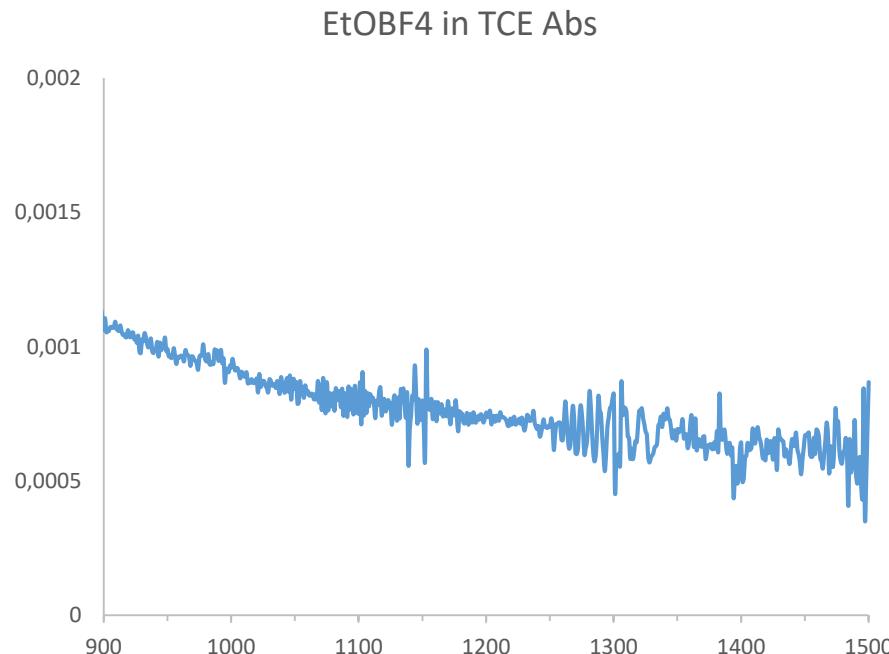
In order to remove the ligands from the surface of NCs we employed:

- Triethyloxonium tetrafluoroborate (NOBF_4)
- Triethyloxonium tetrafluoroborate (Et_3OBF_4)



Ligand Stripping

Both reagents yielded good results:
the size, shape, composition and crystal structure
were not altered upon the ligand removal procedure



Thanks for your
Attention

Current status of the TEQ trap design

**Michael Drewsen
Department of Physics and Astronomy
Aarhus University
Denmark**

**TEQ Meeting, June 21, 2018
University of Southampton, UK**

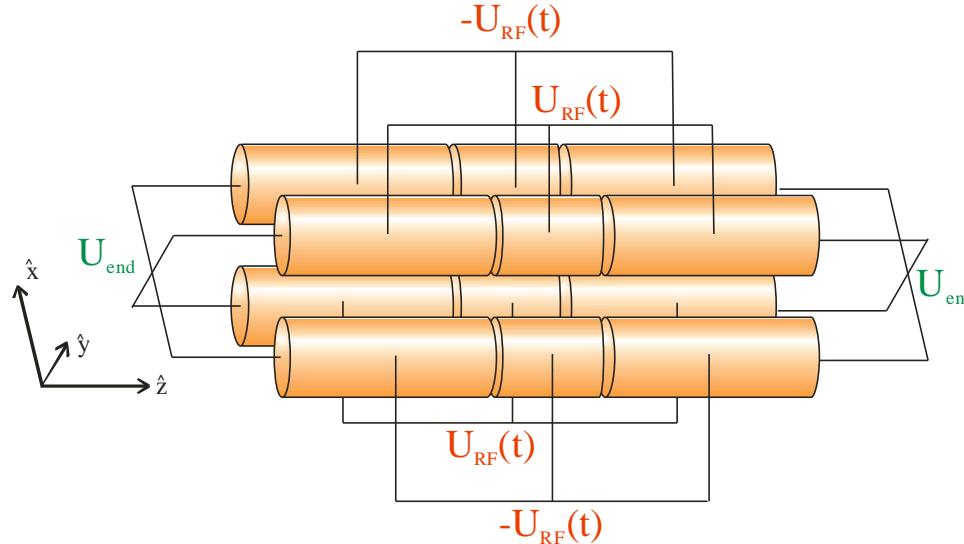


Outline

- I) Physical layout
- I) Requirements related to the electronics and heating
- I) Passive NC cooling
- I) Still unresolved issues

I) Physical layout

The linear Paul trap



Sinusoidal RF potential: $U_{RF}(t)=U_{RF}\sin(\Omega t)$

Effective oscillation freq.'s:

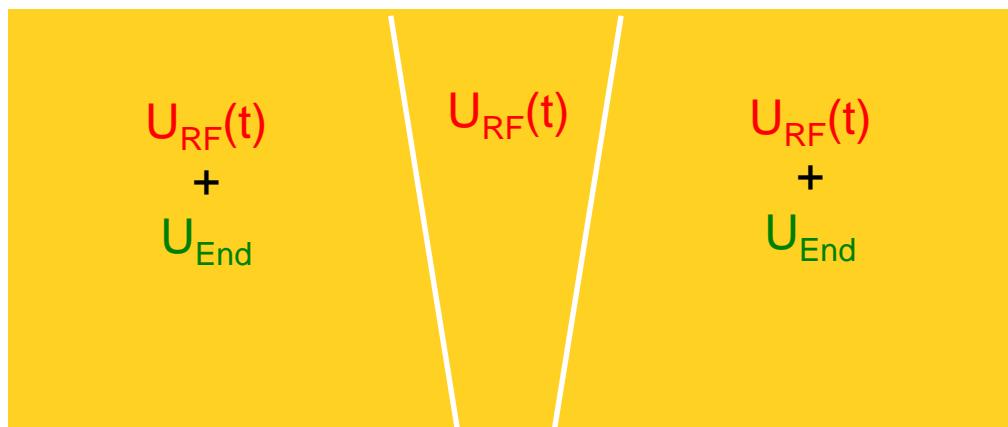
$$\omega_r = 1/2 \beta \Omega, \quad \beta = (1/2 q^2 + a)^{1/2}$$

$$\omega_z = (-1/2 a)^{1/2} \Omega$$

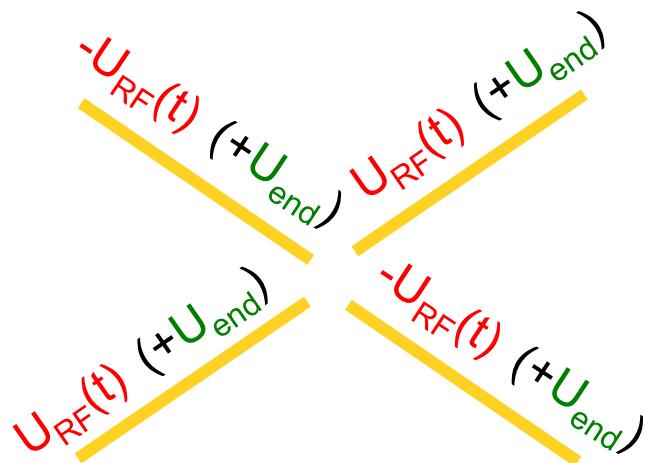
$$q = \frac{4Q U_{RF}}{m \Omega^2 r_0^2} \quad a = -\frac{\alpha Q U_{end}}{m \Omega^2 r_0^2}$$

Blade electrode trap I

Blade electrode structure



Mounted electrodes
in an end view:

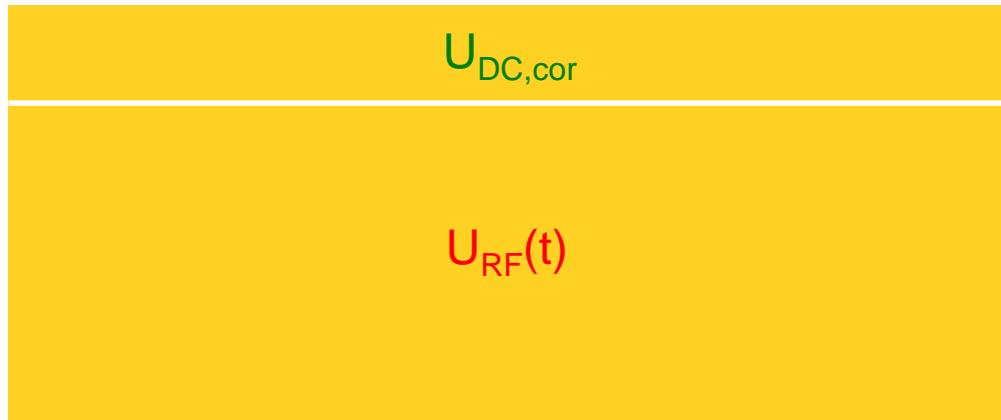


Note:

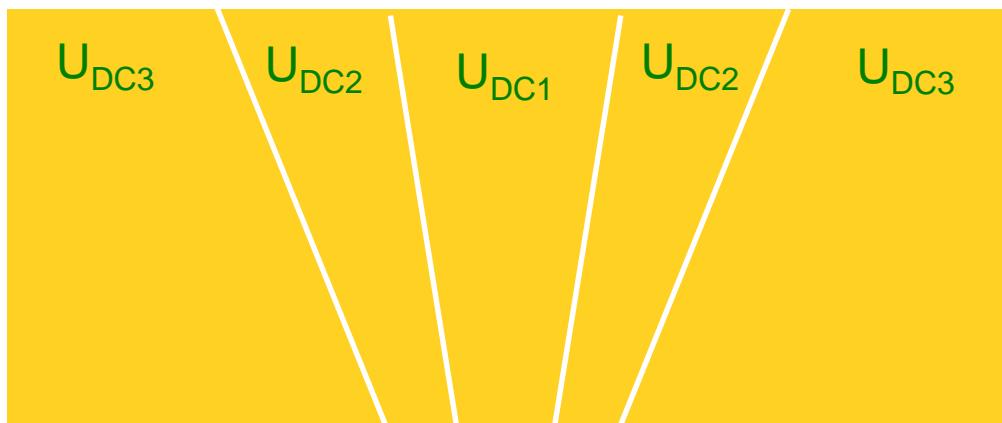
$U_{RF}(t)$ and U_{end} has to be mixed together.

Blade electrode trap II

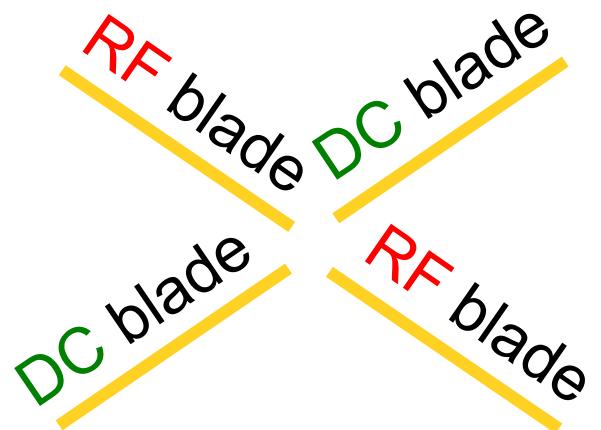
RF blade electrode



DC blade electrode

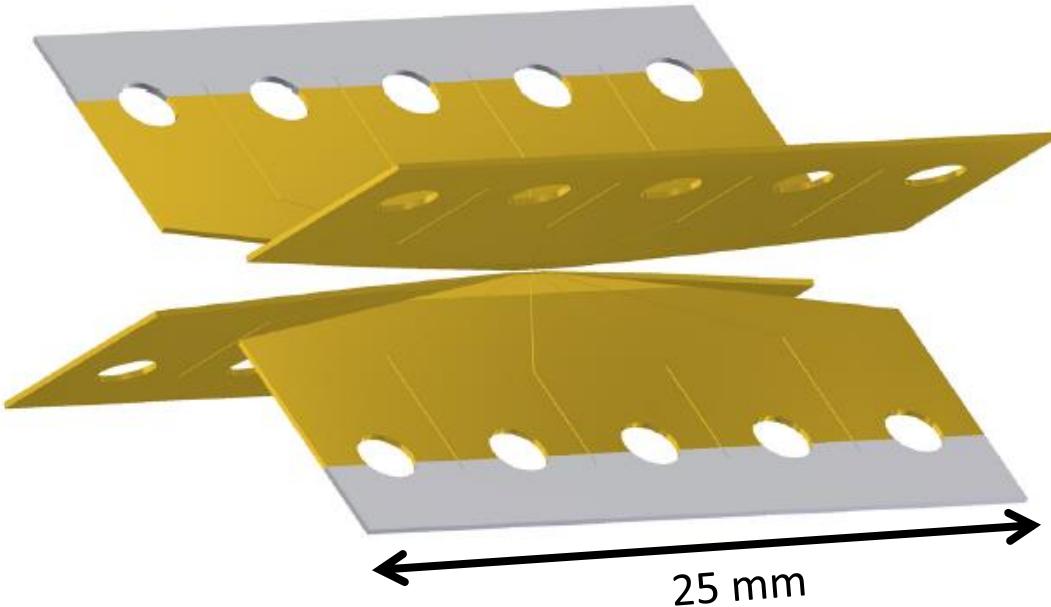


Mounted electrodes
in an end view:



No mixing of $U_{RF}(t)$
and U_{end} needed!

Linear rf trap designed by Chris Monroe's Group

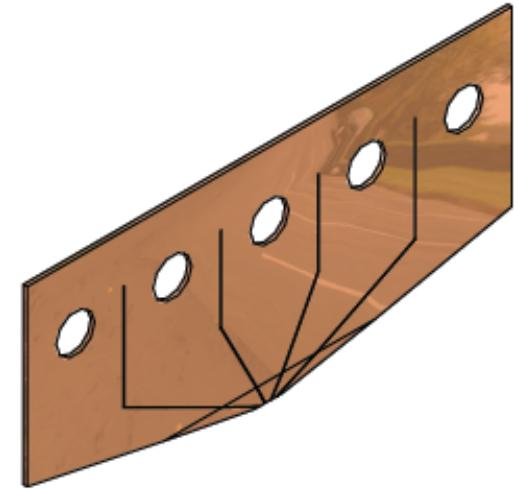
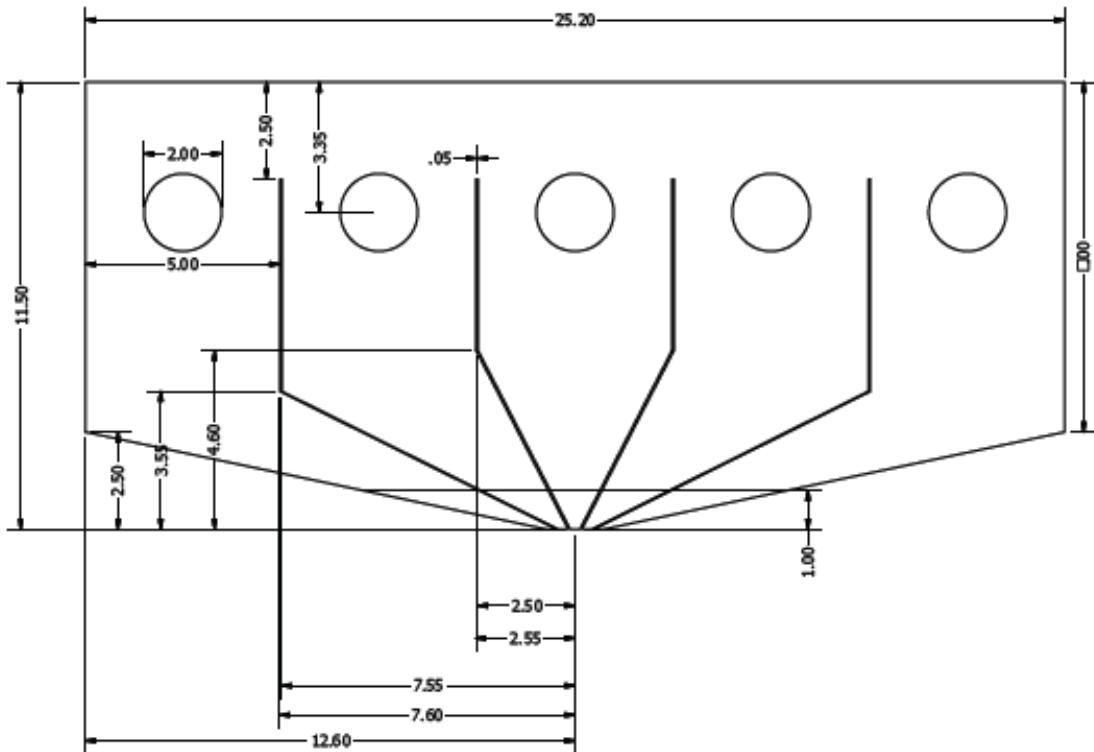


Blade mat.:
Gold on
Alumina

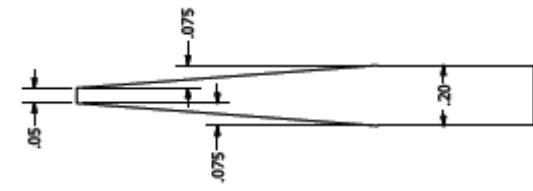
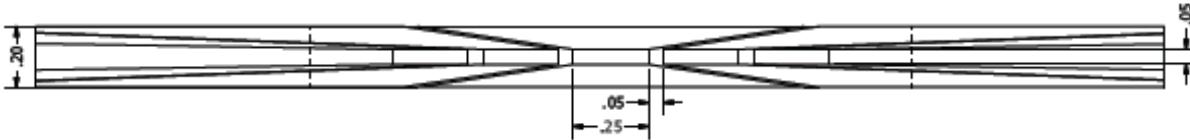
From PhD thesis of David Hucul

TEQ linear rf trap

Design by Chris Monroe's Group

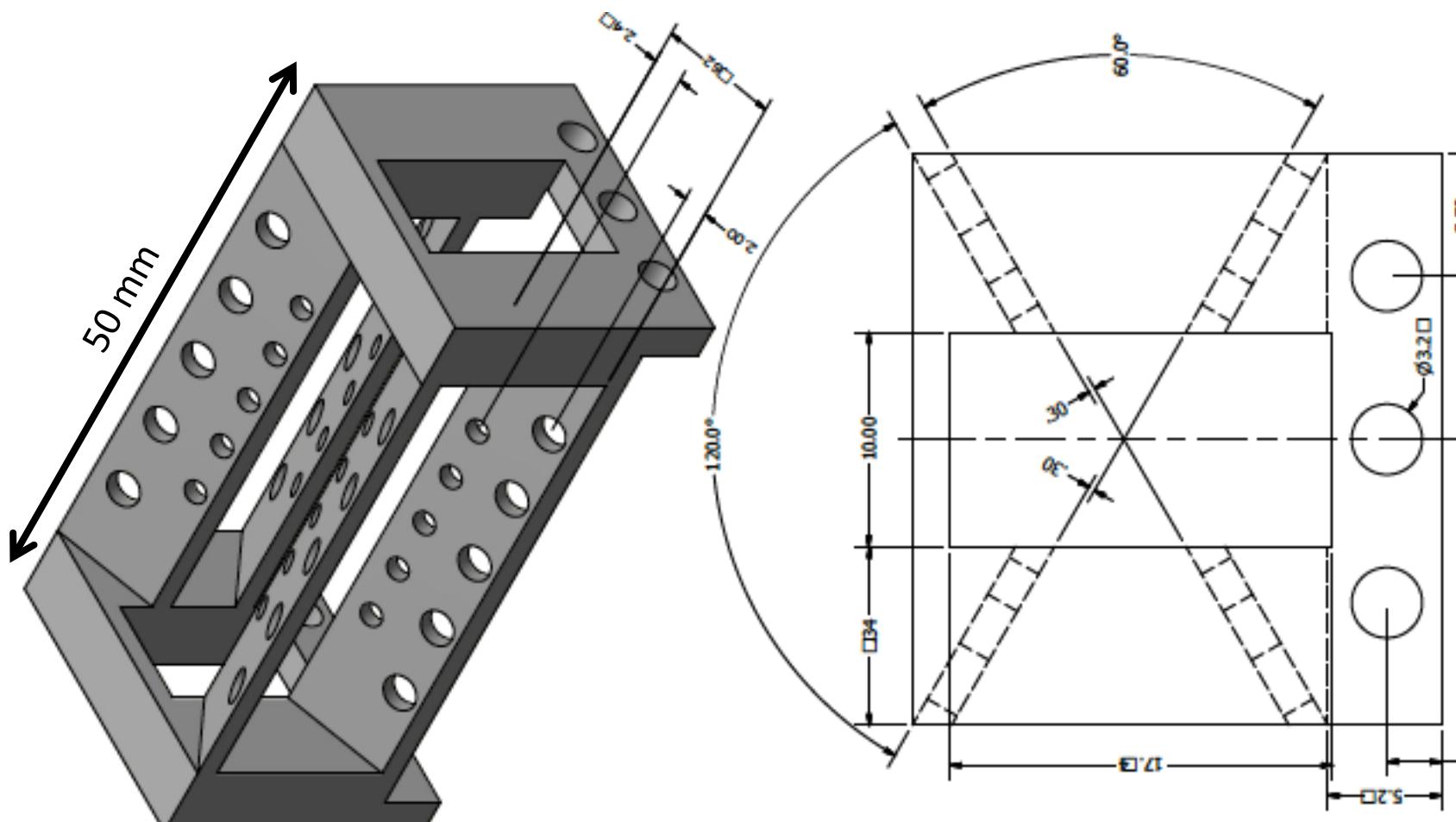


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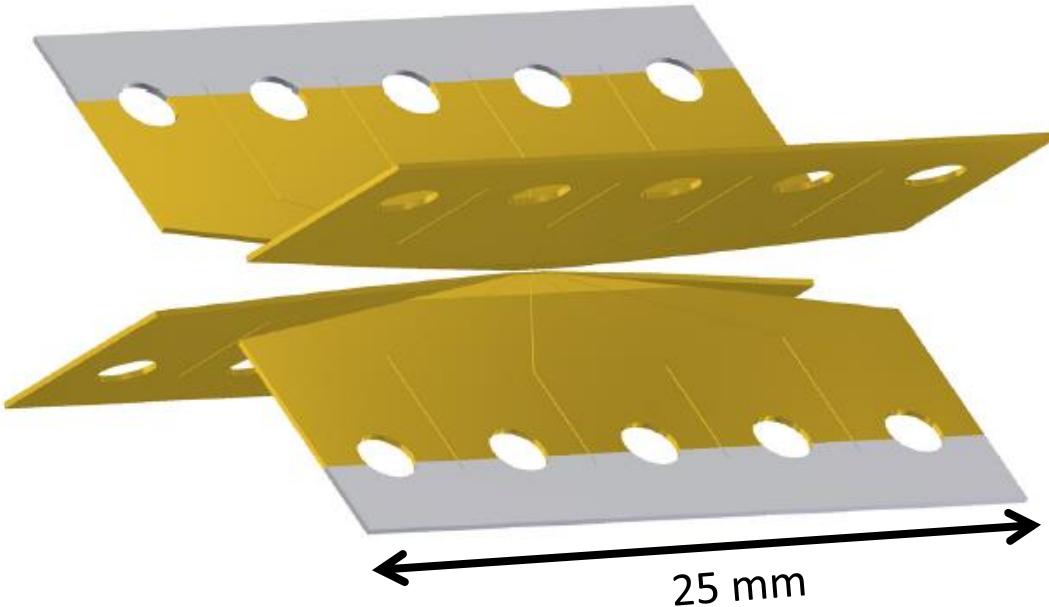


Linear rf trap

designed by Chris Monroe's Group



Linear rf trap designed by Chris Monroe's Group



Blade mat.:
Gold on
Alumina

From PhD thesis of David Hucul

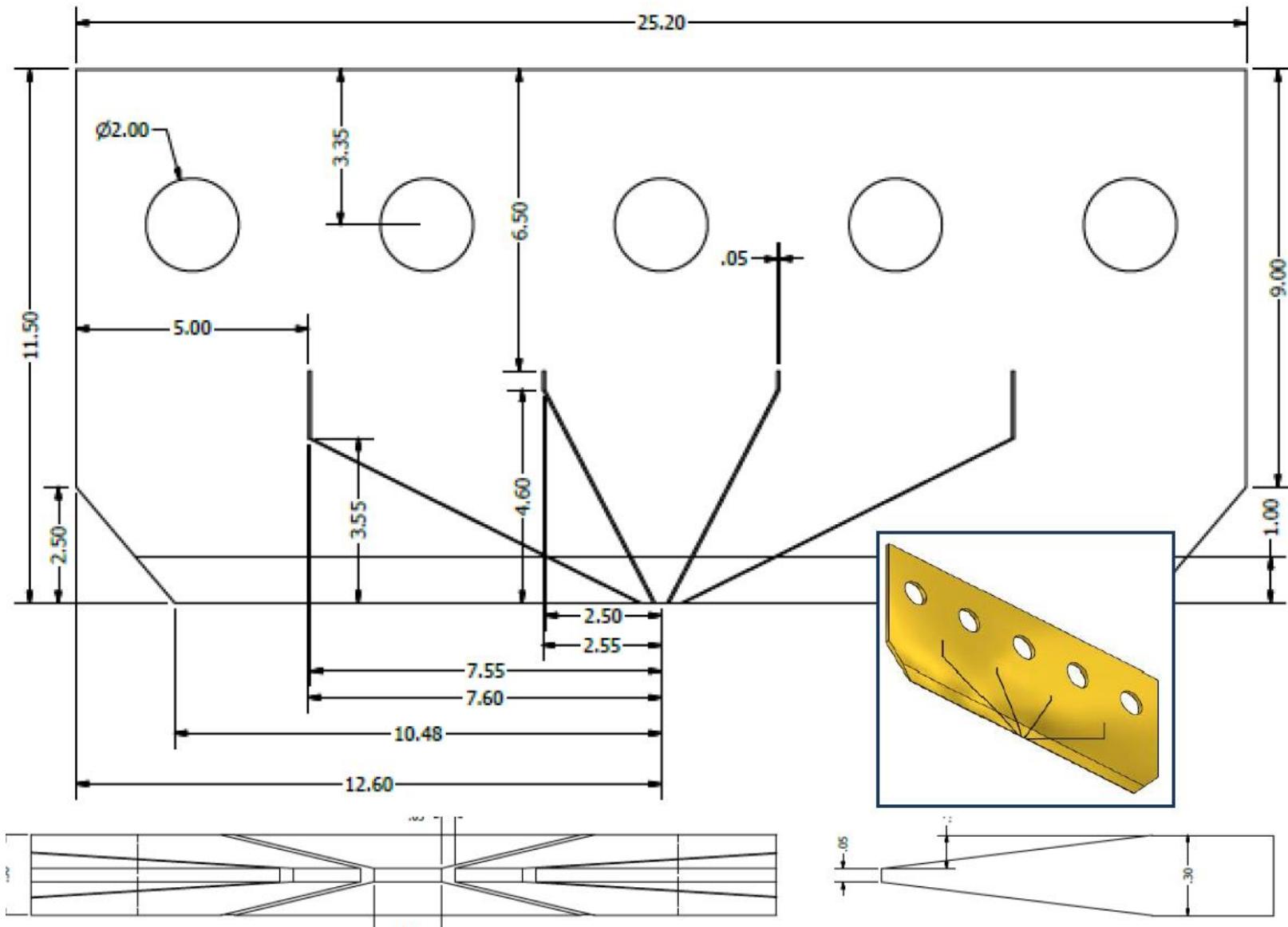
**Linear rf trap
designed by Chris Monroe's Group**

Imaging setup



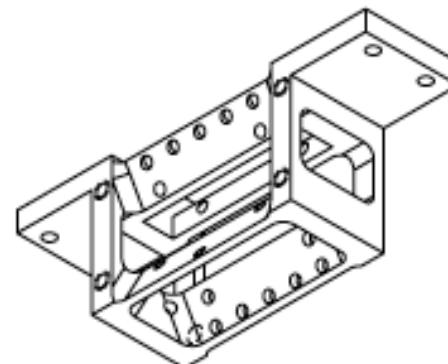
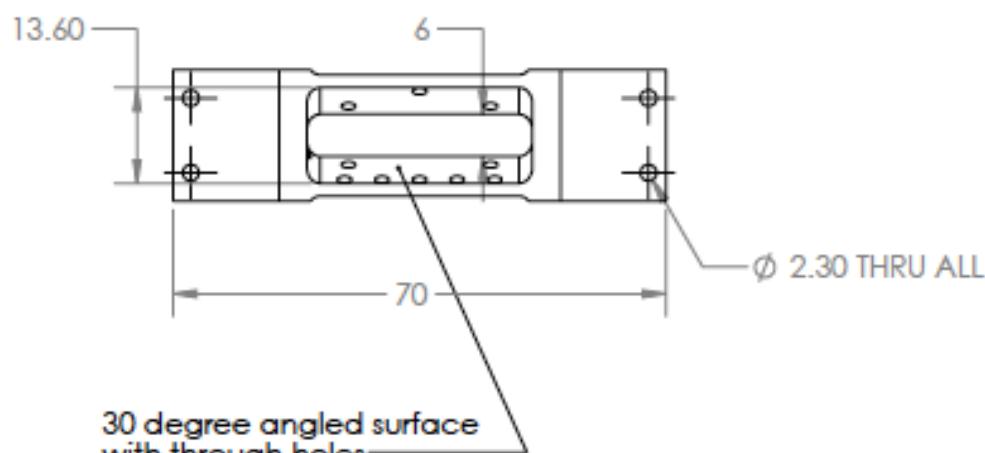
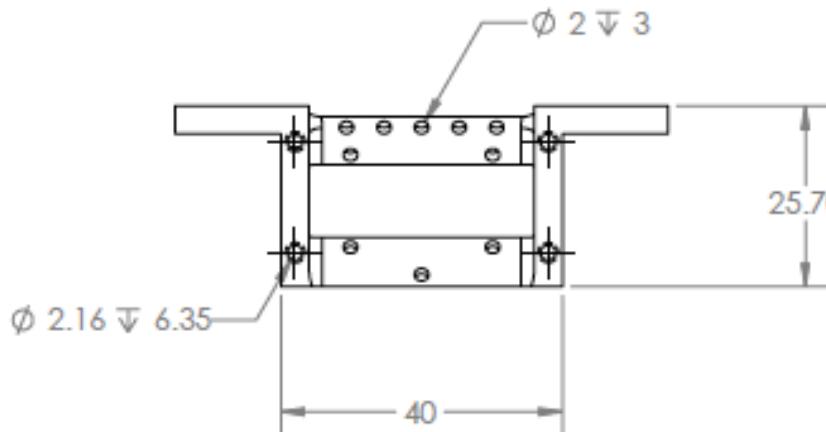
TEQ linear rf (ac) trap?

Design by Chris Monroe's Group



TEQ linear rf (ac) trap?

Design by Chris Monroe's Group

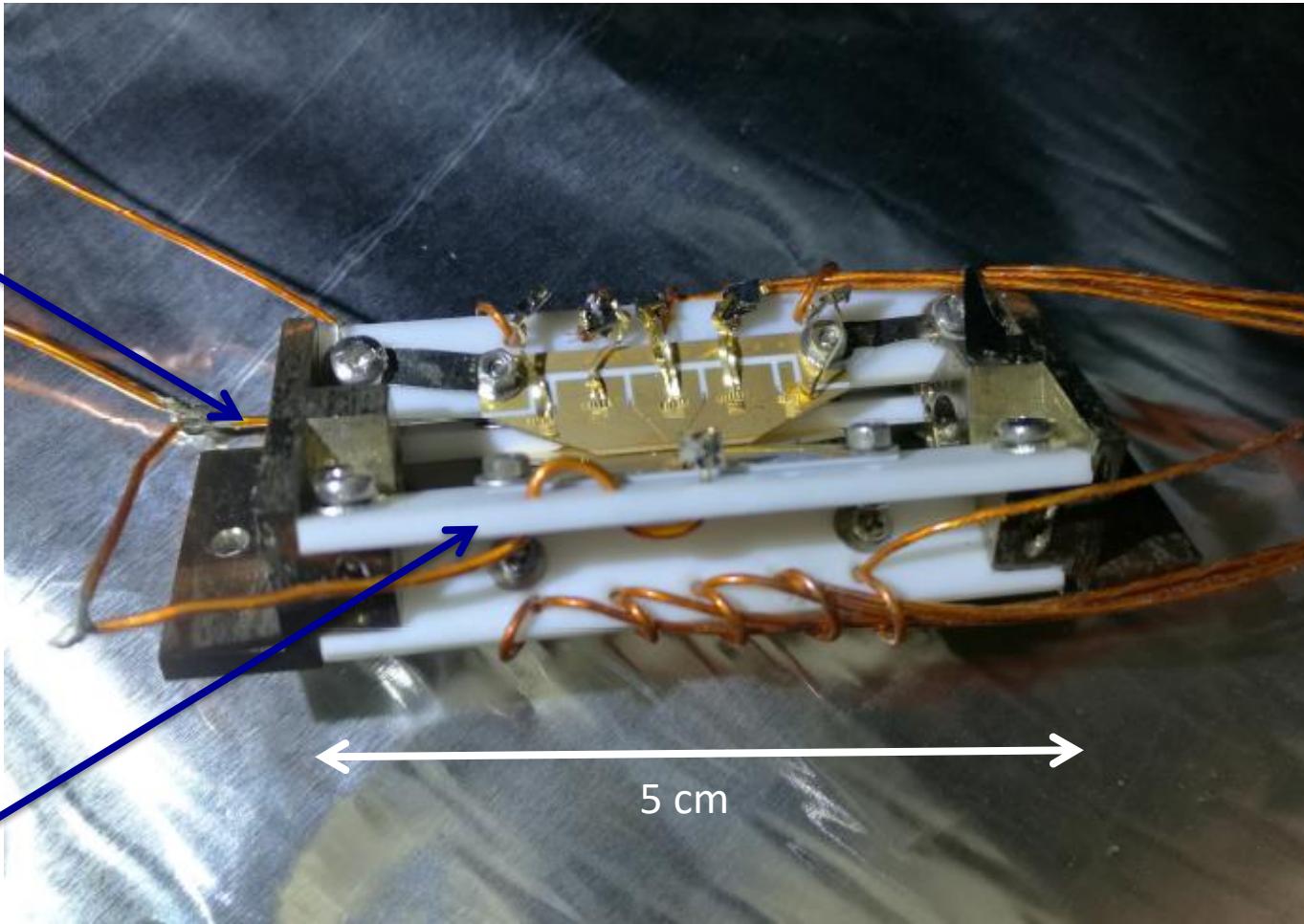


Blade Trap Holder
Drawn By: P.W. Hess
Material: Sapphire or Alumina
Notes:

- All Units in mm
- Tolerances on angled surfaces < 1 mil (0.025 mm)

Another option for blade support constructed by Shuoming An, Tsinghua Uni.

Stainless
steel



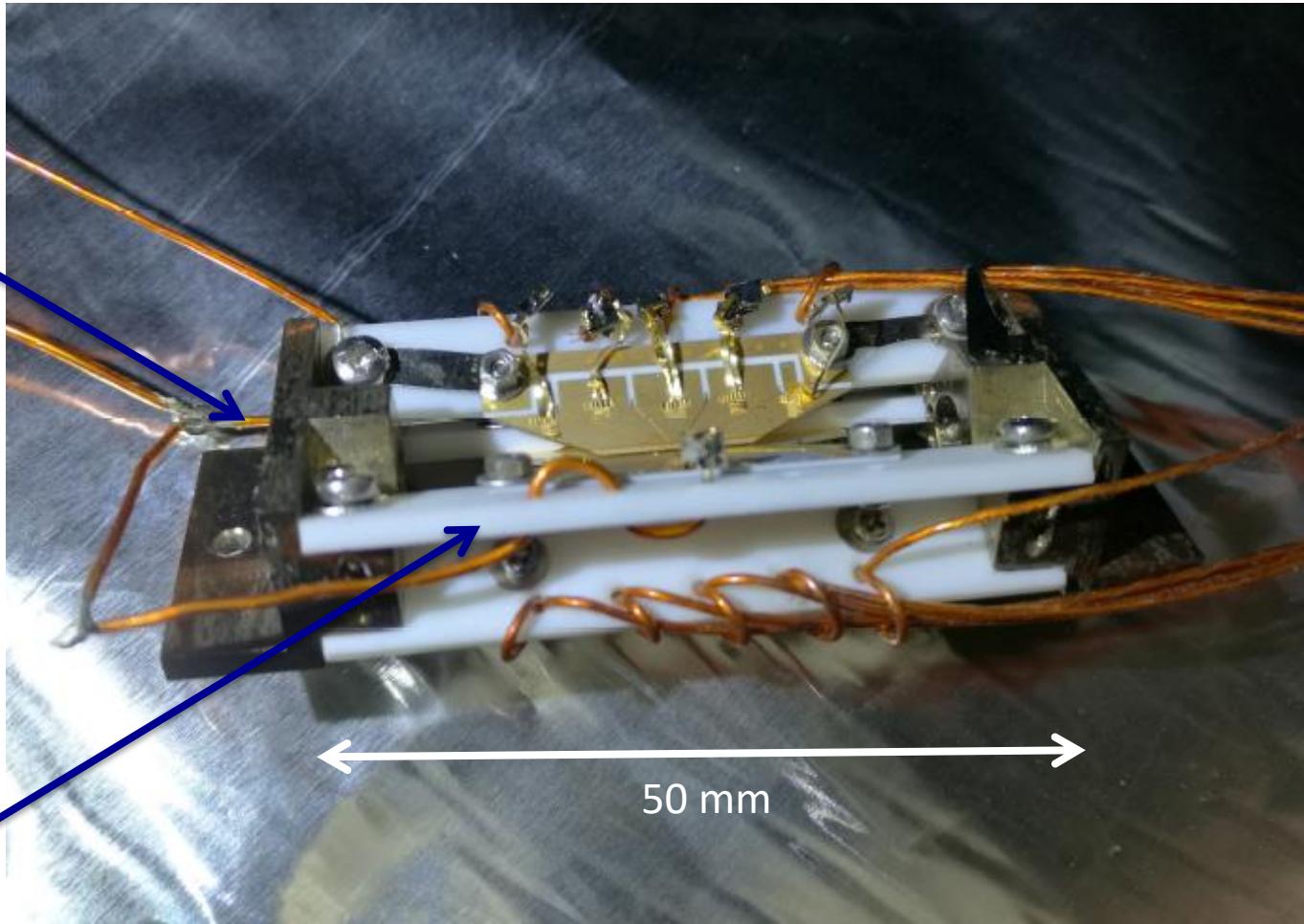
Macor®

5 cm

Another option for blade support constructed by Shuoming An, Tsinghua Uni.

Copper

Shapal™



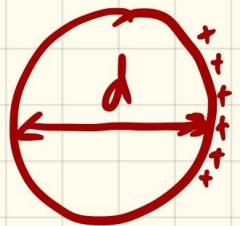
Monolithic blade electrode holder best for precise alignment

II) Requirements related to the electronics and heating

ISSUES REGARDING THE TRAP DESIGN

PARAMETERS RELATED TO PARTICLES:

(1)



Q CHARGES

$$d = 100 \text{ nm}, \rho = 5 \text{ g/cm}^3 \Rightarrow$$

$$\boxed{Q = 10 - 10^4 \text{ e} (?)}$$

$$\boxed{m = 7.6 \cdot 10^{-18} \text{ kg}}$$

RADIAL FREQUENCY:

$$(*) \omega_r^2 = \frac{q^2}{\delta} \Omega^2 - \frac{1}{r^2} \omega_z^2, \quad U_{KF}(r) = U_{KF} \omega_s (r)$$

$$(xx) q = \frac{2U_{KF}}{r_s^2 \Omega^2} \times \frac{\alpha}{m}$$

STABLE motion: $q \in [0; 0.9]$

DC - SUPPLY

REQUIREMENT from EXCUSION PLOT :

(1)

Force noise power spez. : $\sqrt{S_F(\omega)} \leq 3 \cdot 10^{-22} \text{ N}/\sqrt{\text{Hz}}$ $\omega = 2\pi \times$
 $\epsilon (100-1000 \text{ Hz})$

(2)

IN GENERAL, ONE CAN ESTABLISH A SIMPLE RELATION
 BETWEEN THE POWER SPECTRUM OF THE ELECTRIC FIELD
 NOISE $S_E(\omega)$ AND OF THE VOLTAGE APPLIED:

$$(III) \quad S_E(\omega) = A \frac{S_V(\omega)}{\Omega^2}$$

HERE, Ω DEPENDENT ON THE GEOMETRY AND SIZE OF THE
 TRAP ELECTRONES, N_{traps} . A IS RELATED TO THE NUMBER OF ELECTRONES
 TO WHICH A VOLTAGE IS APPLIED.

(3)

For the considered maximal voltages of $\sim 50V$
are needed. Hence,

REQUIREMENTS FOR DC-SUPPLIES:

$$(ii) S_V^{DC}(\omega) \leq 5 \cdot 10^{-16} V^2 / Hz \quad @ \begin{matrix} \omega = 100 - 1000 Hz \\ \text{and } V_{DC} = 50V \end{matrix}$$

(4)

THE REQUIREMENT TO THE AC-SUPPLY IS AT LEAST A FACTOR OF 10 SMALLER, DUE TO THE FACT THAT IT IS THE SAME SOURCE APPLIED TO THE VARIOUS ELECTRODES, THERE ARE FEWER ELECTRODES, AND IN PRINCIPLE THE NOISE WILL MAINLY ACT ON THE RADIAL MOTION. HENCE,

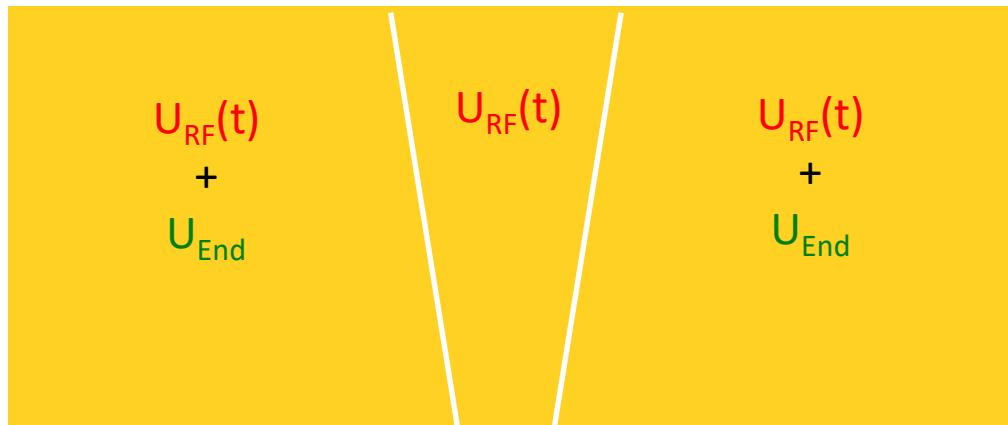
REQUIREMENTS FOR AC SUPPLY:

$$(II) S_V^{AC}(\omega) \leq 5 \cdot 10^{-15} \text{ V}^2/\text{Hz} @ \begin{array}{l} \omega = (10\omega - 100\omega_{12}) \times 2\pi \\ V_{AC} = 30 \text{ V, rms} \\ \omega_{AC} = 2\pi n(1-10 \text{ kHz}) \end{array}$$

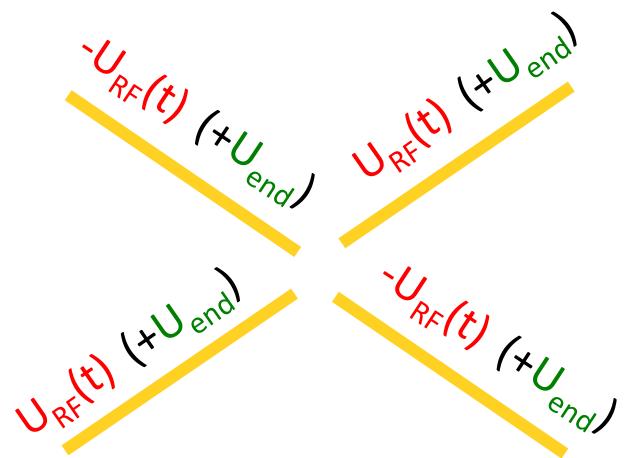
Can we meet these requirements in both potential trap configurations?

Blade electrode trap I

Blade electrode structure



Mounted electrodes
in an end view:

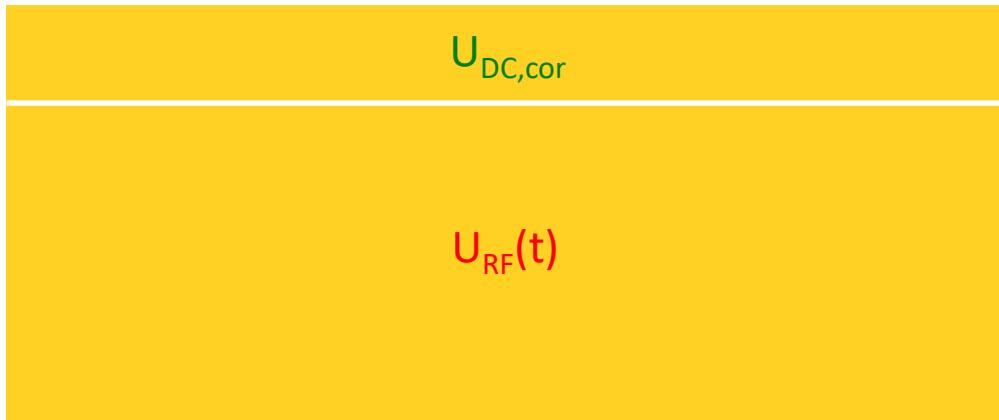


Note:

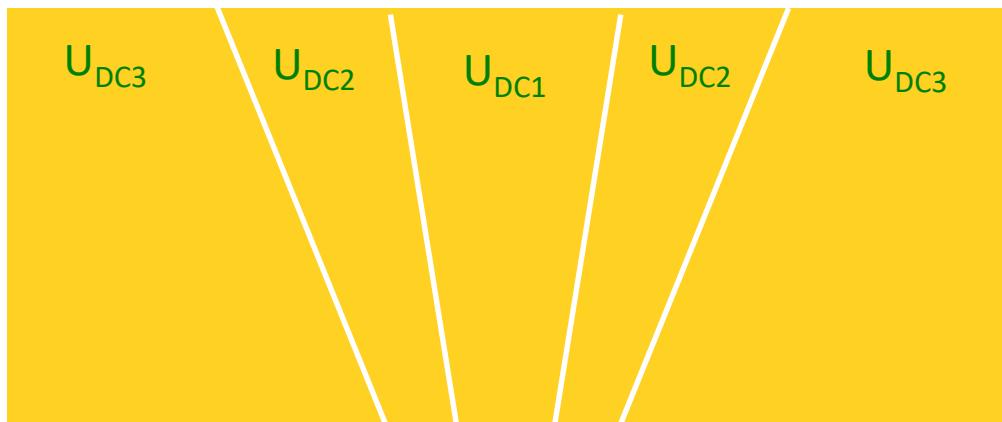
$U_{RF}(t)$ and U_{end} has to be mixed together.

Blade electrode trap II

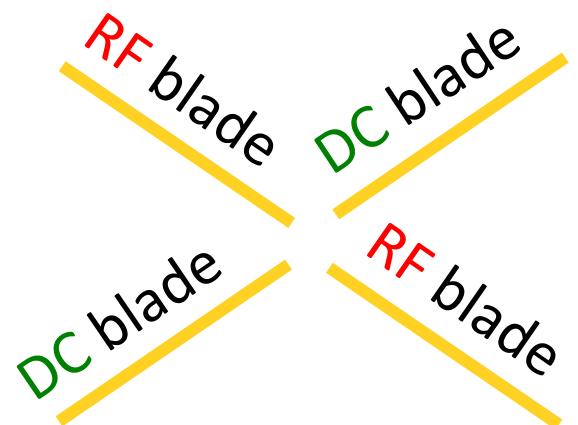
RF blade electrode



DC blade electrode



Mounted electrodes
in an end view:



No mixing of $U_{RF}(t)$
and U_{end} needed!

WHAT ABOUT HEAT WAD?

IF LEAD WIRES HAS A LENGTH OF $l = 20 \text{ cm} = 0.2 \text{ m}$

$$\Rightarrow R_{\text{wires}} = 6.7 \cdot 10^{-5} \Omega$$

$$R_{\text{resistor}} = 3 \cdot 10^{-5} \Omega$$

$\ell \sim 0.01 \text{ m}$

$$\Rightarrow R_{\text{tot}} = 20 \times (R_{\text{wires}} + R_{\text{resistor}}) \approx 2 \text{ m} \Omega. \quad (4)$$

Then the total ^{MEAN} ~~extreme~~ power dissipated is

$$\overline{P}_{\text{TOT}} = R_{\text{TOT}} \cdot \overline{i^2(t)}$$

$$= \frac{1}{2} R_{\text{TOT}} \cdot C_{\text{TOT}}^2 \cdot \mu^2 \cdot U_{\text{RF}}^2$$

For $\mu = 2\pi \times 30 \text{ kHz}$ and $U_{\text{RF}} \approx 300 \text{ V}$, one gets

(S)
$$\overline{P}_{\text{TOT}} = 1.3 \cdot 10^{-7} \text{ W} = 0.1 \mu\text{W} \ll P_{\text{Cu0}} \approx 50 \mu\text{W}$$

Enough!

ESTIMATE OF TEMPERATURE DIFF. \checkmark BETWEEN

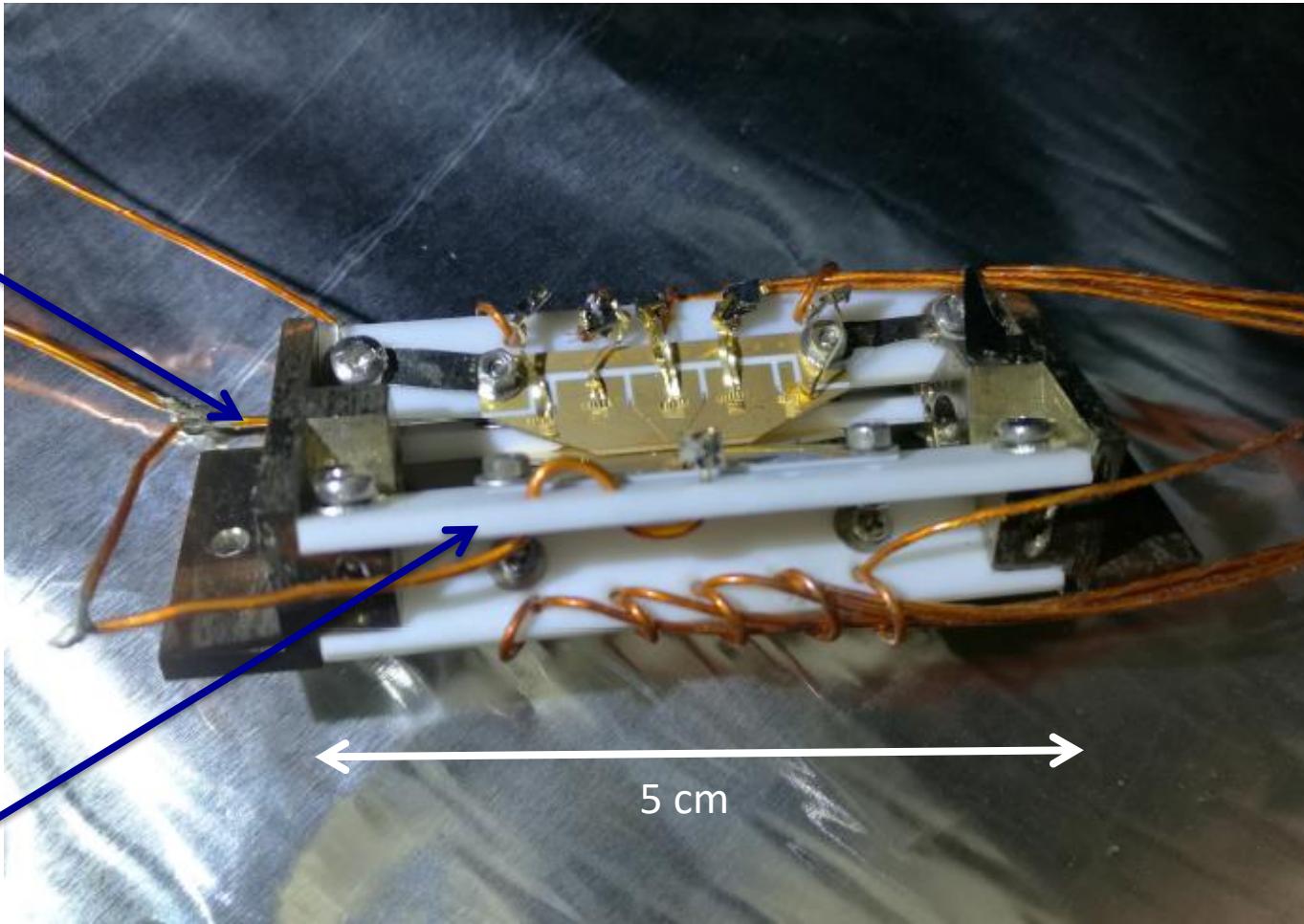
THRO A IR CHA-HEAD :

ESTIMATE OF HEAT LOAD FROM WIRES

GOWG FROM 4K → 20 mK

Another option for blade support constructed by Shuoming An, Tsinghua Uni.

Copper



Shapal™

5 cm

III) Passive NC cooling

NOTES ON RADIATIVE AND BUFFER GAS COOLING

RADIATIVE COOLING:

$$\left\{ \frac{dE_{NC}}{dt} = -A \cdot \sigma T^4, \quad A = 4\pi \cdot r_{NC}^2 \text{ AND} \right.$$

$\sigma = \text{STEFAN-BOLTZMANN CONST}$
 $= 5.67 \cdot 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$

$$E_{NC} = C_{\text{tot}}(T) \cdot T = \frac{4\pi}{3} \rho_{NC} \cdot r_{NC}^3 C_m(T) \cdot T,$$

$C_m(T) = \text{HEAT CAPACITY/kg}$



$$(8) \quad \left\{ \frac{dT}{dA} = -\alpha_R(T) T^4, \quad \right.$$

$$\alpha_R(T) = \frac{3\sigma}{C_m(T) \cdot \rho_{NC} \cdot r_{NC}}$$

①

ASSUME $\alpha_K = \text{const}$:

$$\frac{dT}{dt} = -\alpha_K T^4 \Rightarrow \frac{1}{T^4} dt = -\alpha_K dt$$

↓ $\left[-\frac{1}{3} \frac{1}{T^3} \right]_{T_0}^T = -\alpha_K (+ - t_0)$

↓ $\frac{1}{3} \left[\frac{1}{T_0^3} - \frac{1}{T^3} \right] = -\alpha_K t \quad (t_0 \equiv 0)$

(9) $T^3 = \frac{1}{\frac{1}{T_0^3} + 3\alpha_K t}$

ASSUME now $T_{\text{final}} \ll T_0$ ($T_0 \approx 300 \text{ K}$, $T_{\text{final}} = 300 \text{ mK}$)

THEN

(10) $T \approx \beta_R t^{-\frac{1}{3}}, \quad \beta_R \equiv \frac{1}{(3\alpha_K)^{\frac{1}{3}}}$

LET'S LOOK AT TYPICAL COOLING TIMES:

$$\left\{ \begin{array}{l} r_{wc} = 50 \text{ nm}, \rho_{wp} = 2200 \text{ kg/m}^3, C_m = 700 \text{ J/(kg·K)} \\ \alpha_R = \frac{3\sigma}{C_m \rho_{wc} \cdot r_{wc}} \end{array} \right.$$

$$\alpha_R = 2.2 \cdot 10^{-6} \frac{1}{\text{s K}^3}$$

$$\beta_R = \frac{1}{(3\alpha_R)^{1/3}} \Rightarrow \beta_R = 53 \frac{\text{K}}{\text{s}^{1/3}}$$

$$T \approx \beta_R t^{-1/3} \quad \text{and} \quad T_{final} = 1 \text{ K}$$

$$(II) \quad t_{final} \approx 1.5 \cdot 10^5 \text{ sec} \sim 50 \text{ hours!}$$

NB:

EXTREMELY LOW TIME \Rightarrow THAWING AT W/W TEMP?
FOR WEEKS NEEDED?

Buffer Gas Cooling:

WE WILL ASSUME $m_{BG} \ll m_{NC}$, WHICH IS
 CLEARLY SATISFIED FOR A BUFFER GAS OF ${}^3\text{He}$!

IN THIS SCENARIO A HEAD ON COLLISION WILL LEAD
 TO THE FOLLOWING KINETIC APPROXIMATION

BEFORE COLLISION



AFTER COLLISION



HENCE

$$\begin{aligned} E_{BG}^4 &= \frac{1}{2} m_{BG} \cdot v_{BG}^{i^2} \\ &= E_{BG}^i + \frac{1}{2} m_{BG} \cdot v_{NC}^{i^2} \pm m_{BG} \cdot v_{BG}^i \cdot v_{NC}^i \end{aligned}$$

THE SIGN OF THE LAST TERM DEPENDS ON THE DIRECTION OF v_{NC}^i

(12)

So in average it will be zero, and the average
kinetic energy of the buffer gas particle will
be

$$\Delta E_{BG} = \frac{1}{2} m_{BG} \bar{v}_{BG}^2$$

Energy conservation gives hence

$$\begin{aligned} \Delta E_{BG} &= -\frac{1}{2} m_{BG} \cdot \bar{v}_{BG}^2 \\ &= -\frac{1}{2} \frac{m_{BG}}{m_{NC}} \cdot k_B T, \end{aligned}$$

(12)

Since $\frac{1}{2} k_B T = \frac{1}{2} m_{NC} \cdot \bar{v}_{BG}^2$.

If we assume a collision rate of Γ_{coll}

then we can establish the following equation

(13)

For the internal energy loss of the NC:

$$\frac{dE_{NC}}{dt} = -\Delta E_{NC} \cdot \Gamma_{coll}$$

↓

$$C_{tot}(T) \cdot \frac{dT}{dt} = -\frac{1}{2} \frac{m_{NC}}{m_{NC}} \cdot k_B \Gamma_{coll} \cdot T$$

↓

$$\frac{dT}{dt} = -\alpha_{BG} T ,$$

(13)

$$\alpha_{BG} \equiv \frac{1}{2} \frac{m_{BG}}{m_{NC}} \frac{k_B \Gamma_{coll}}{C_{tot}(T)}$$

SINCE $m_{NC} = \frac{4\pi}{3} \rho_{NC} \cdot r_{NC}^3$, $C_{tot} = \frac{4\pi}{3} \rho_{NC} \cdot r_{NC}^3 \cdot C_m$

IT MEANS $\Gamma_{coll} = \Gamma_{BG} \cdot \sigma_{coll}$, WHERE $\Gamma_{BG} = FWT \text{ OF BG IATRS}$
 $\sigma_{coll} = \pi \cdot r_{NC}^2$

$\sigma_{coll} = \text{COLLISIONAL CROSS-SECTION}$

(14)

WE CAN WRITE THE λ_{BG} AS

$$\lambda_{BG} = \frac{q}{32\pi} \times \frac{m_{BG} \cdot k_B}{\rho_{BG}^2 \cdot C_m} \times \frac{1}{r_{BG}^4} \times \Phi_{BG} \\ \approx n_{BG} \cdot \overline{v}_{BG}$$

ASSUMING THE BG ATOMS IS AN IDEAL GAS, THEN

$$\left\{ \begin{array}{l} n_{BG} = \frac{\rho_{BG}}{k_B T_{BG}} \\ \overline{v}_{BG} = \left(\frac{3k_B T_{BG}}{m_{BG}} \right)^{1/2} \end{array} \right.$$

\Downarrow

$$\Phi_{BG} = \rho_{BG} \cdot \left(\frac{3}{m_{BG} \cdot k_B \cdot T_{BG}} \right)^{1/2}$$

Ans
(14)

$$\lambda_{BG} = \frac{3^{\frac{5}{2}}}{32\pi} \times \frac{\rho_{BG}}{\rho_{BG}^2 \cdot C_m} \times \left(\frac{n_{BG} \cdot k_B}{T_{BG}} \right)^{1/2} \times \frac{1}{r_{BG}^4}$$

EXAMPLE:

(14) ↓



$$\rho_{WC} = 2200 \text{ kg/m}^3$$

$$r_{WC} = 50 \text{ nm}$$

$$c_m = 700 \text{ J/(kg·K)}$$

$$T = 1 \text{ K}$$

$$P_{BC} = 10^{-3} \text{ mbar} = 0.1 \text{ Pascals}$$

$$m_{BC} = 3 \cdot 1.6 \cdot 10^{-27} \text{ kg} = 5 \cdot 10^{-27} \text{ kg}$$

(15) ↓

$$\alpha_{BG} \approx 2 \cdot 10^{-7} \text{ s}^{-1}$$

$$t_{BG} = \frac{1}{\alpha_{BG}} = 5 \cdot 10^6 \text{ s} \approx 1000 \text{ hours}$$

 $\approx 40 \text{ DAYS}$
 $\approx 1 \text{ month}$ ☀

Solution: smaller WC's or $P_{BC} \approx 1 \text{ mbar} = 100 \text{ Pa}$??

$$\Downarrow P = 1 \text{ mbar} = 100 \text{ Pa} \text{ and } T_{\text{BG}} = 1 \text{ K}$$

$$n_{\text{BG}} = 7 \cdot 10^{24} \text{ m}^{-3}$$

(Sous μ_C : $n \approx 10^{25}$)

so ok!

$$(\lambda_{\text{de Broglie}} = 1.5 \text{ nm} @ T=1\text{K})$$

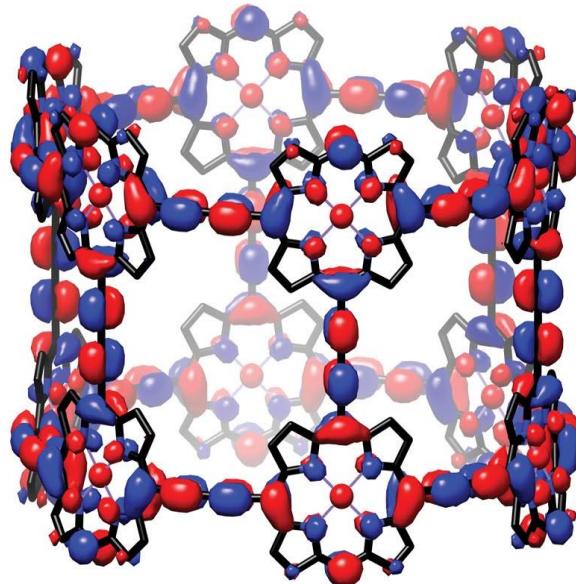
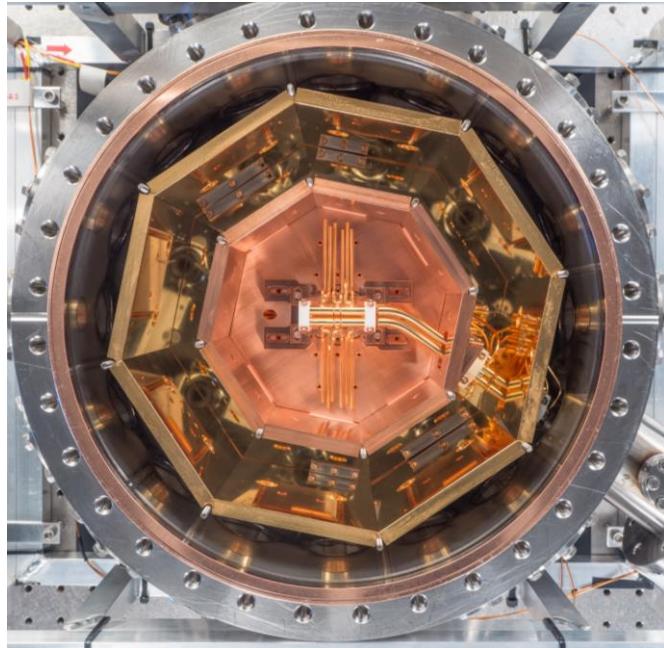
Same results would be achieved by assuming a lower T_{BG}

IV) Still unresolved issues

- I) Integrating of optical elements (Imaging and cooling)
- I) CNP loading
- II) Resistive cooling (Circuitry at 4K or lower?)
- I) Effect of charge migration on the NCs during experiments
- II) Changing in mass during an experiment due to adsorption
- I) ...

Potentially new AU TEQ contribution

Experiments med ground-state-cooled
highly-charged bio-molecule homologues
in a cryogenically cooled linear rf trap



Cryogenically cooled linear rf trap

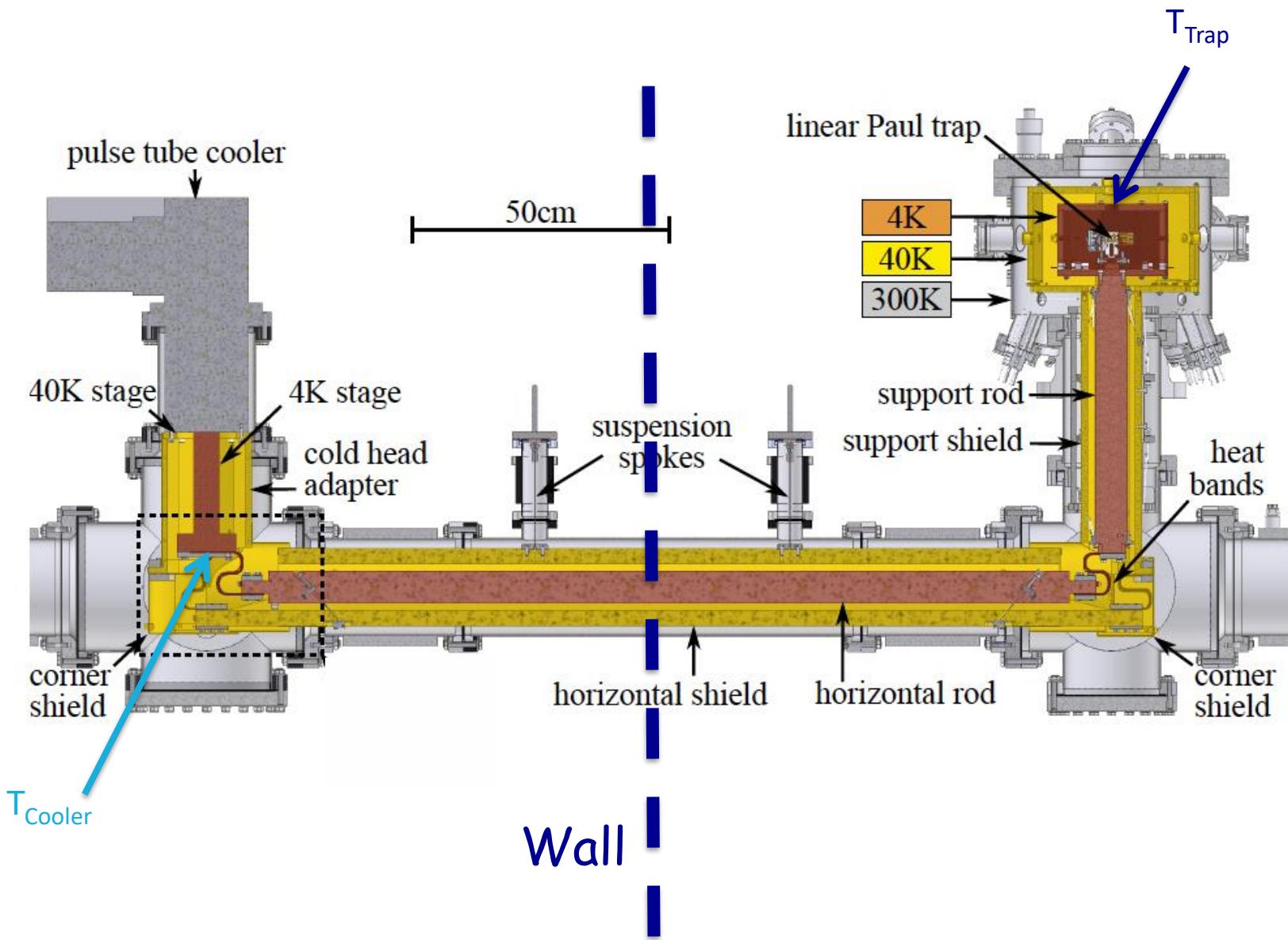
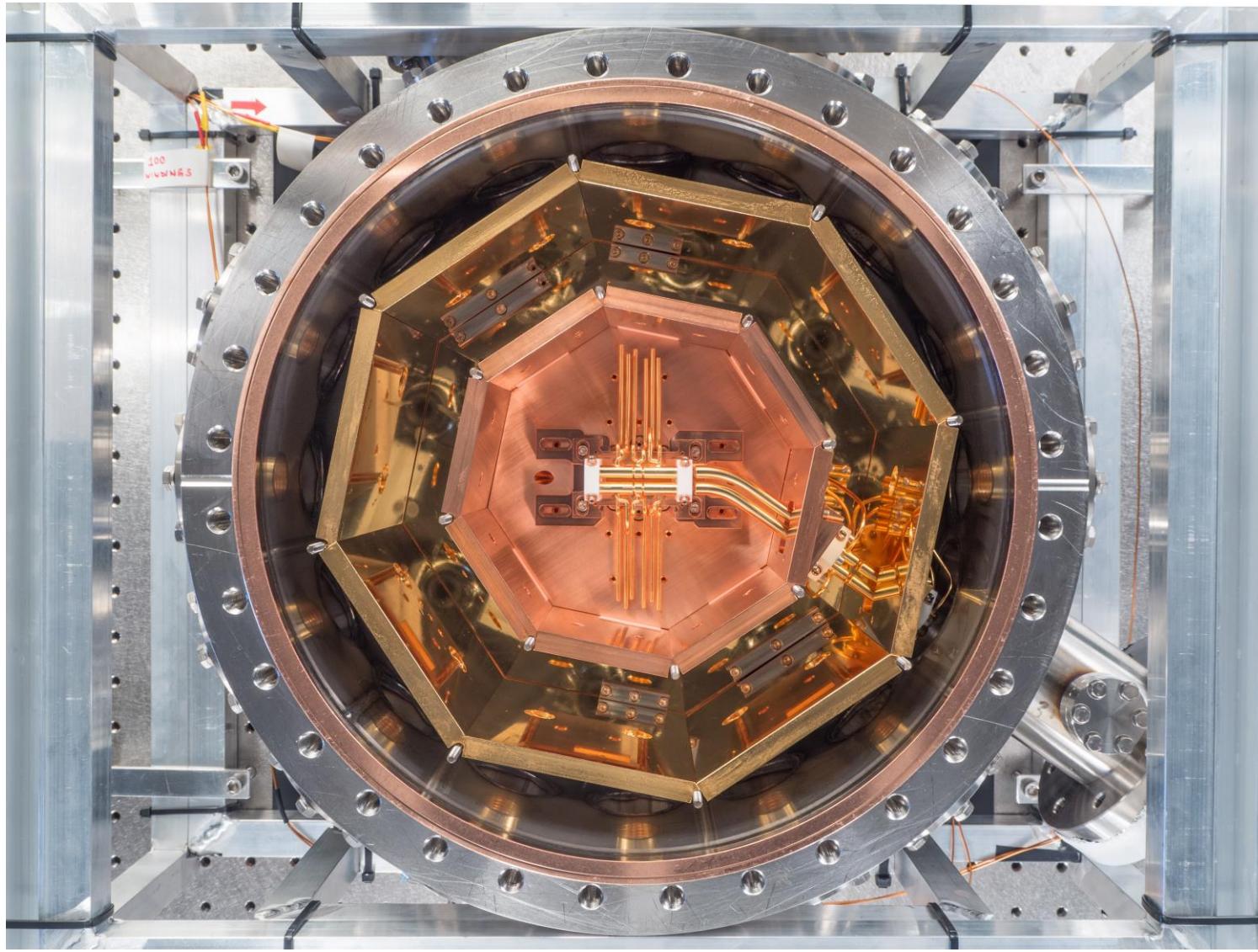


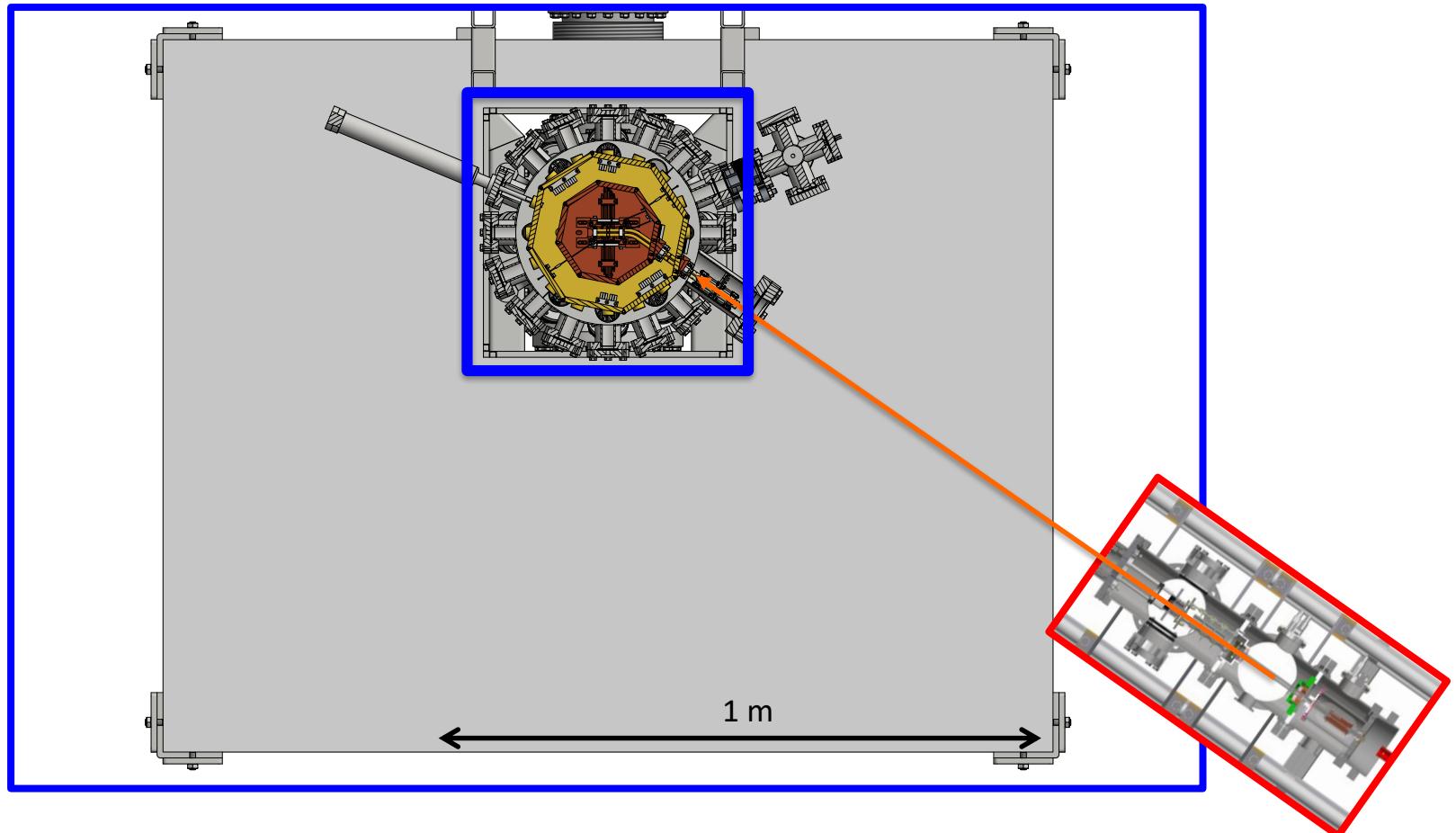
Photo of central trapping region



30 cm

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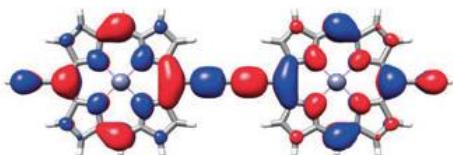


New collaborator

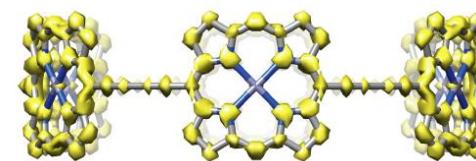


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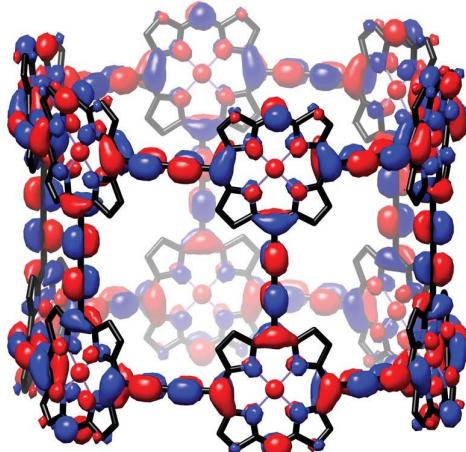
Molecular Engineering



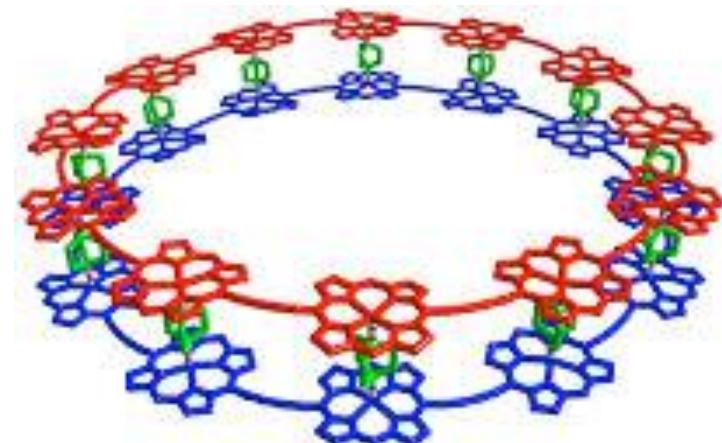
2-porphyrin



6-porphyrin

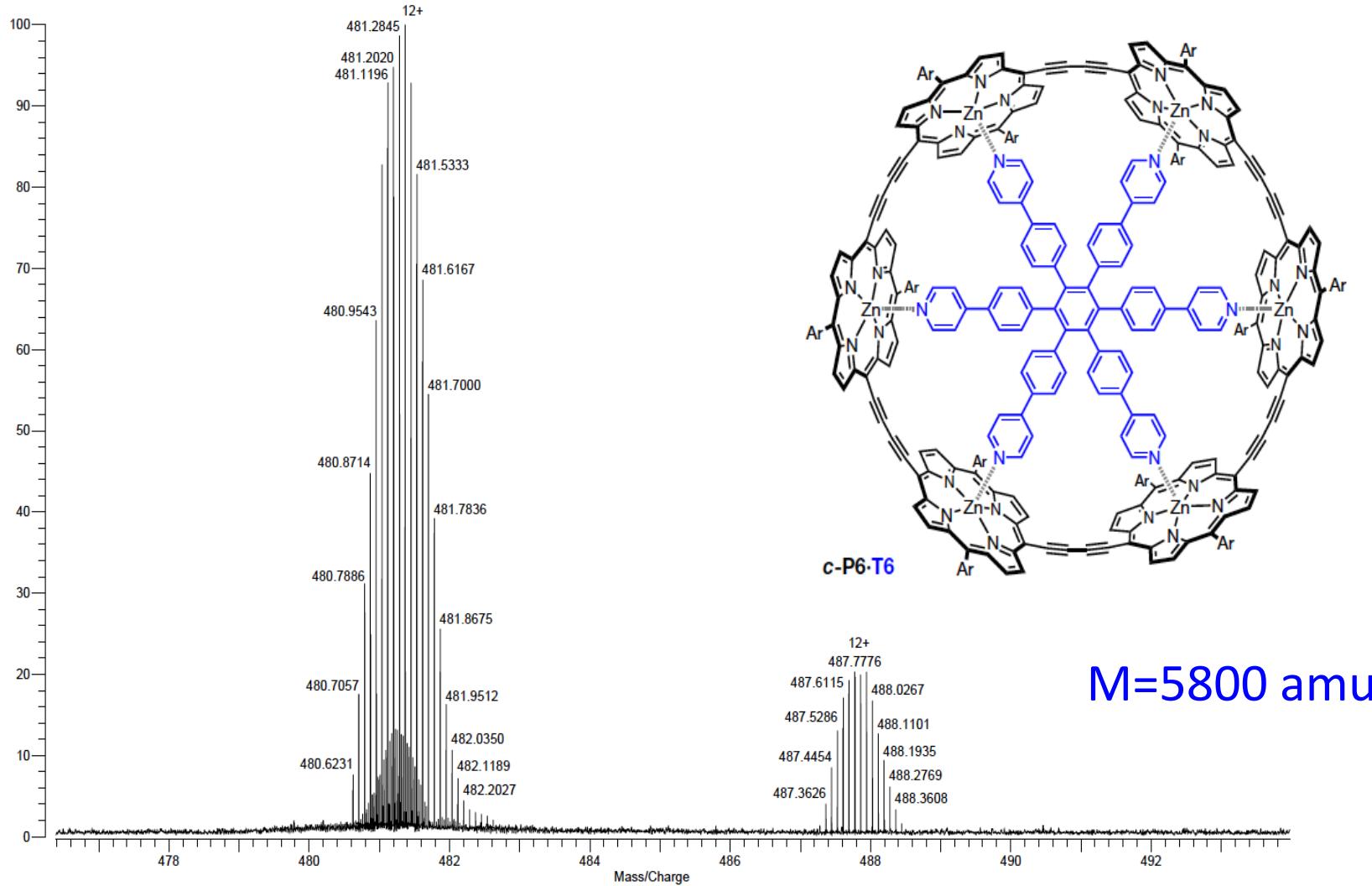


12-porphyrin

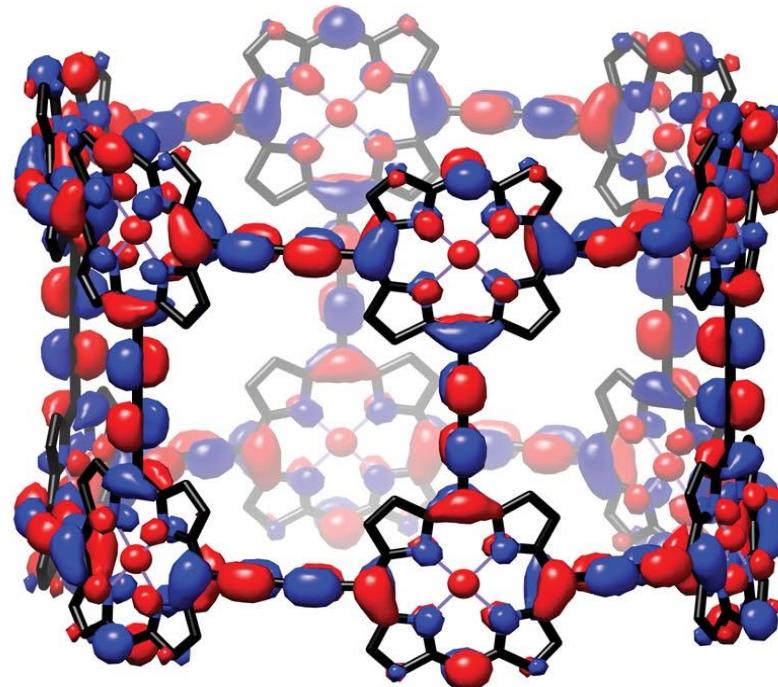


24-porphyrin

Electrospray mass spectra of highly charged c-P6•T6 porphyrine



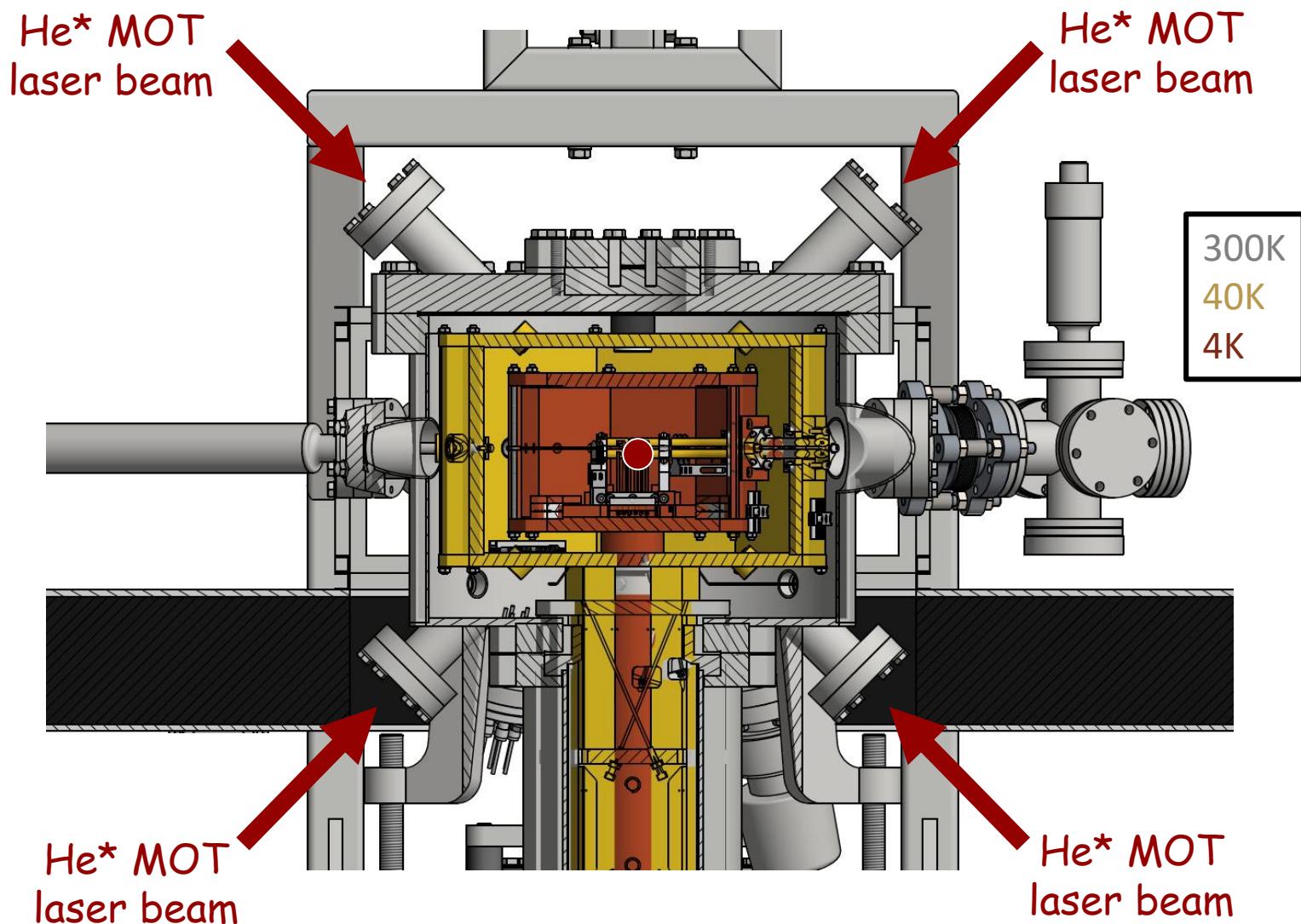
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$M > 10^4$ amu !

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Buffer gas cooling with quenched He* MOT atoms



$T_{He} \sim 1 \text{ mK} \Rightarrow$ hopefully very cold molecular ions too!

Ways towards improved detection sensitivity?

I) Creation of Schrödinger's Cat states

PRL 116, 140402 (2016)

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Observation of Quantum Interference between Separated Mechanical Oscillator Wave Packets

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$$|\psi_{\text{ent}}\rangle = \frac{1}{\sqrt{2}}(|+\rangle|\alpha\rangle + |-\rangle|-\alpha\rangle)$$

II) Quantum lock-in detection of change in motional state

Quantum Lock-in Force Sensing using Optical Clock Doppler Velocimetry

Ravid Shaniv¹ & Roee Ozeri¹

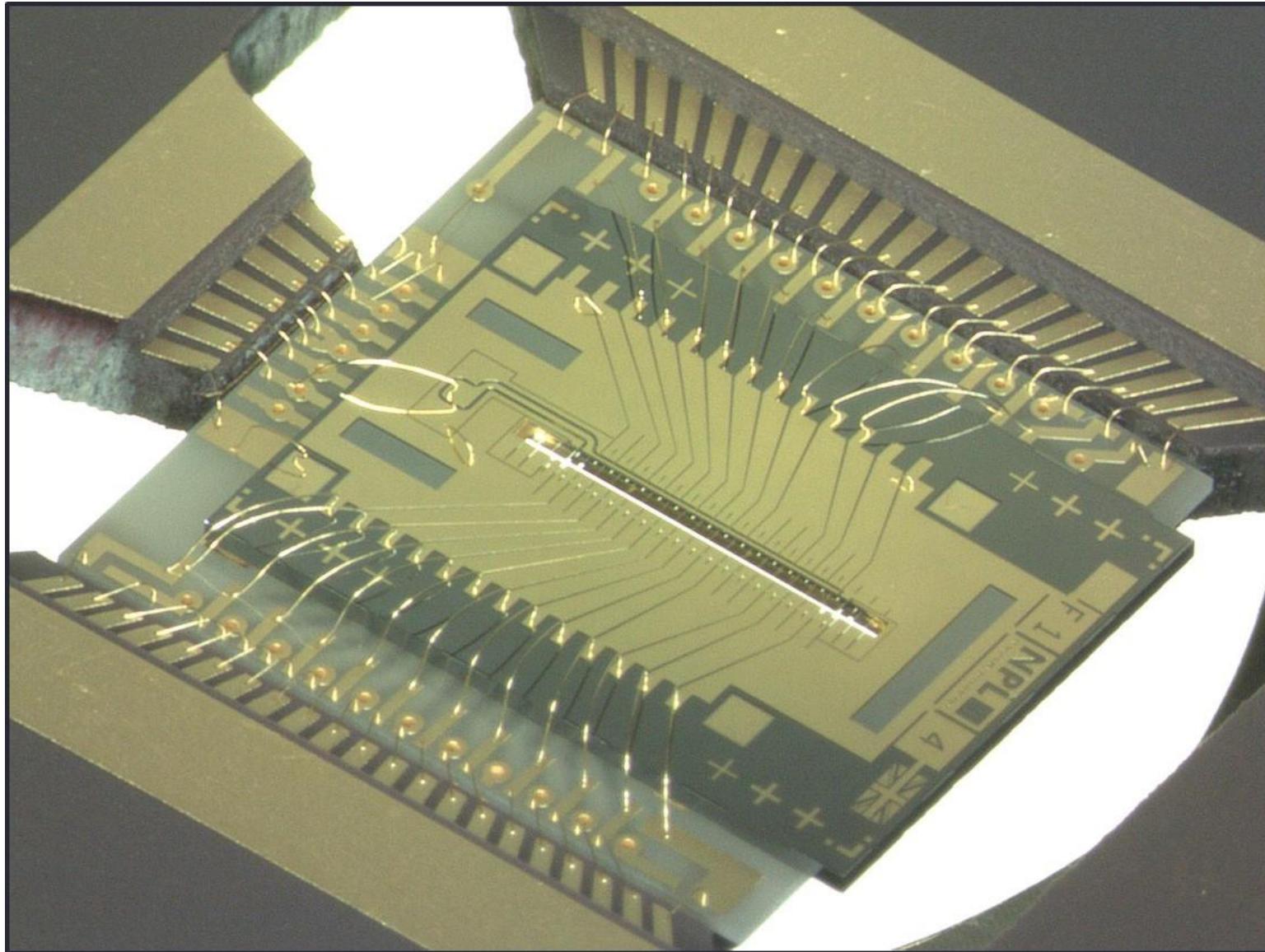
March 1, 2016

Abstract

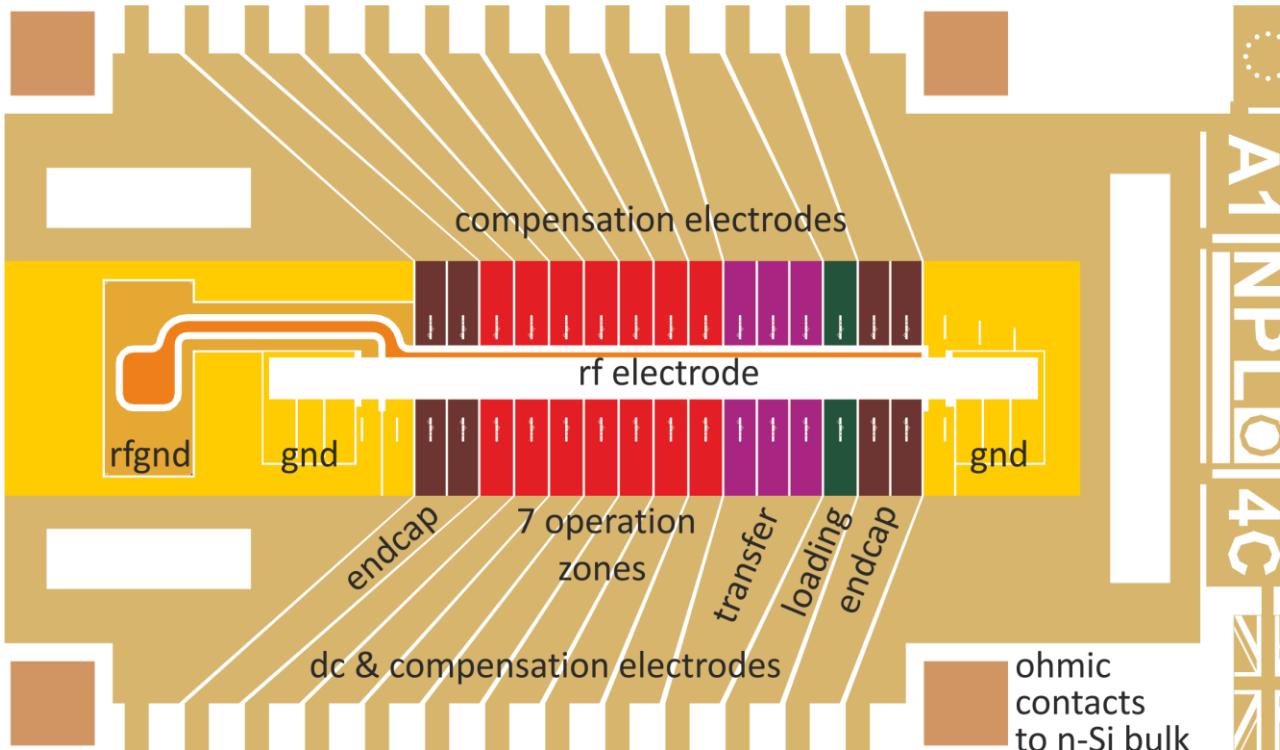
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NPL monolithic trap

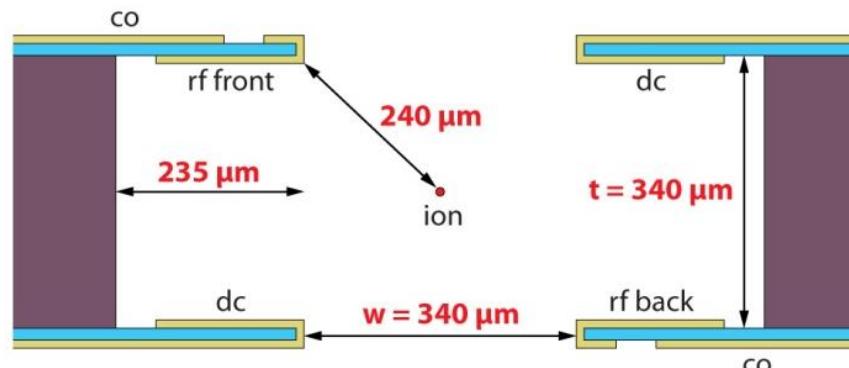


NPL monolithic trap



Electrode layout

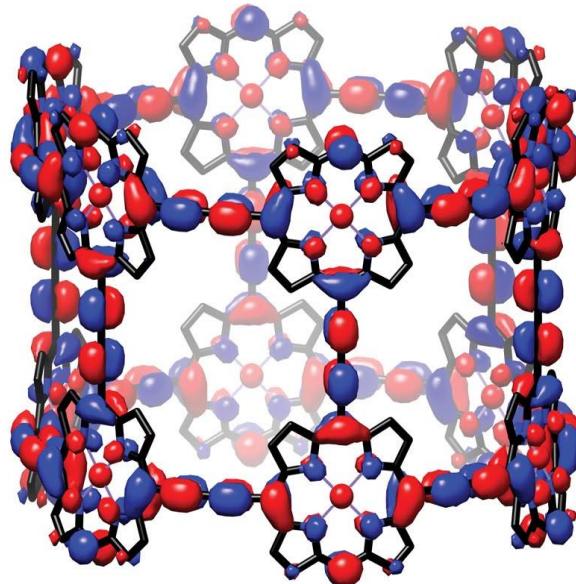
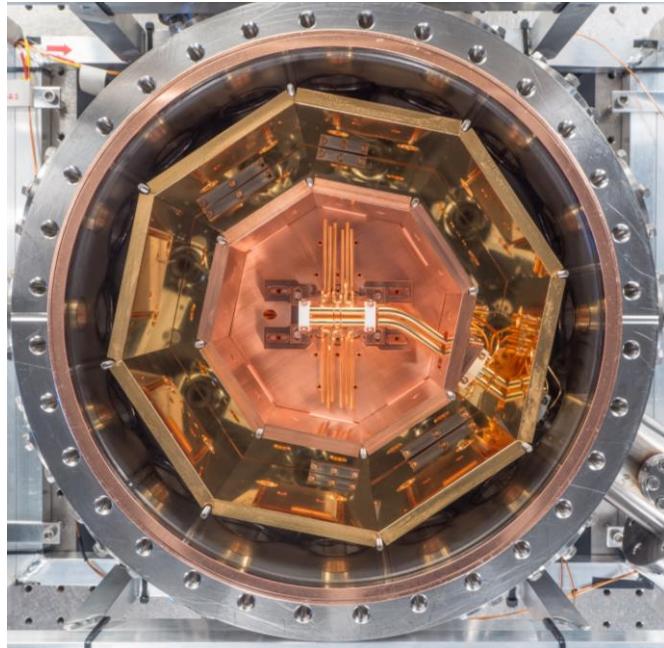
Cross-section



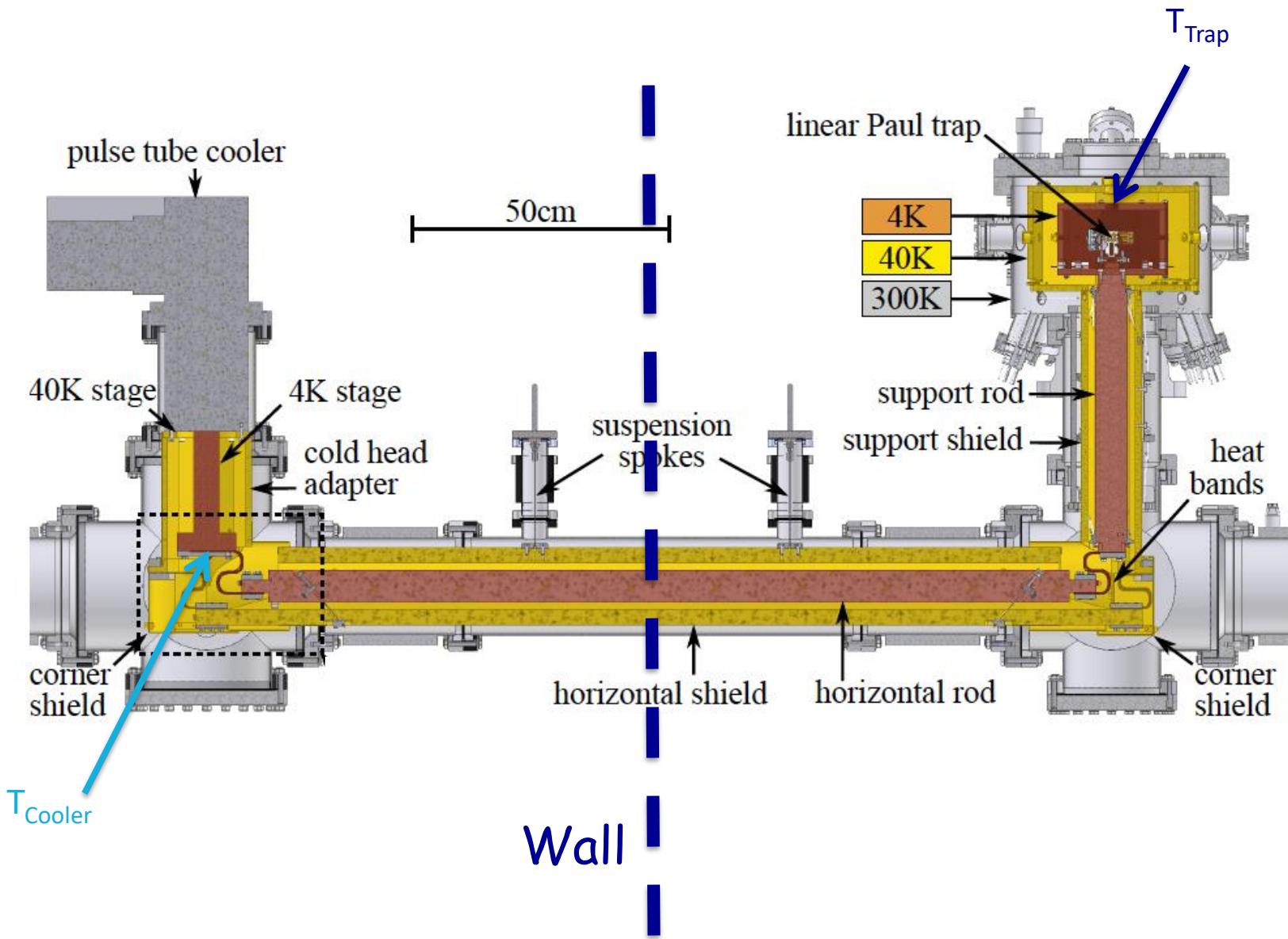
gold silicon silica

Potentially new AU TEQ contribution

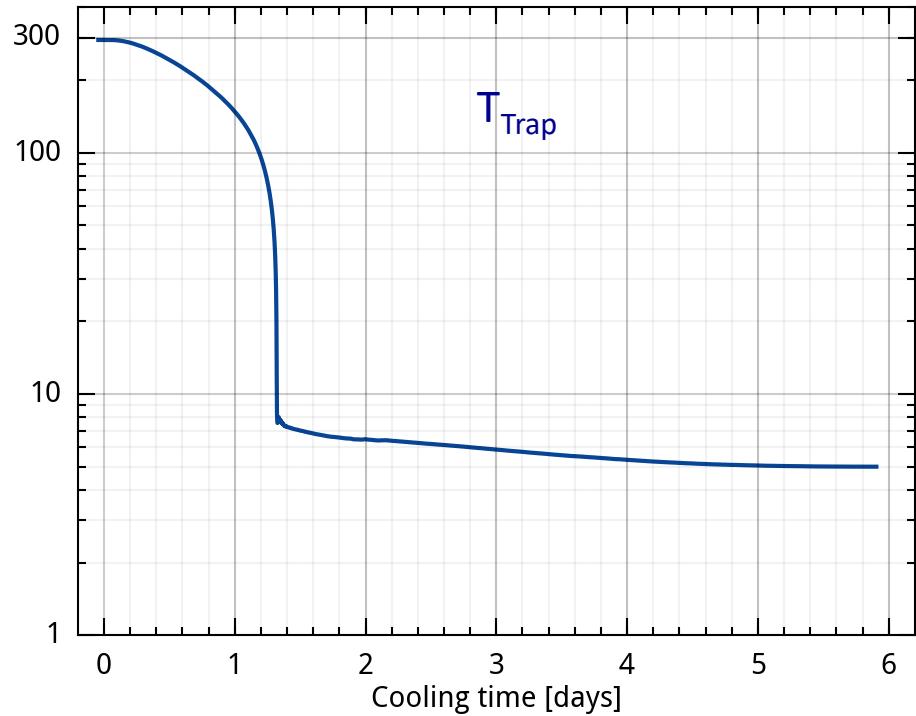
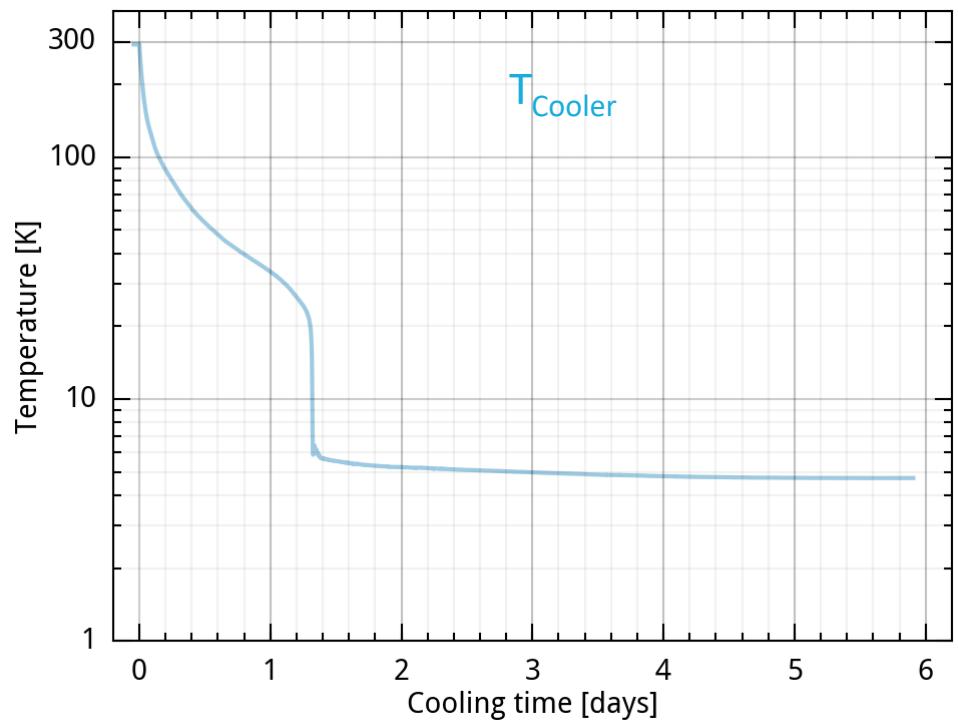
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Cryogenically cooled linear rf trap



Cryogenically cooled linear rf trap



Trap details

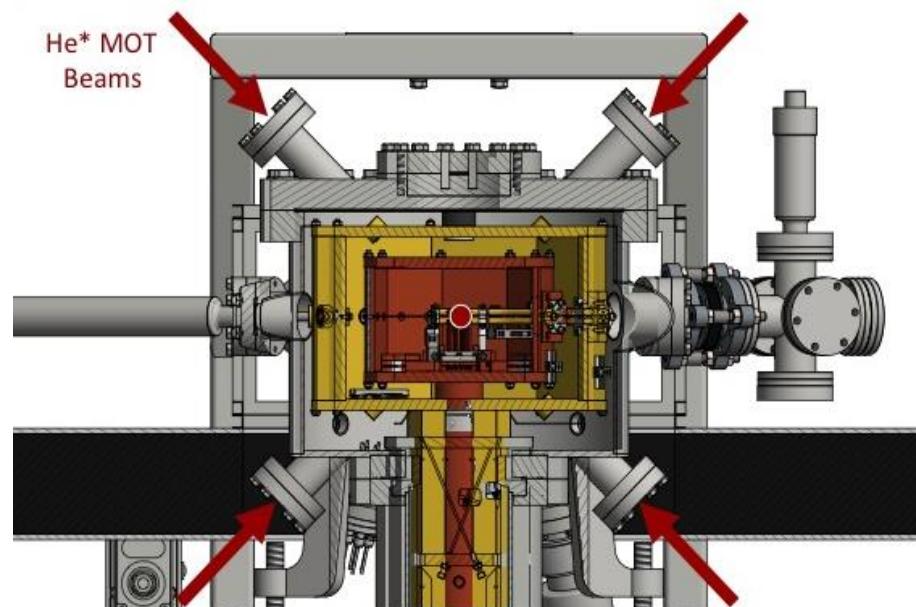
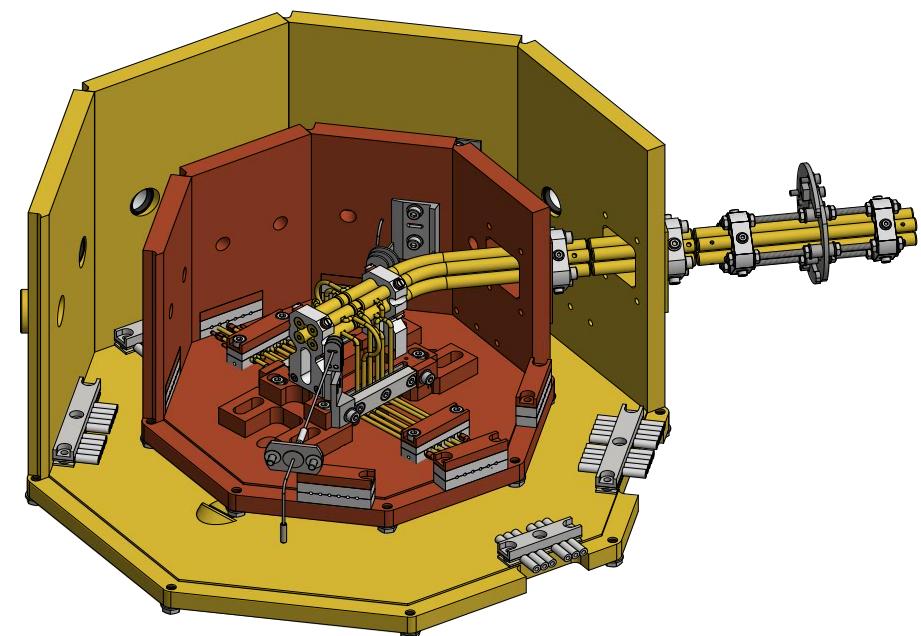
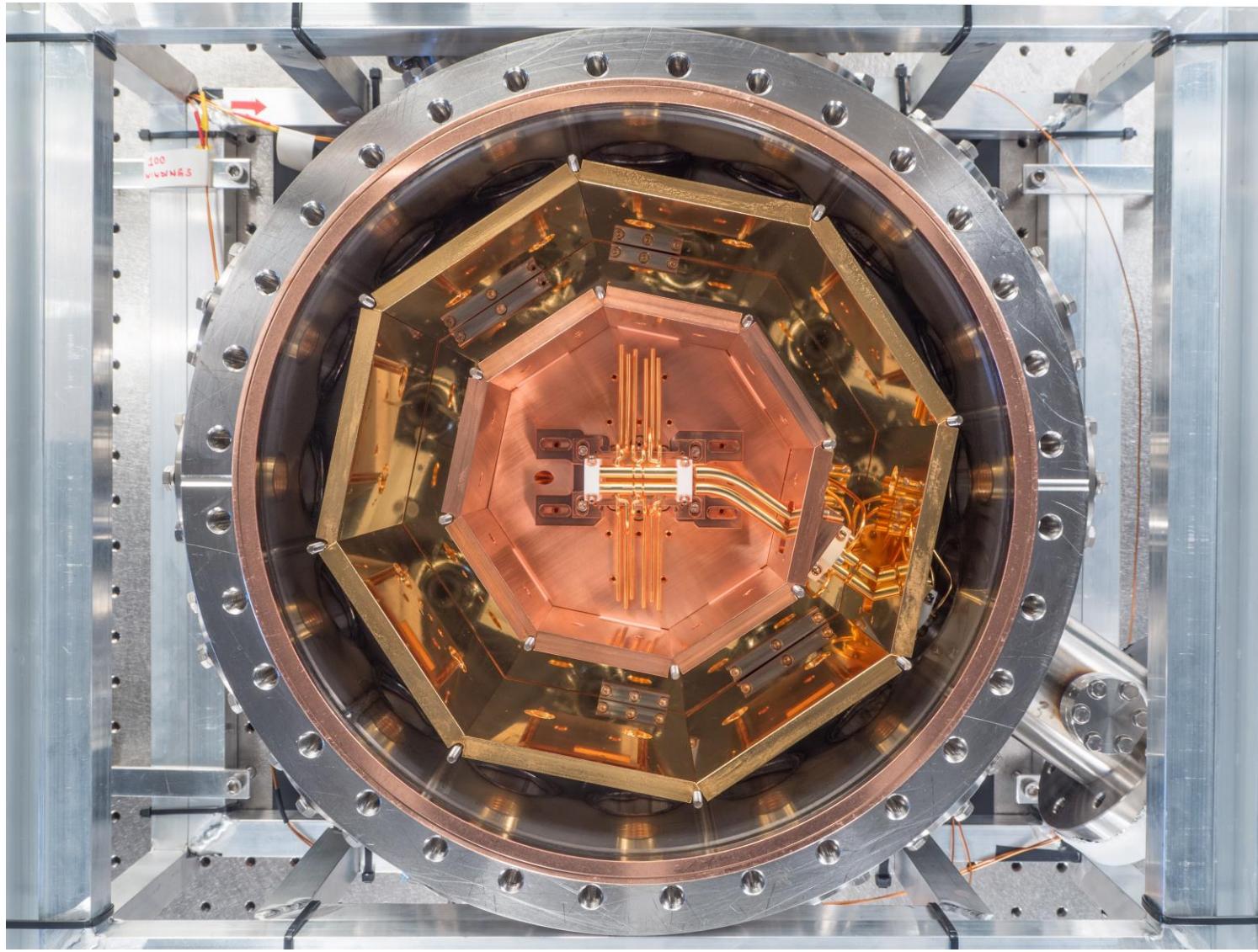


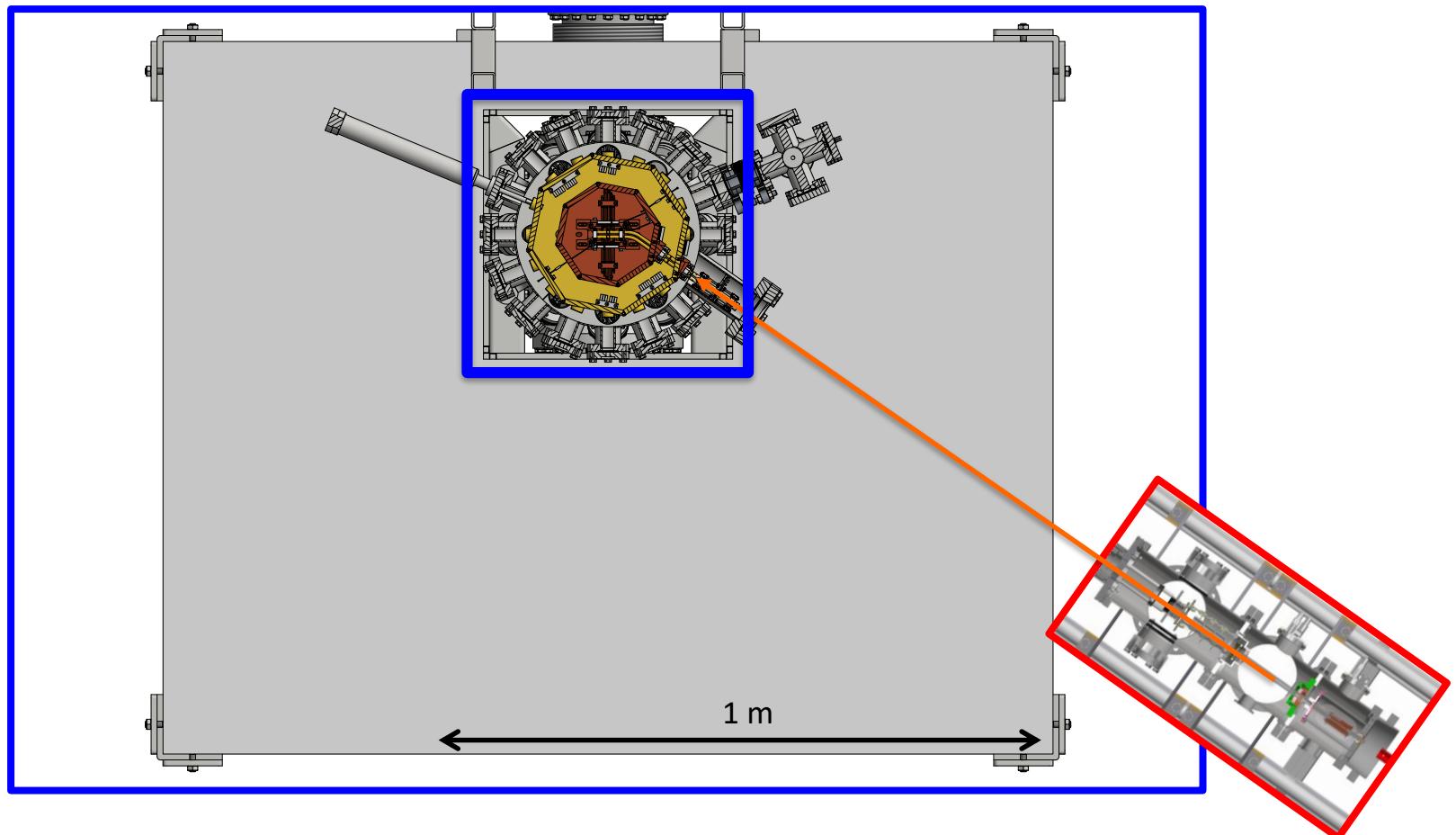
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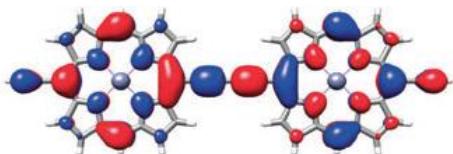


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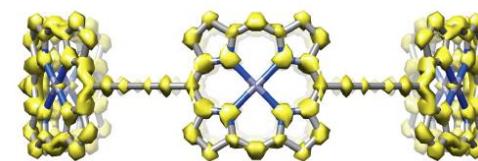


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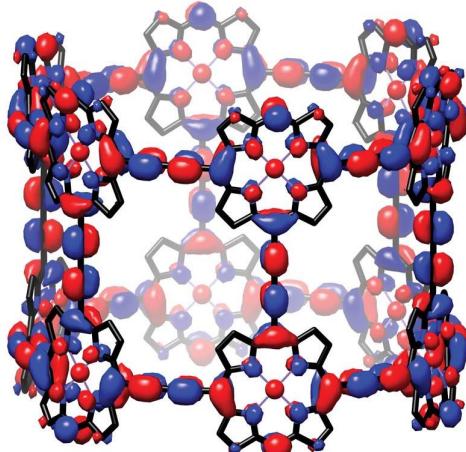
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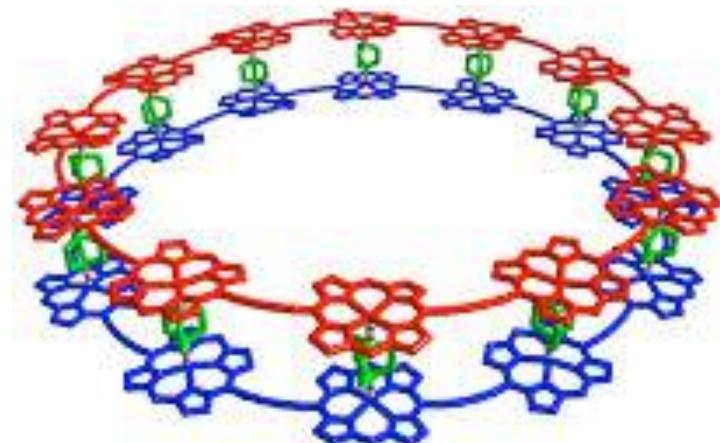
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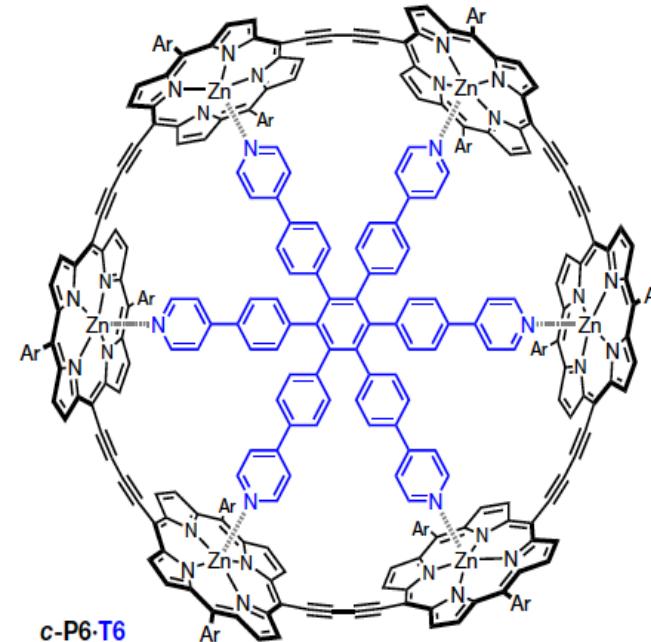
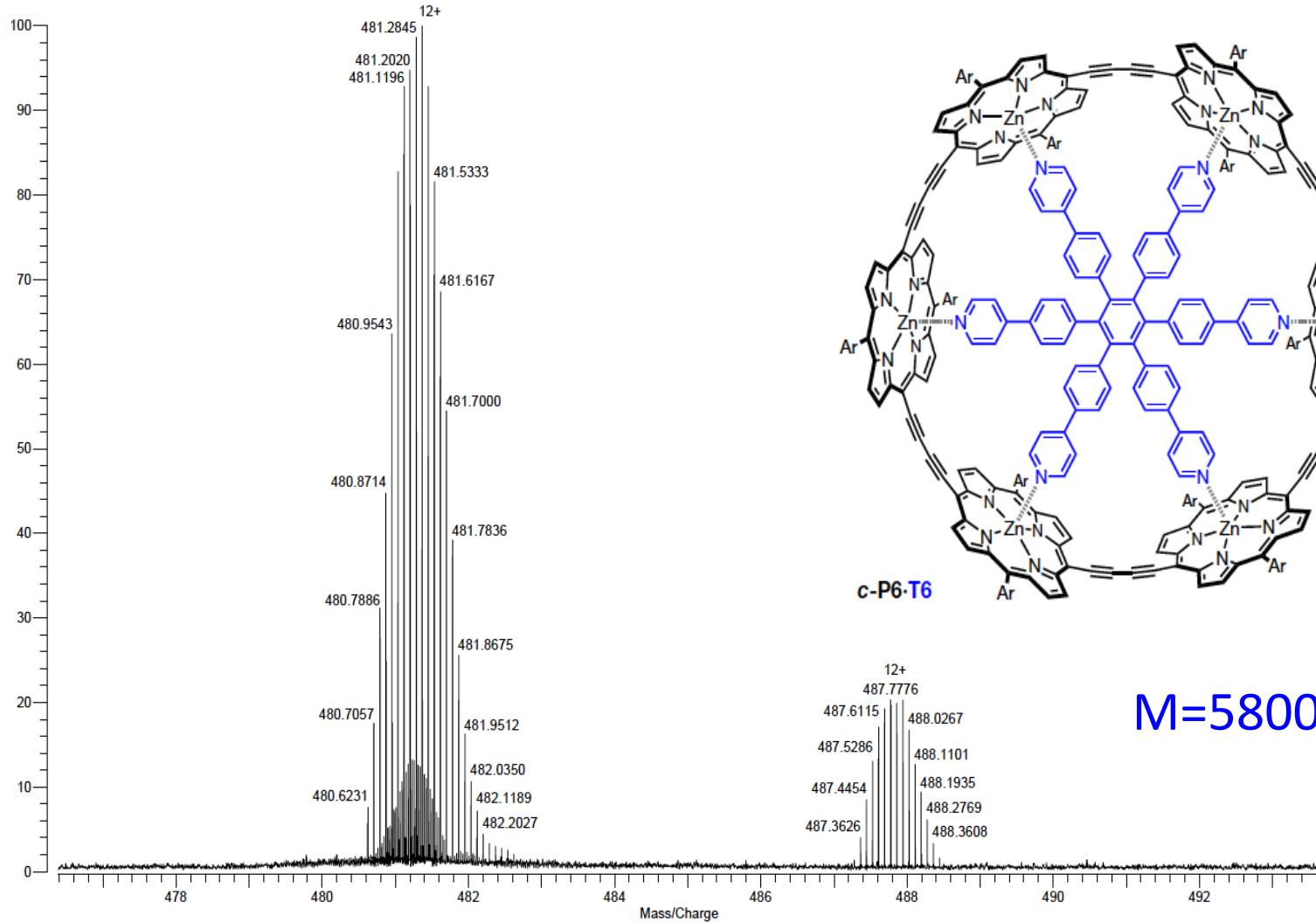


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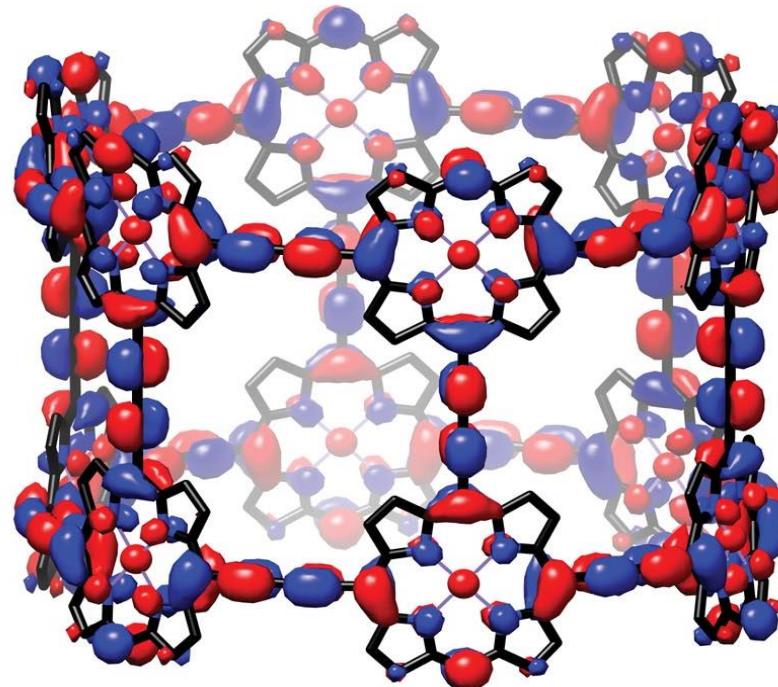
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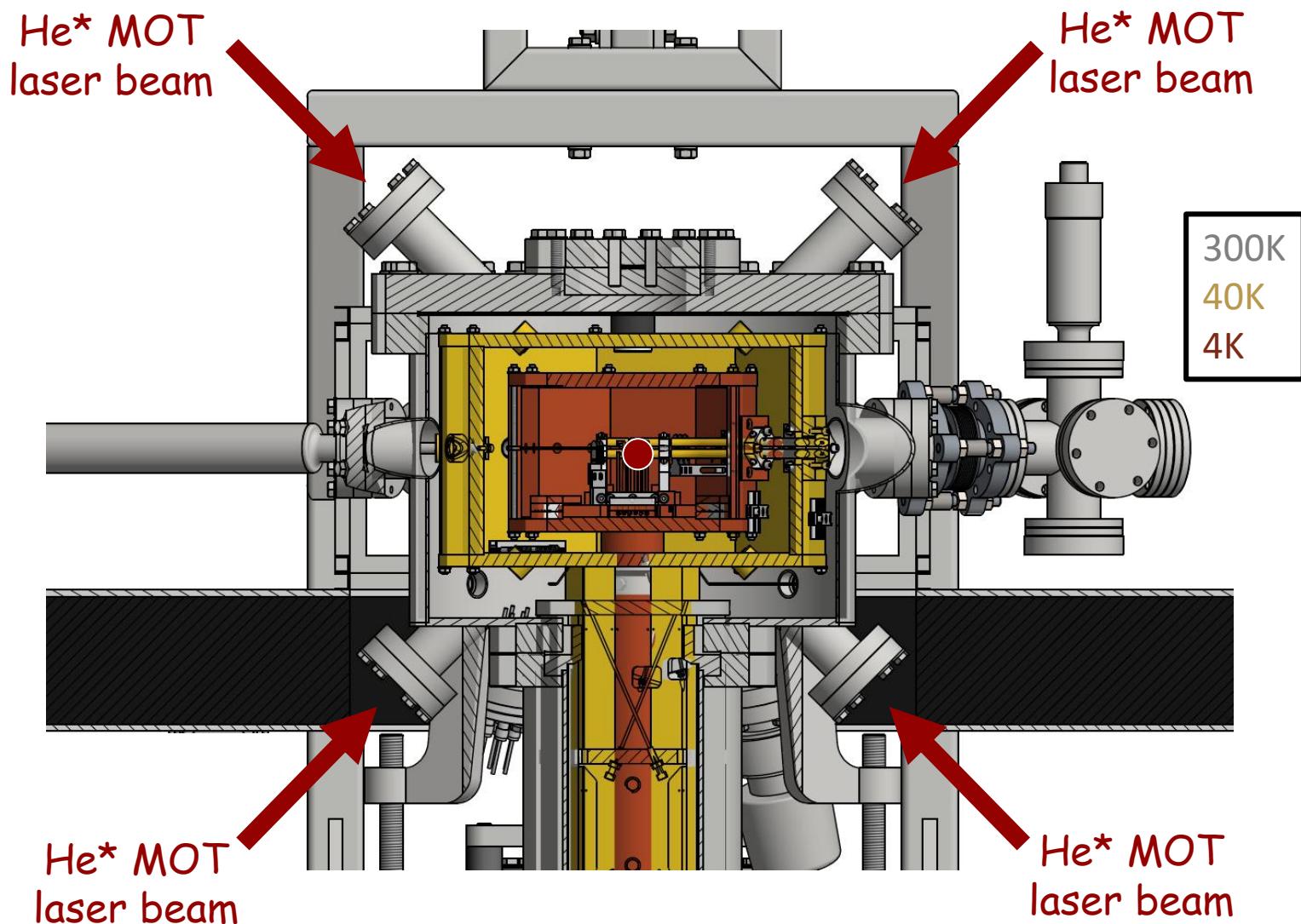
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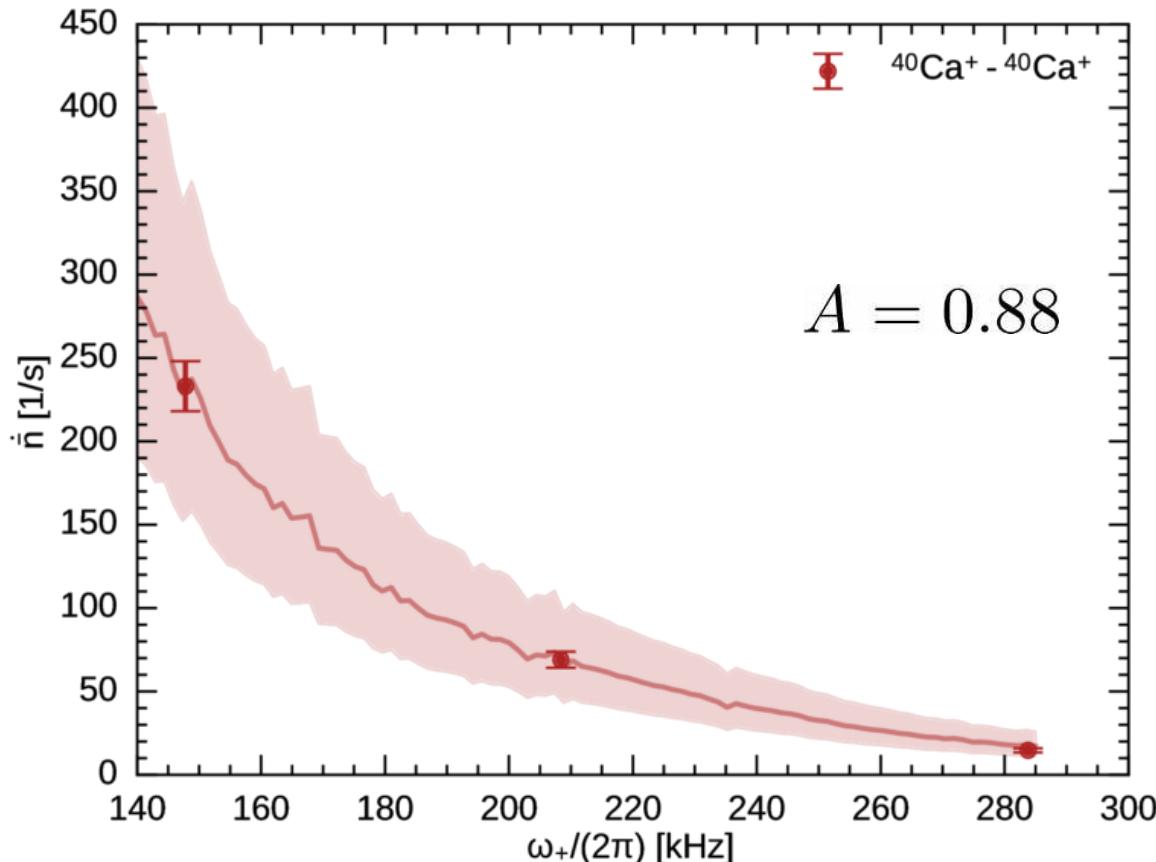
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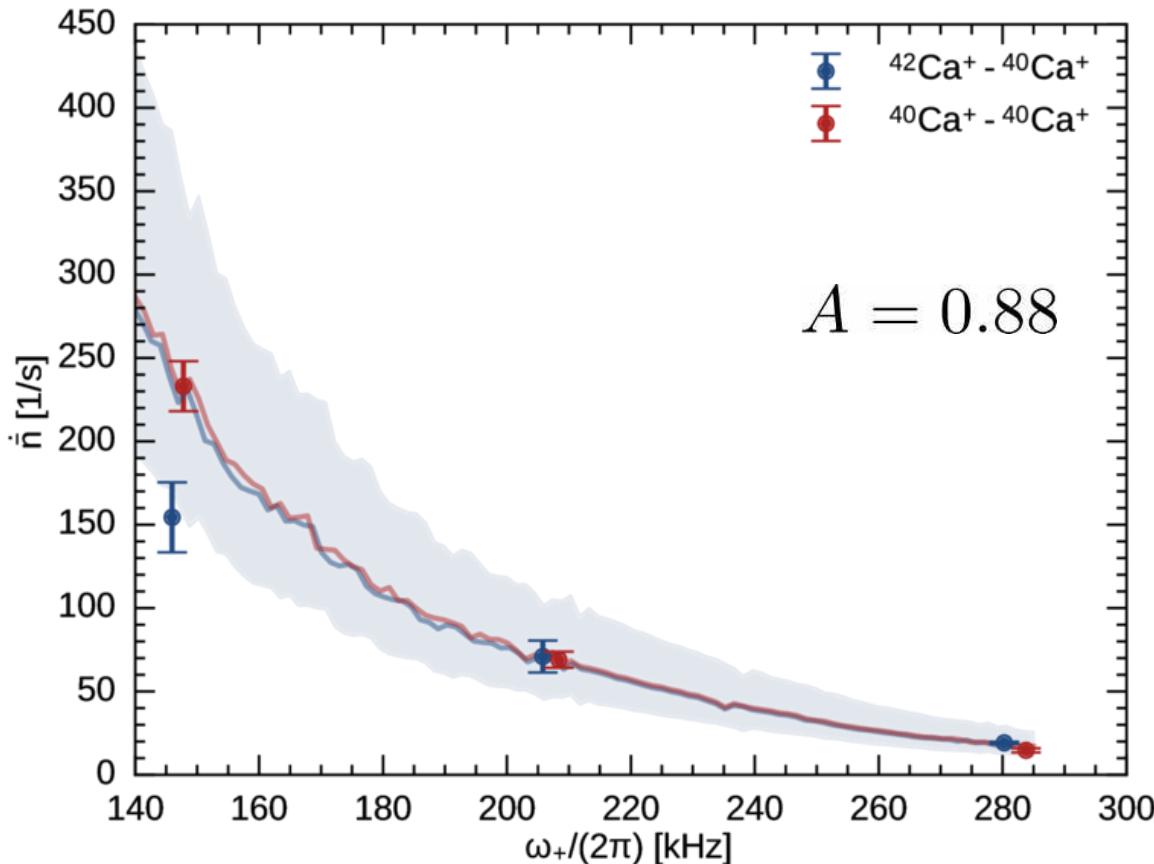
Heating of two ions

$$\dot{n} \simeq A \times 8 \frac{e^2}{4m_1 \hbar \omega_{\pm}} \frac{S_{VDC}(\omega_{\pm})}{D^2} \left(\beta_1^{\pm'} + \frac{\beta_2^{\pm'}}{\sqrt{\mu}} \right)^2$$



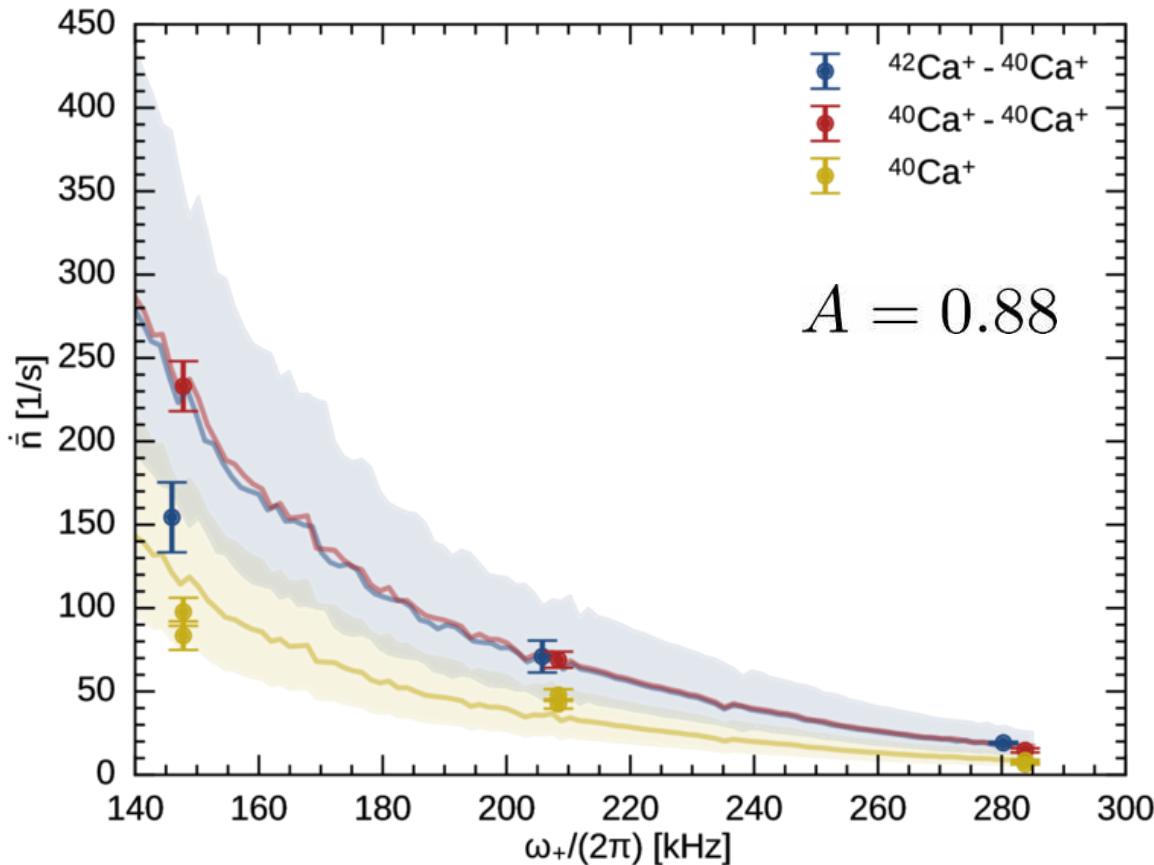
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Thermophysical properties of sapphire, AlN and MgAl₂O₄ down to 70 K

St. Burghartz, B. Schulz

Kernforschungszentrum Karlsruhe, Institut für Materialforschung I, P.O. Box 3640, 76021 Karlsruhe, Germany

SHAPAL at 100 K 2.1 W/cm K

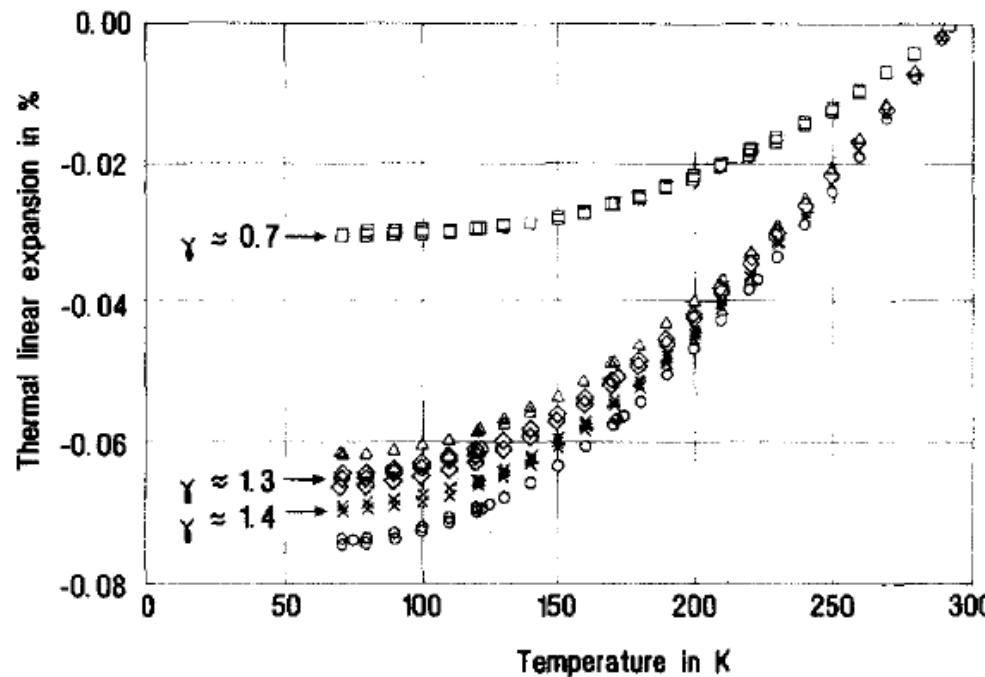
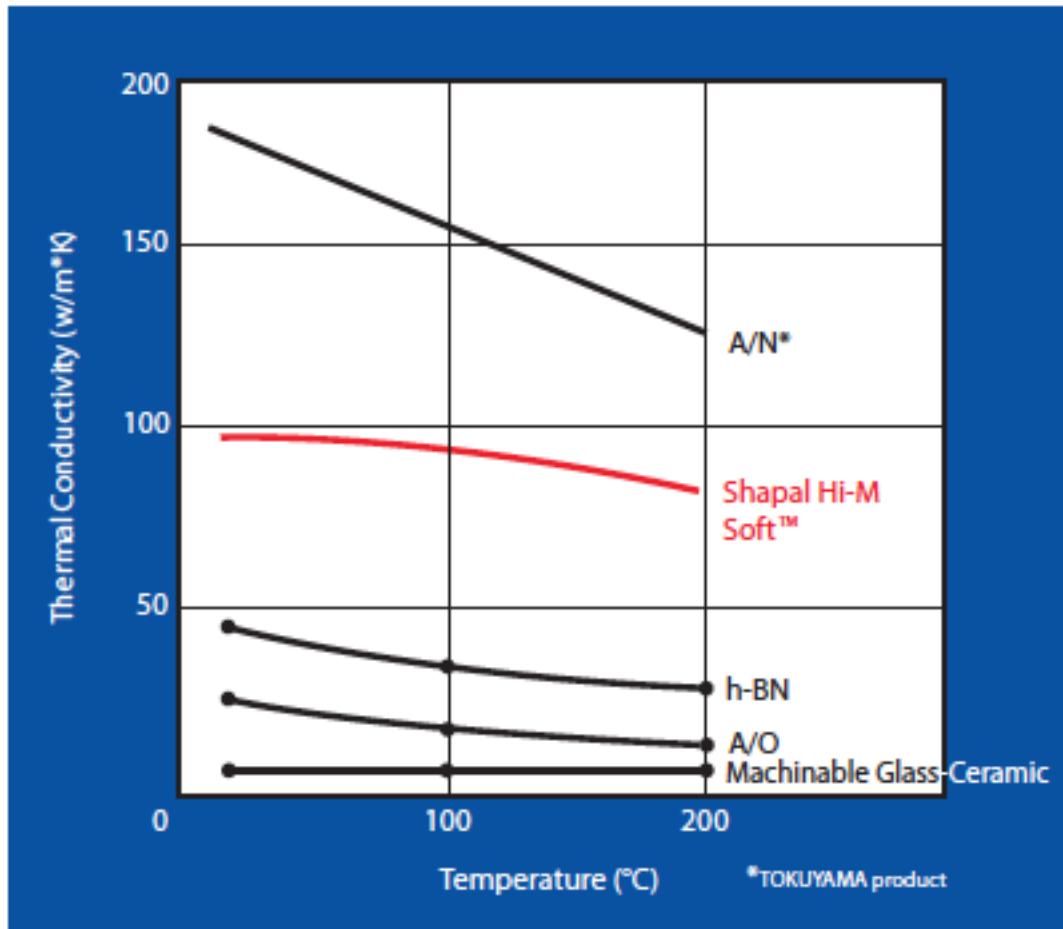
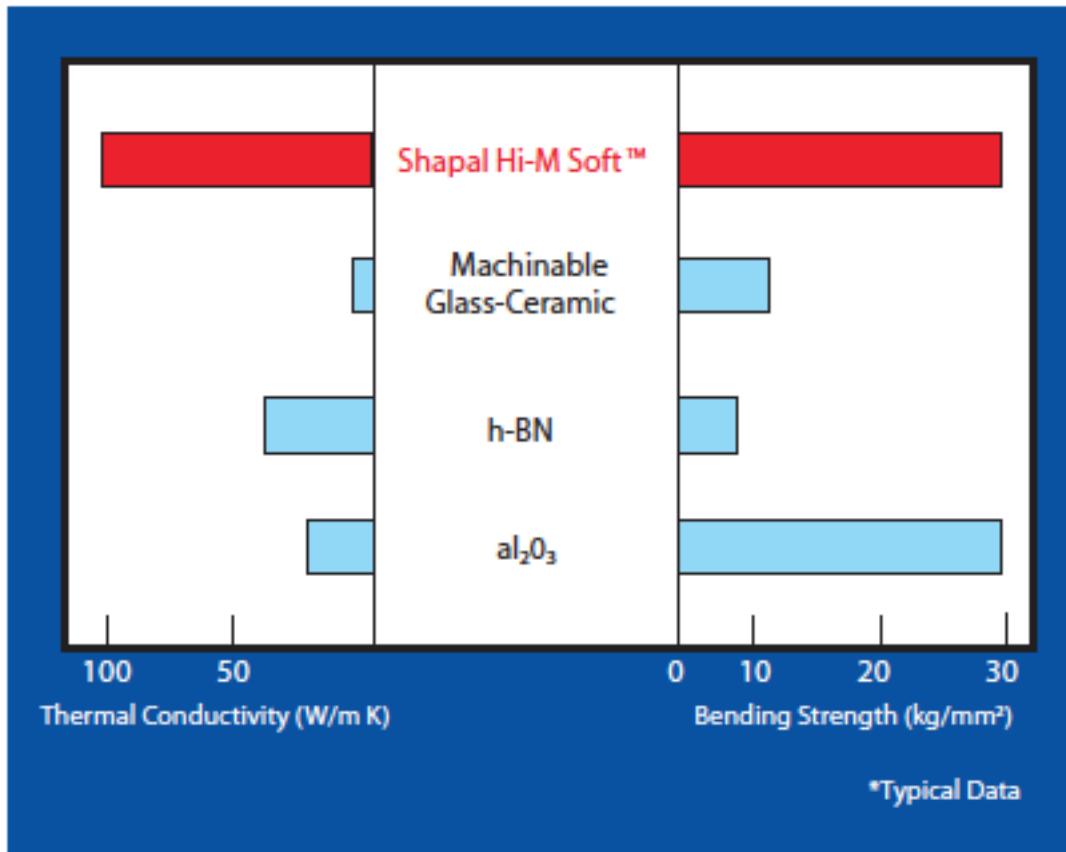


Fig. 2. Thermal linear expansion of sapphire ((○) $\parallel c$, (Δ) $\perp c$), α -Al₂O₃ (\diamond), AlN Shapal (\square) and MgAl₂O₄ (\times), γ is the Grüneisen constant.

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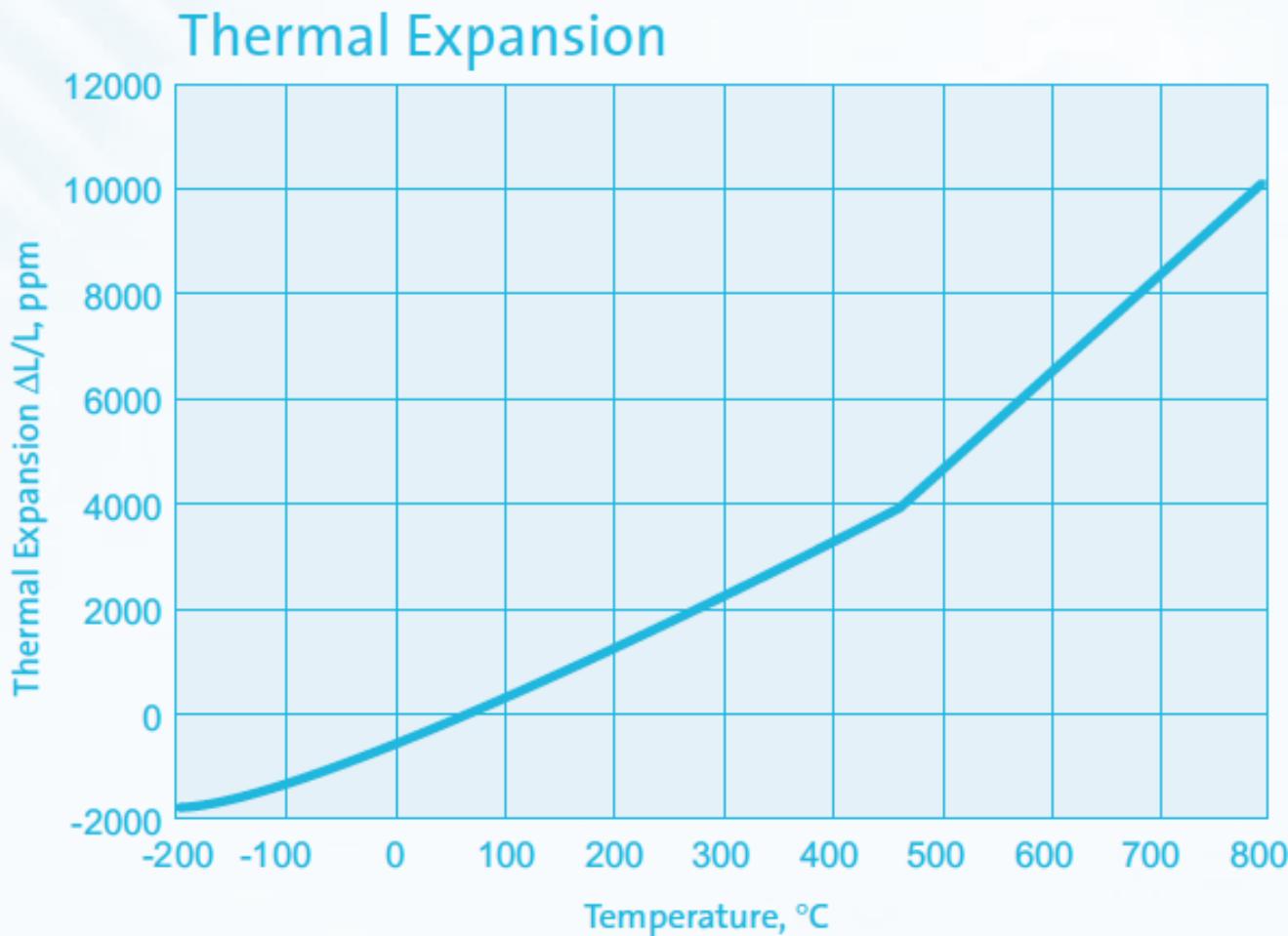


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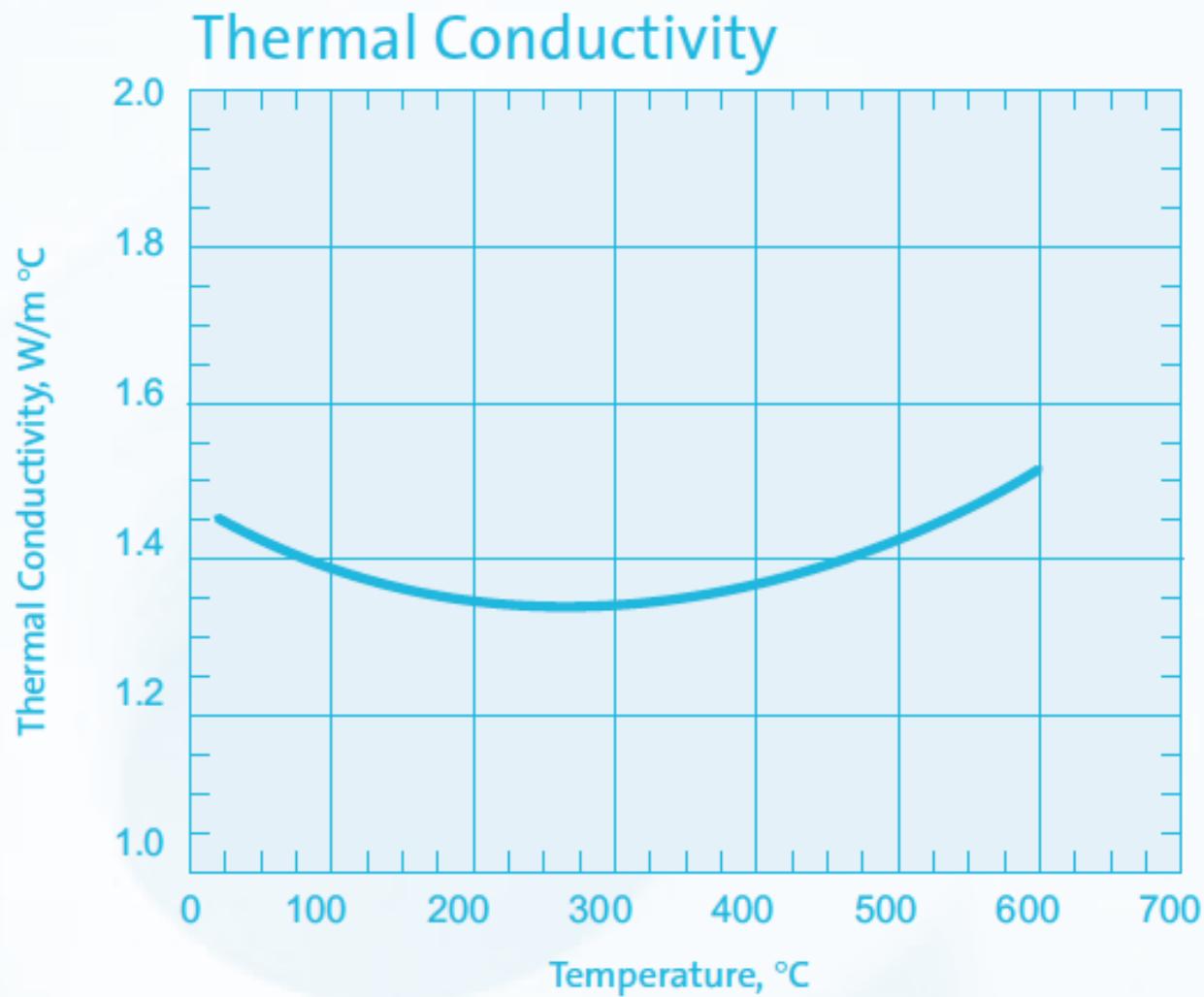
Machinable Glass Ceramic

	Approximate Weight %
Silicon - SiO ₂	46%
Magnesium - MgO	17%
Aluminum - Al ₂ O ₃	16%
Potassium - K ₂ O	10%
Boron - B ₂ O ₃	7%
Fluorine - F	4%

Macor®

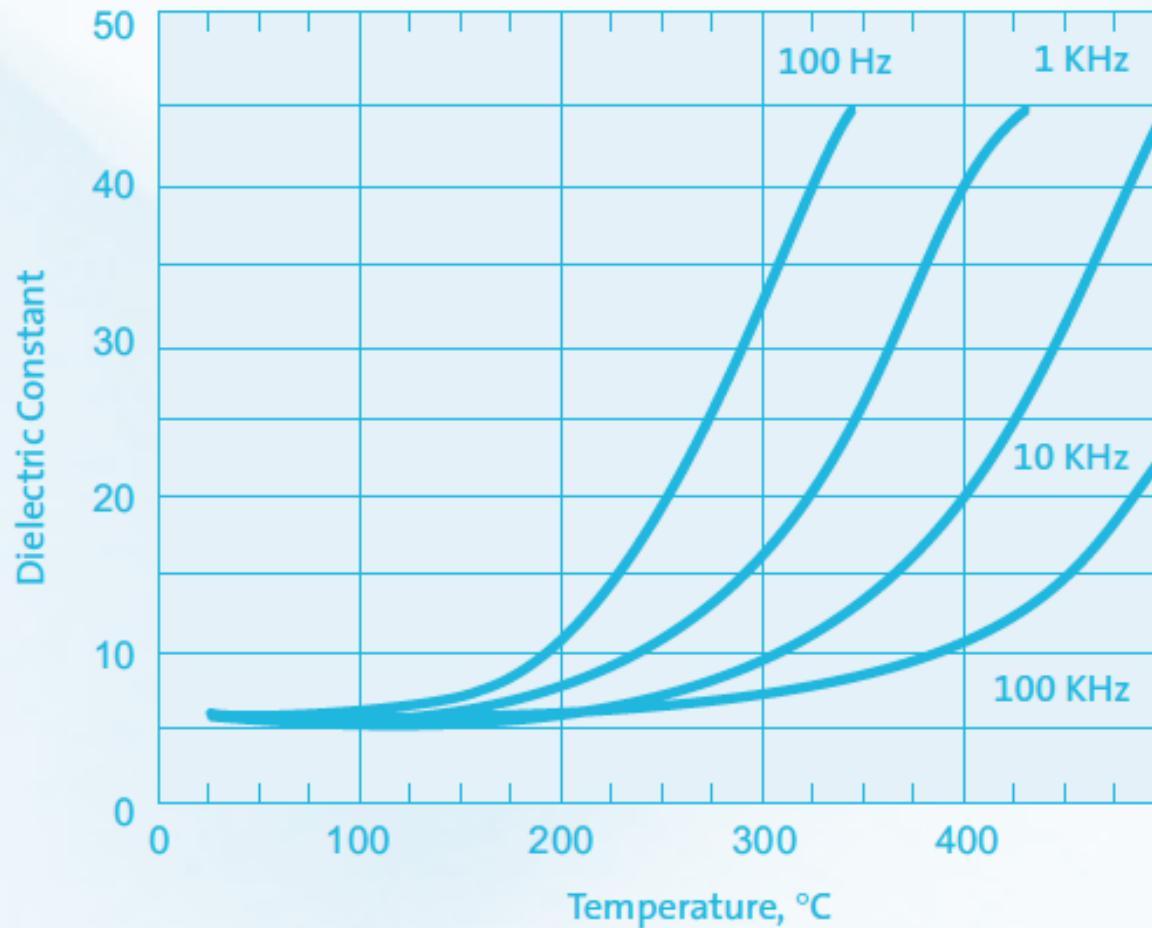


Macor®

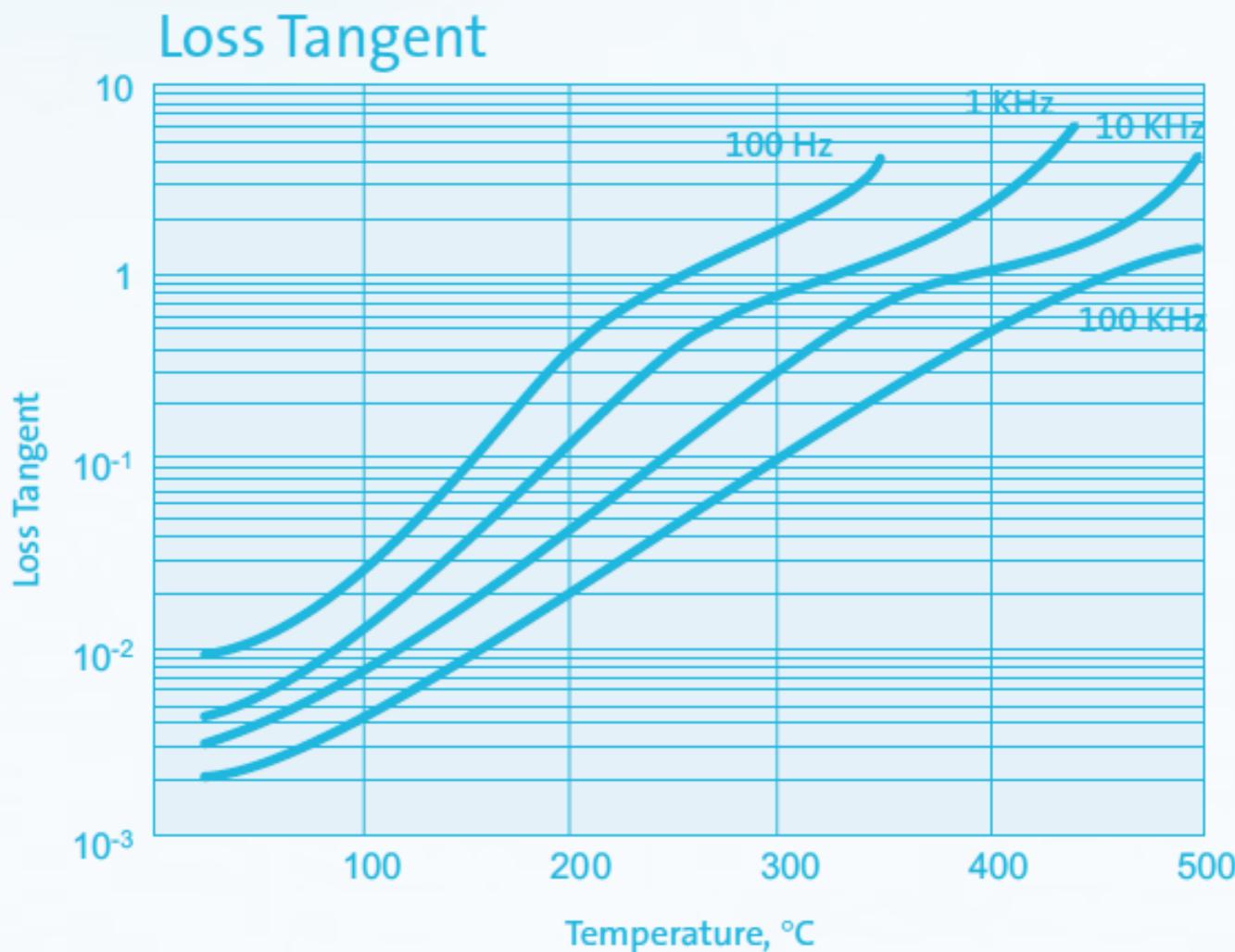


Macor®

Dielectric Constant

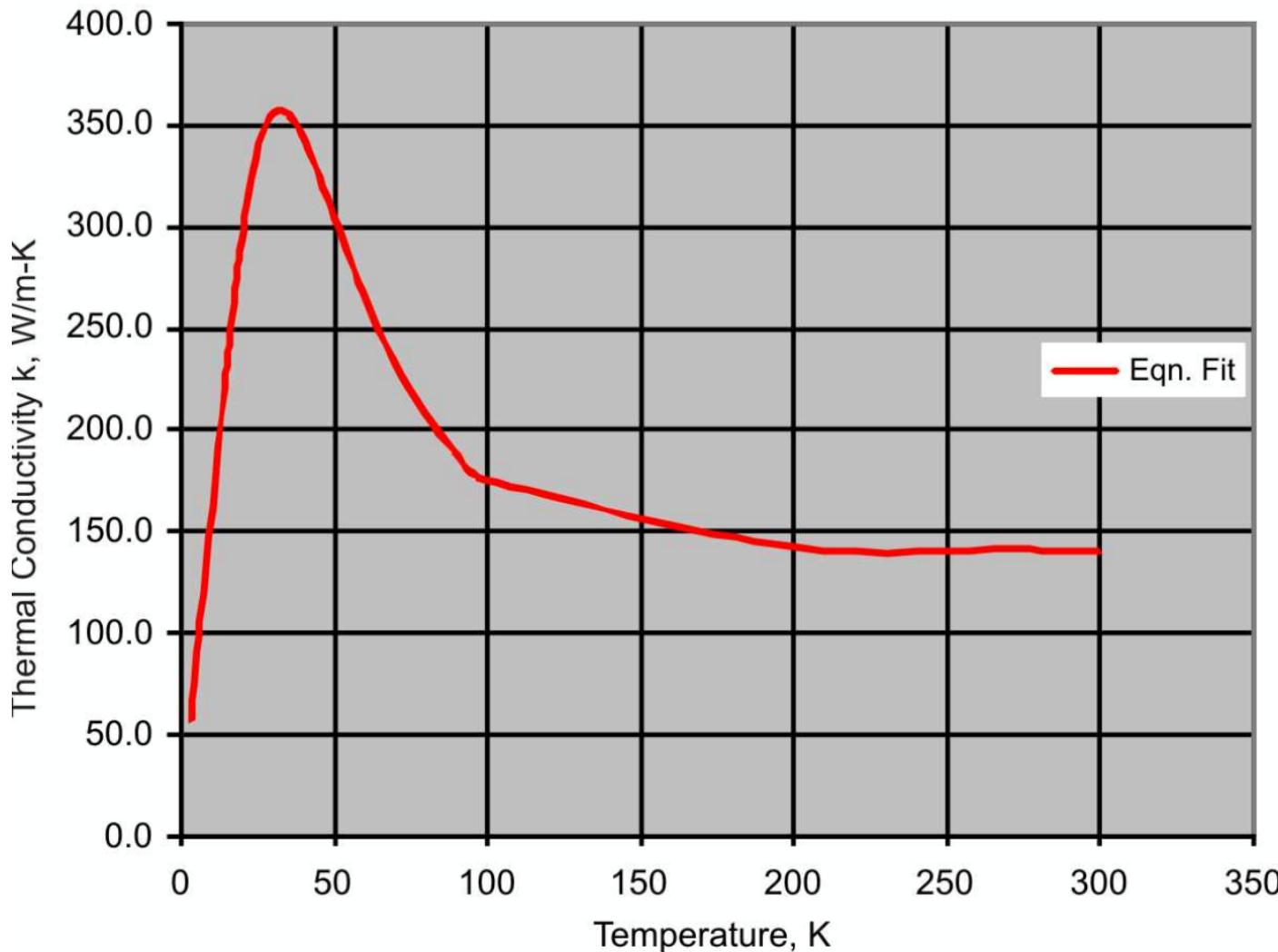


Macor®

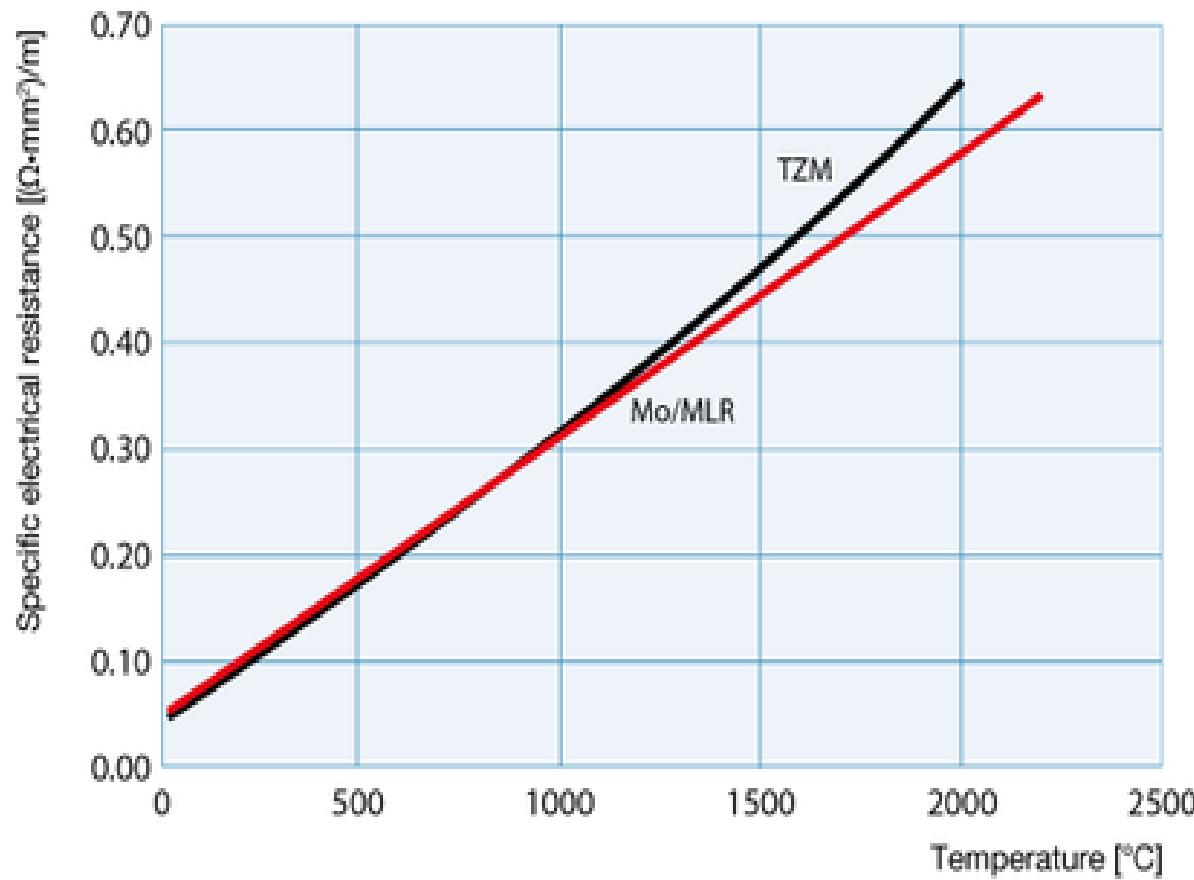


Molybdenum

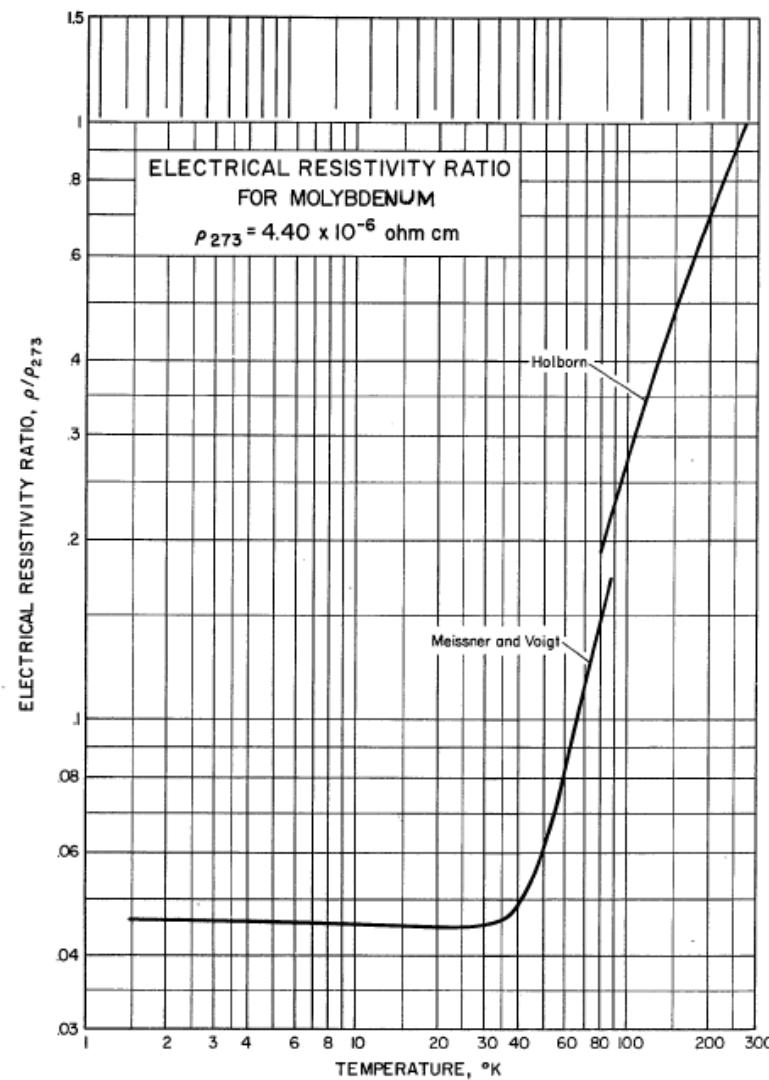
Molybdenum Thermal Conductivity



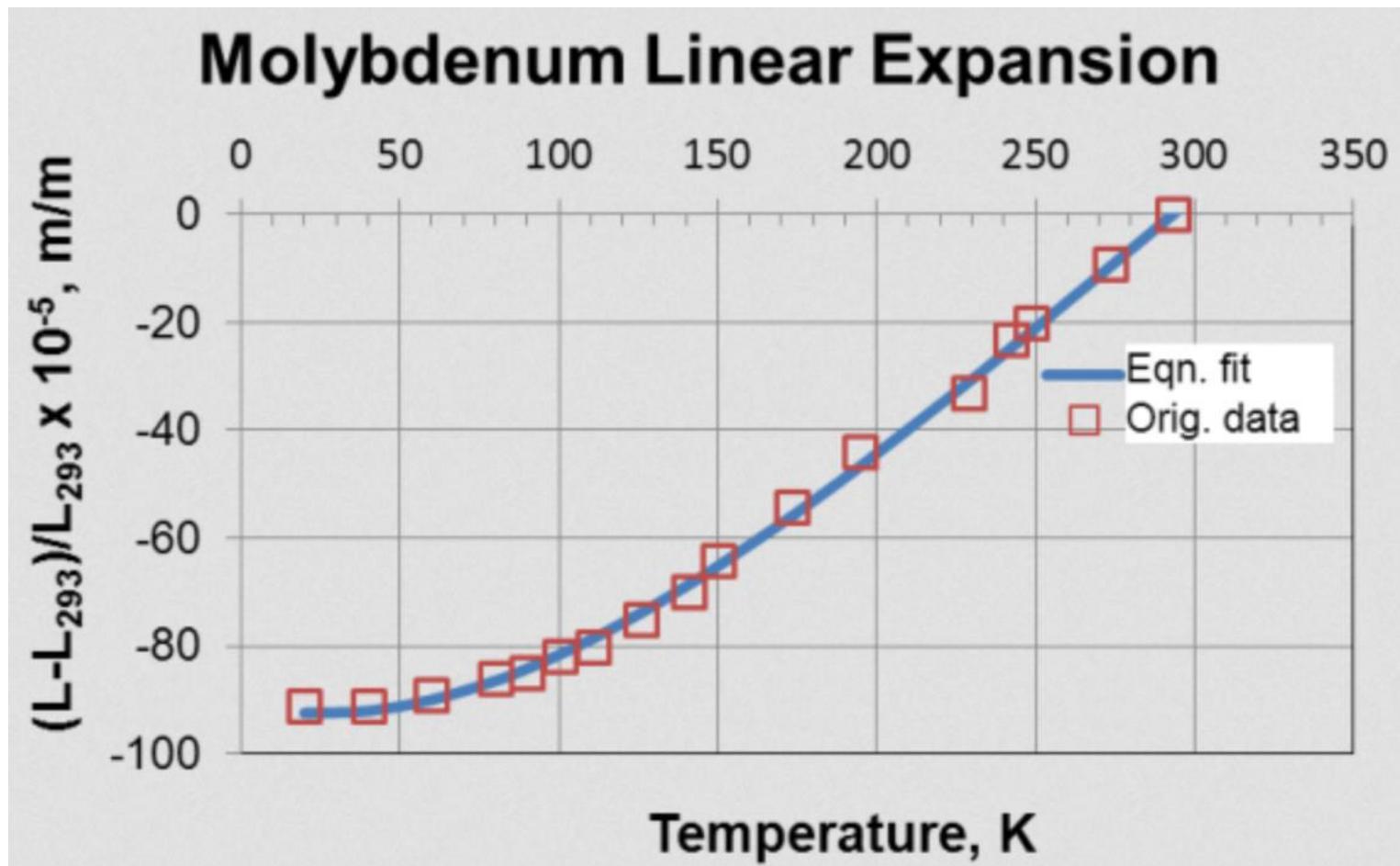
Molybdenum



Molybdenum



Molybdenum



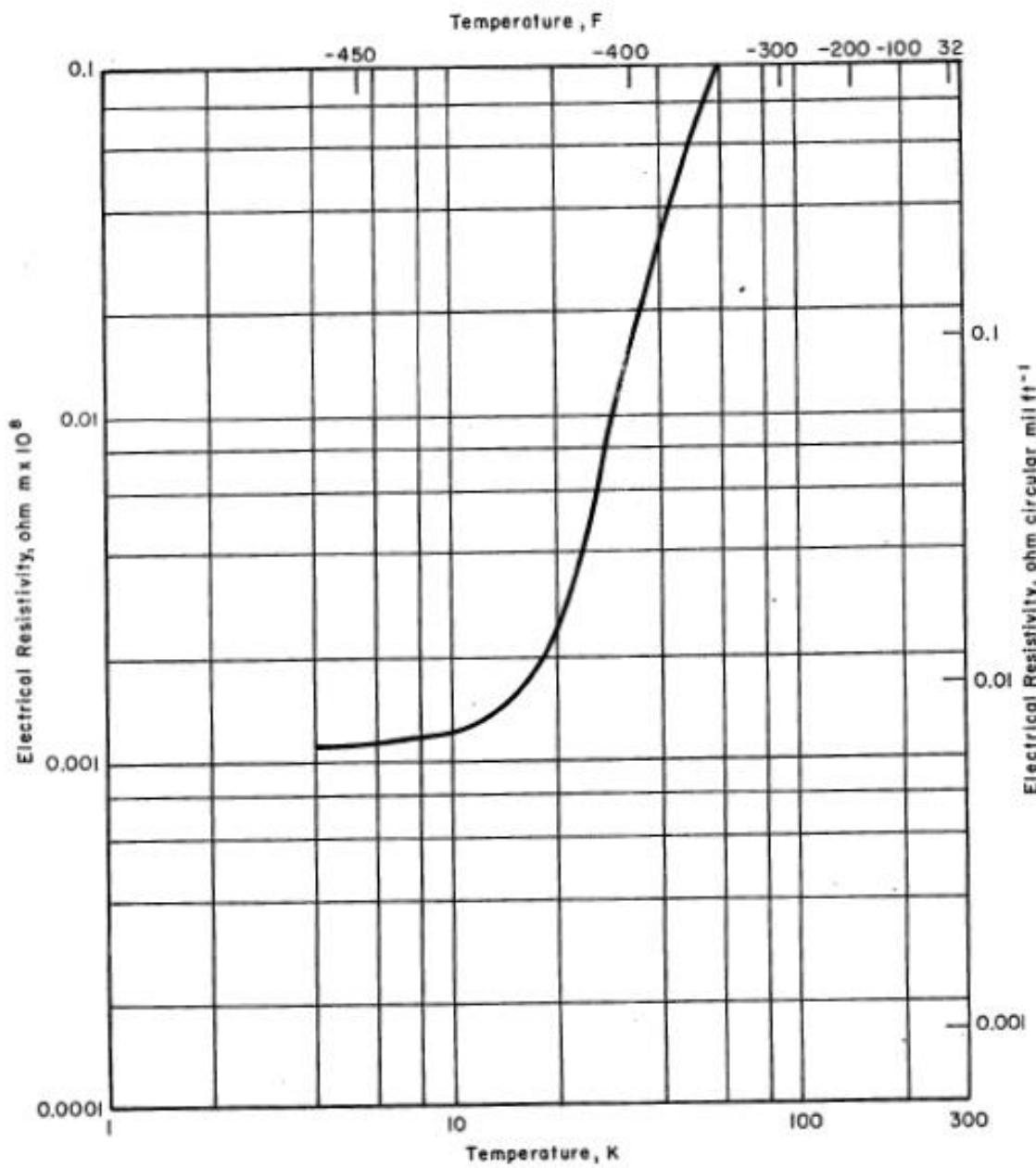
Copper

TABLE 2. RECOMMENDED VALUES FOR THE ELECTRICAL RESISTIVITY
OF COPPER

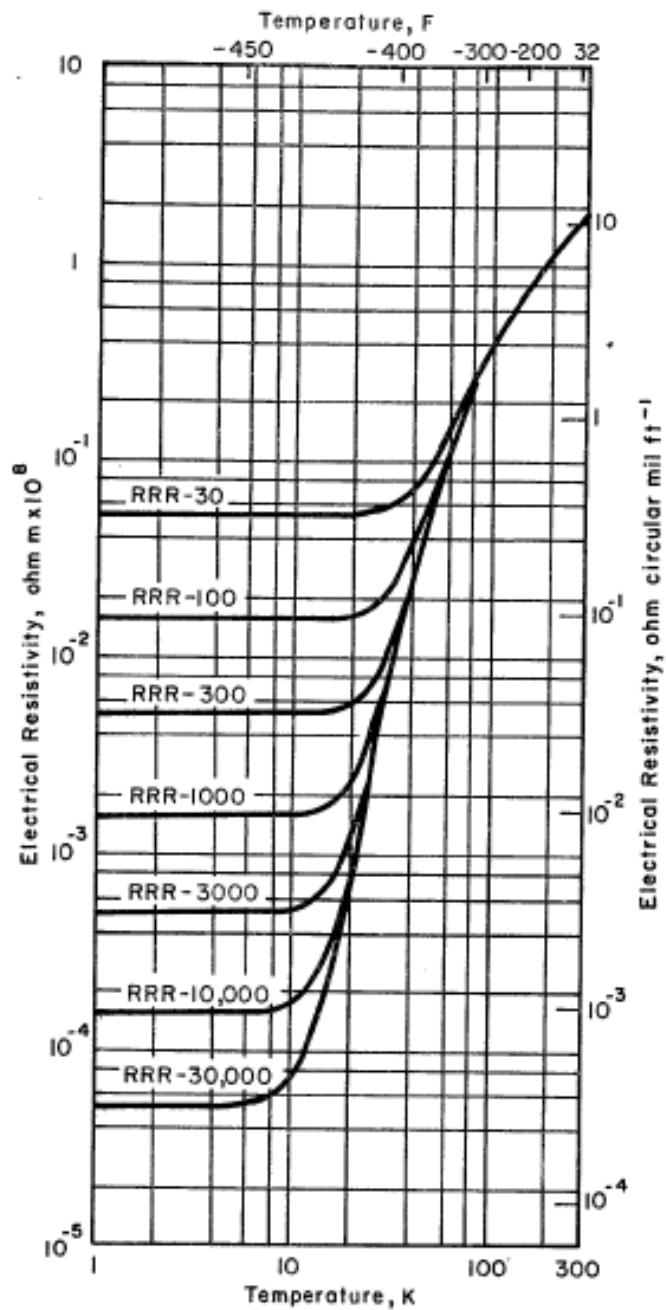
[Temperature, T, K; Total Resistivity, ρ , $10^{-8} \Omega \text{ m}$; Intrinsic Resistivity, ρ_i , $10^{-8} \Omega \text{ m}$]

Solid

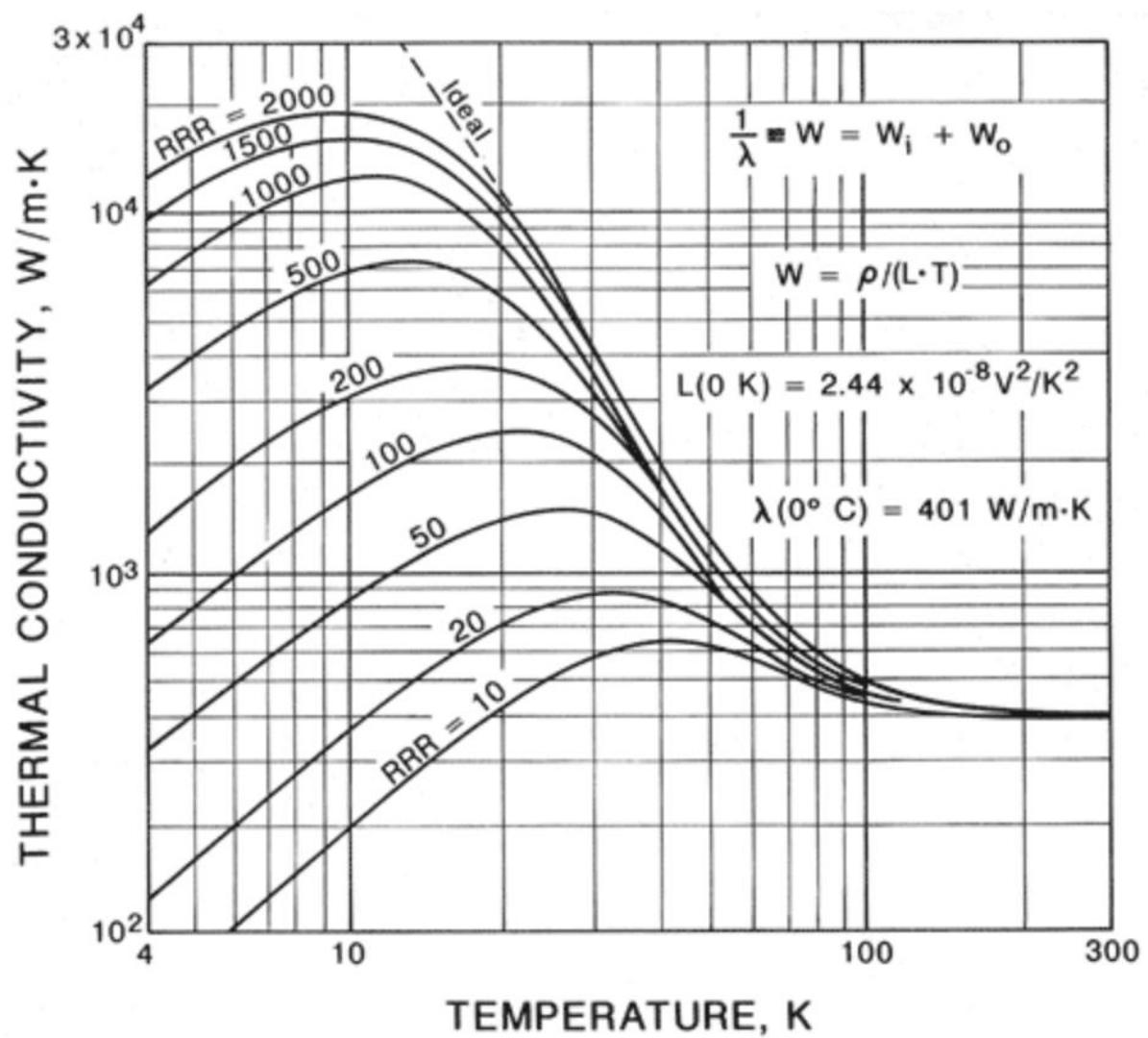
T	$\rho_i^{\text{a},\text{b}}$	$\rho^{\text{a},\text{c}}$	T	$\rho_i^{\text{a},\text{b}}$	$\rho^{\text{a},\text{c}}$
1		0.00200	175	0.872	0.874
4		0.00200	200	1.044	1.046
7		0.00200	225	1.215	1.217
10		0.00202	250	1.385	1.387
15		0.00218	273.15	1.541	1.543
20	0.000798*	0.00280	293	1.676	1.678
25	0.00249*	0.00449	300	1.723	1.725
30	0.00628	0.00828	350	2.061	2.063
35	0.0127	0.0147	400	2.400	2.402
40	0.0219	0.0239	500	3.088	3.090
45	0.0338	0.0358	600	3.790	3.792
50	0.0498	0.0518	700	4.512	4.514
55	0.0707	0.0727	800	5.260	5.262
60	0.0951	0.0971	900	6.039	6.041
70	0.152	0.154	1000	6.856	6.858
80	0.213	0.215	1100	7.715	7.717
90	0.279	0.281	1200	8.624	8.626
100	0.346	0.348	1300	9.590	9.592
125	0.520	0.522	1357.6	10.169	10.171
150	0.697	0.699			



ELECTRICAL RESISTIVITY VERSUS TEMPERATURE FOR COPPER



ELECTRICAL RESISTIVITY VERSUS TEMPERATURE FOR COPPER



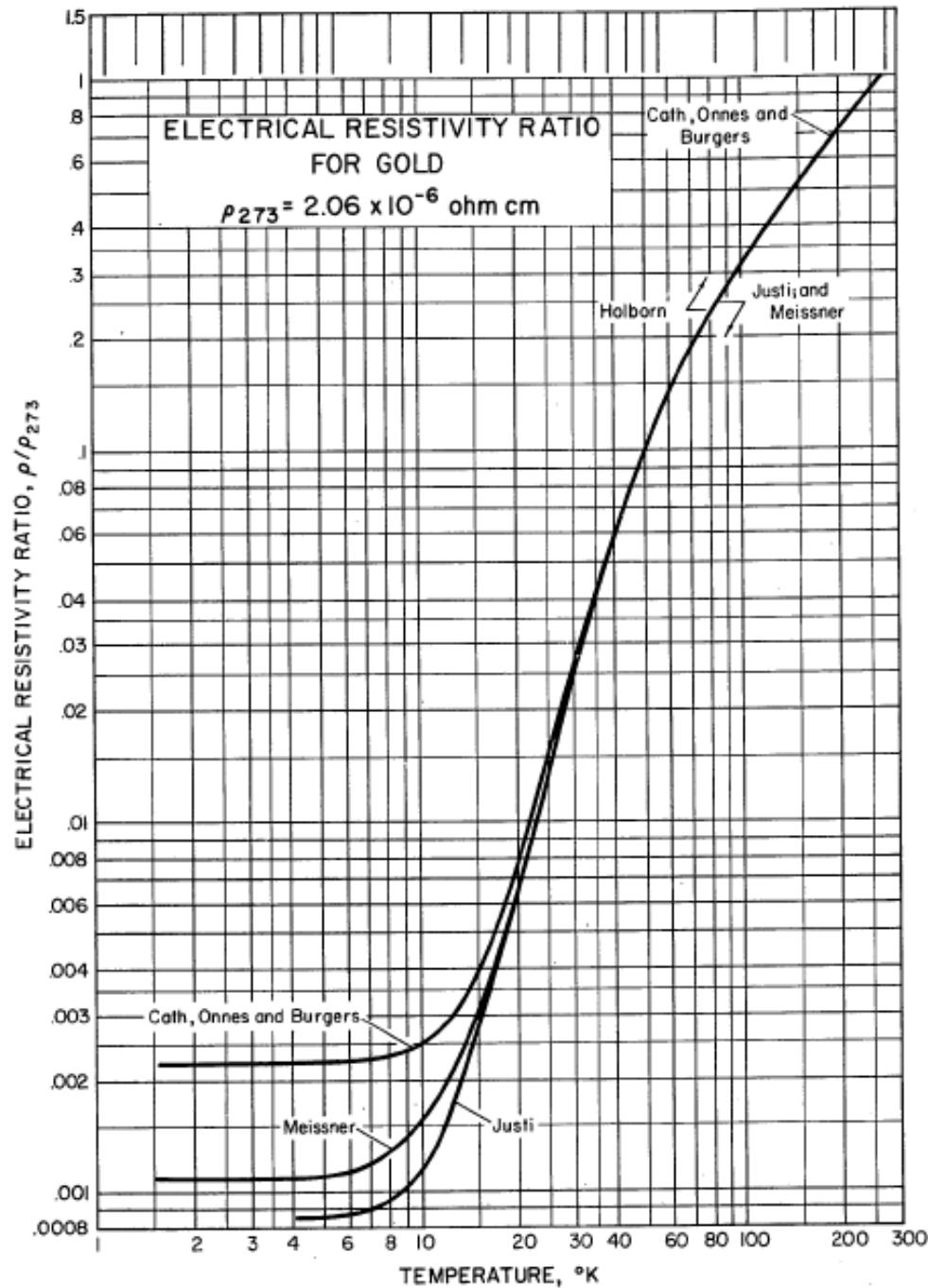
Gold

TABLE 5. RECOMMENDED VALUES FOR THE ELECTRICAL RESISTIVITY
OF GOLD

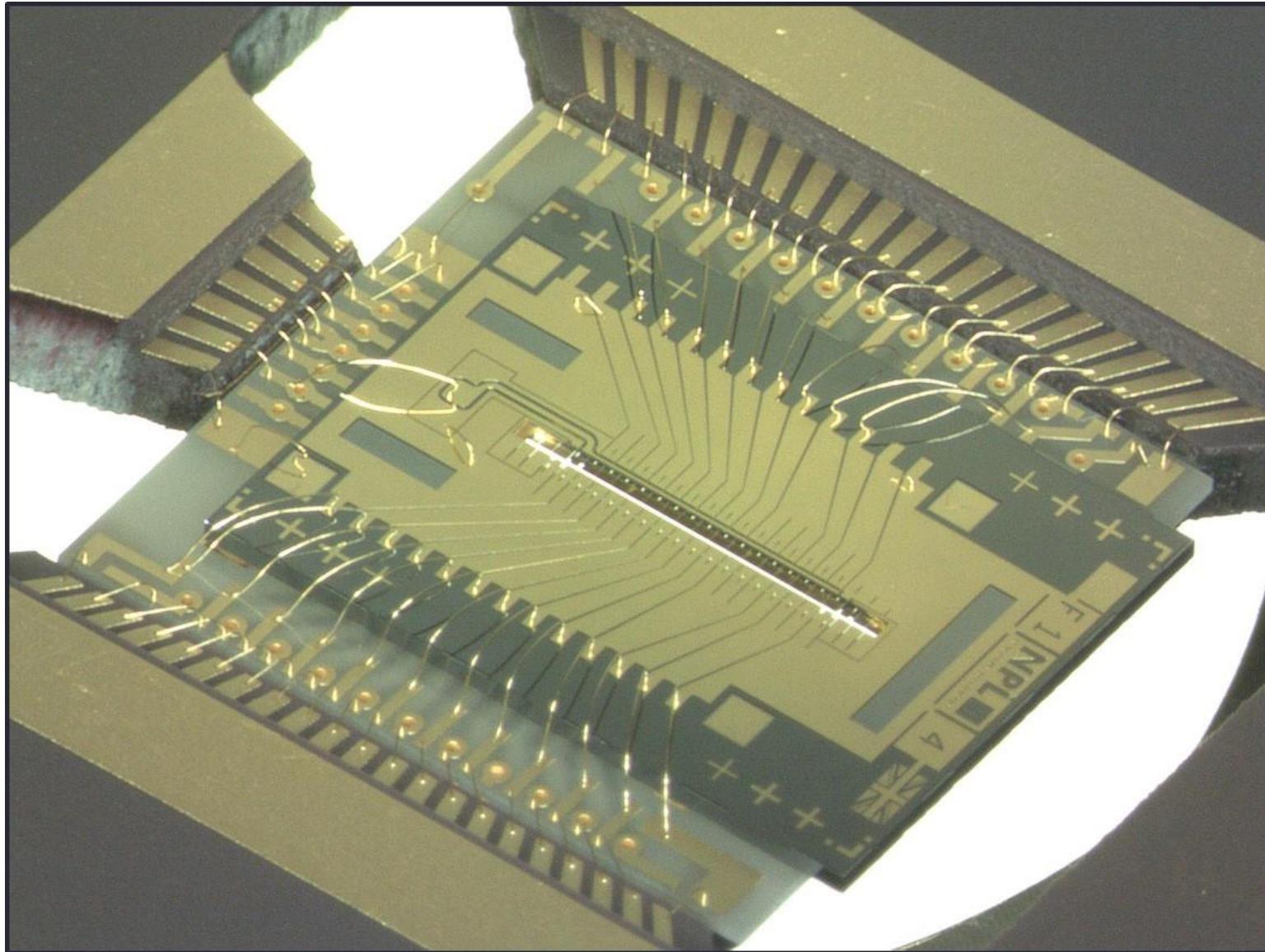
[Temperature, T, K; Total Resistivity, ρ , $10^{-8} \Omega \text{ m}$; Intrinsic Resistivity, ρ_i , $10^{-8} \Omega \text{ m}$]

Solid

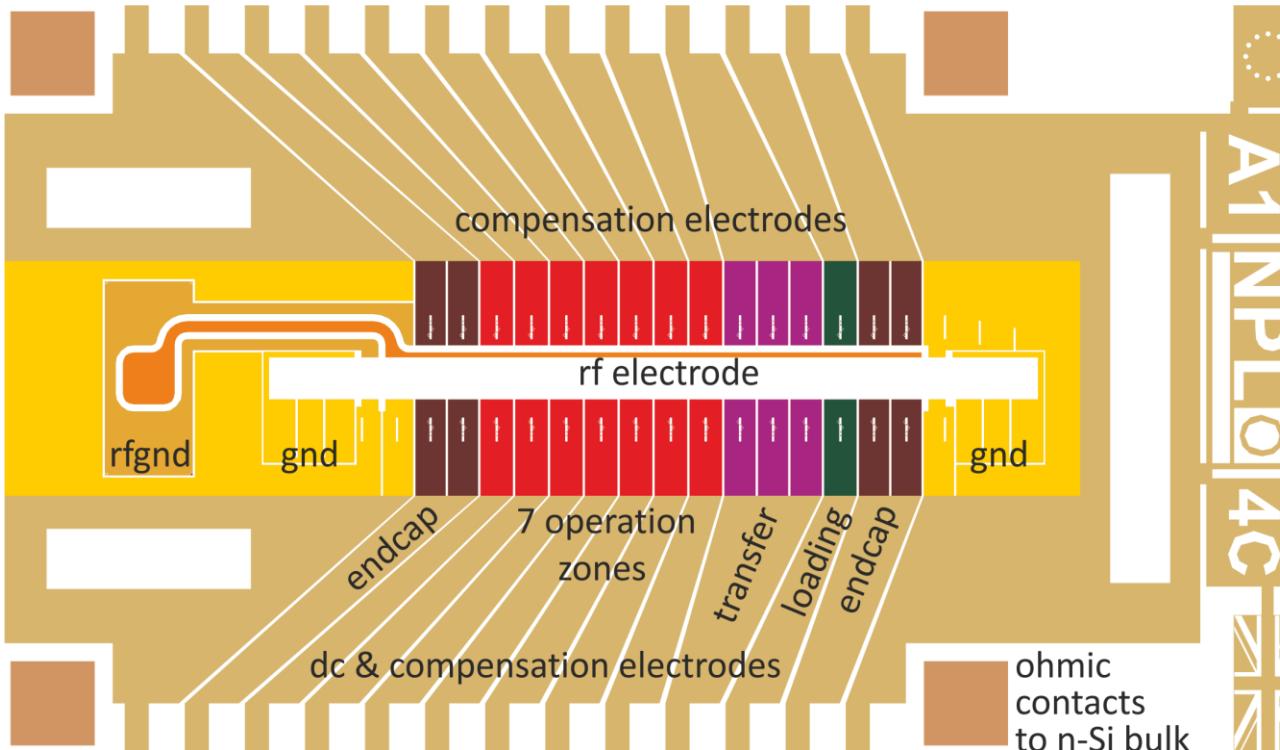
T	$\rho_i^{\text{a},\text{b}}$	$\rho^{\text{a},\text{c}}$	T	$\rho_i^{\text{a},\text{b}}$	$\rho^{\text{a},\text{c}}$
1		0.0220	175	1.240	1.262
4		0.0220	200	1.440	1.462
7		0.0221	225	1.640	1.662
10		0.0226	250	1.842	1.864
15	0.00376*	0.0258	273.15	2.029	2.051
20	0.0126*	0.0346*	293	2.192	2.214
25	0.0282*	0.0502*	300	2.249	2.271
30	0.0505*	0.0725*	350	2.663	2.685
35	0.0798*	0.1018*	400	3.085	3.107
40	0.119*	0.141*	500	3.952	3.974
45	0.159	0.181	600	4.853	4.875
50	0.199	0.221	700	5.794	5.816
55	0.248	0.270	800	6.786	6.808
60	0.286	0.308	900	7.840	7.862
70	0.373	0.395	1000	8.964	8.986
80	0.459	0.481	1100	10.169	10.191
90	0.544	0.566	1200	11.464	11.486
100	0.628	0.650	1300	12.832	12.854
125	0.835	0.857	1337.58	13.366	13.388
150	1.039	1.061			



NPL monolithic trap

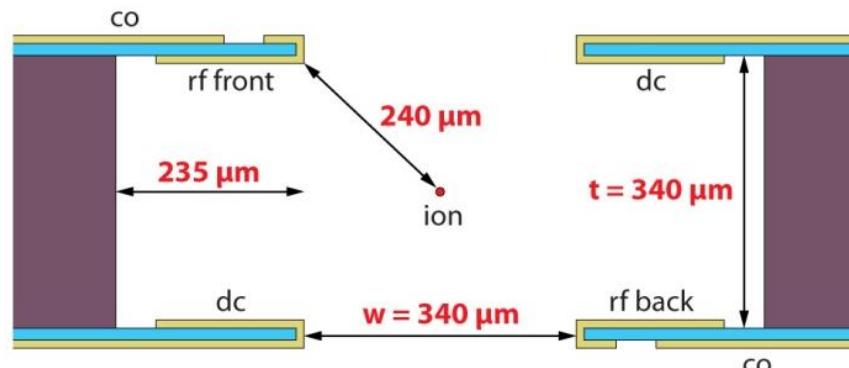


NPL monolithic trap



Electrode layout

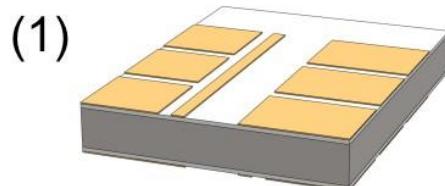
Cross-section



gold silicon silica

Microfabrication

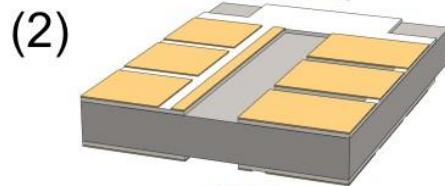
metallisation



NPL prototype

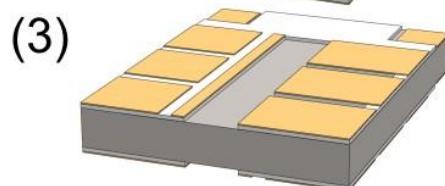
wafer

SiO_2 etch



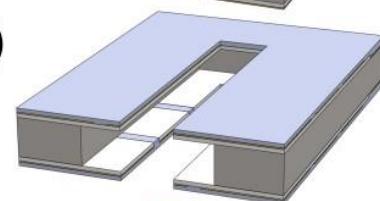
wafer

ohmic
metallisation



wafer

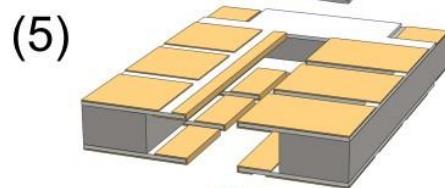
Si etch



die

wafer

internal
metallisation

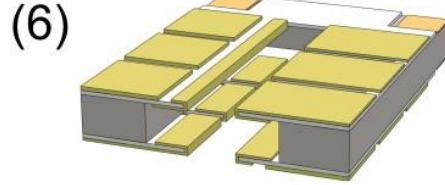


die

with

wafer

electroplate



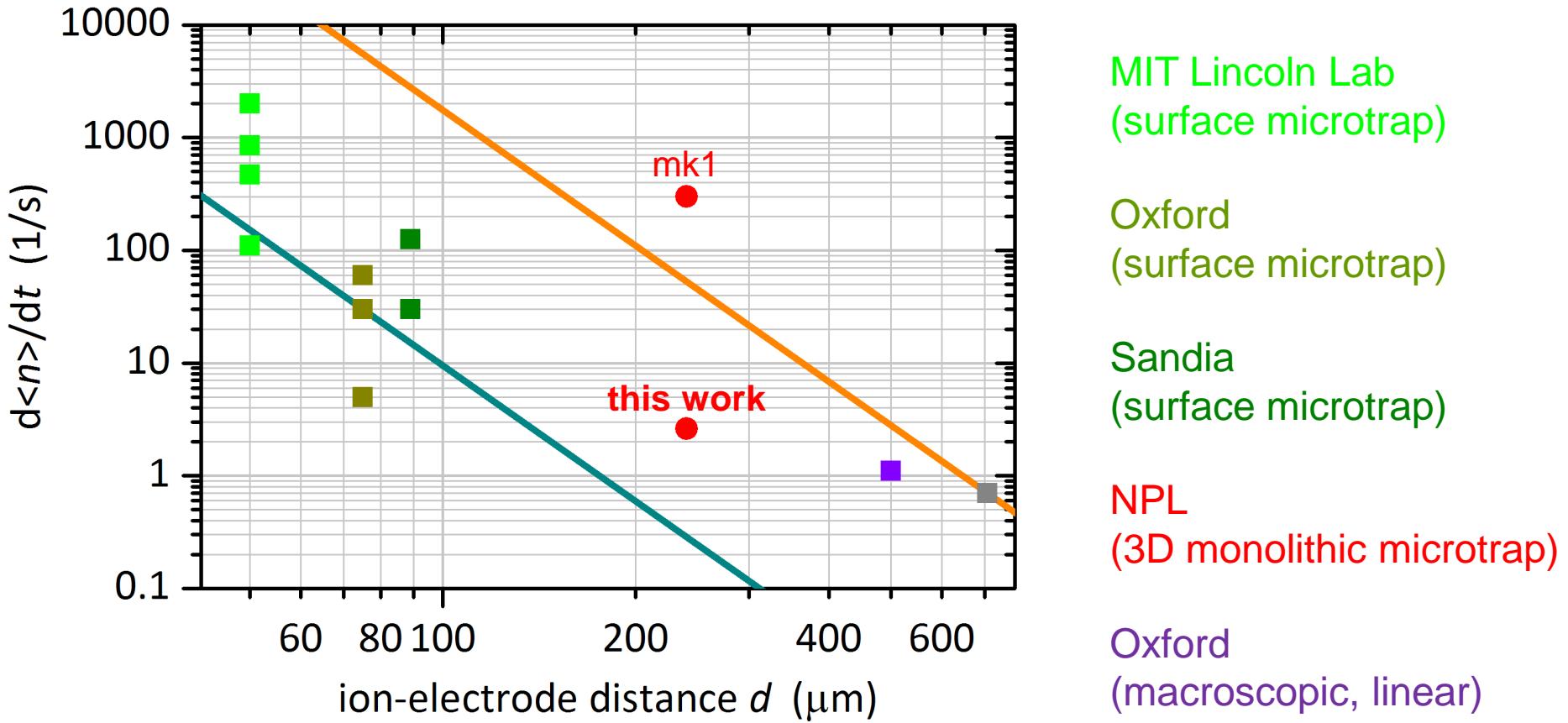
die

die



Innovate UK

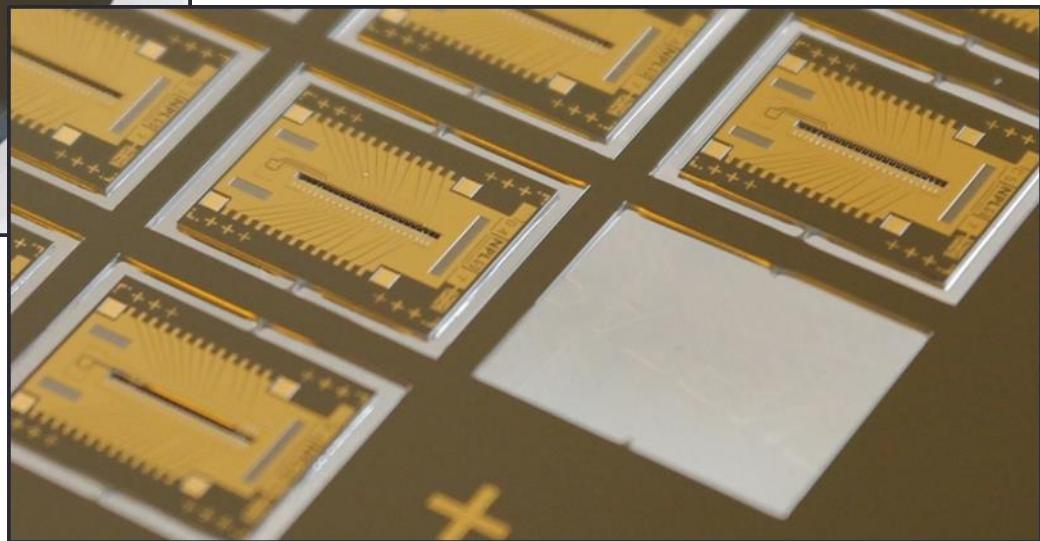
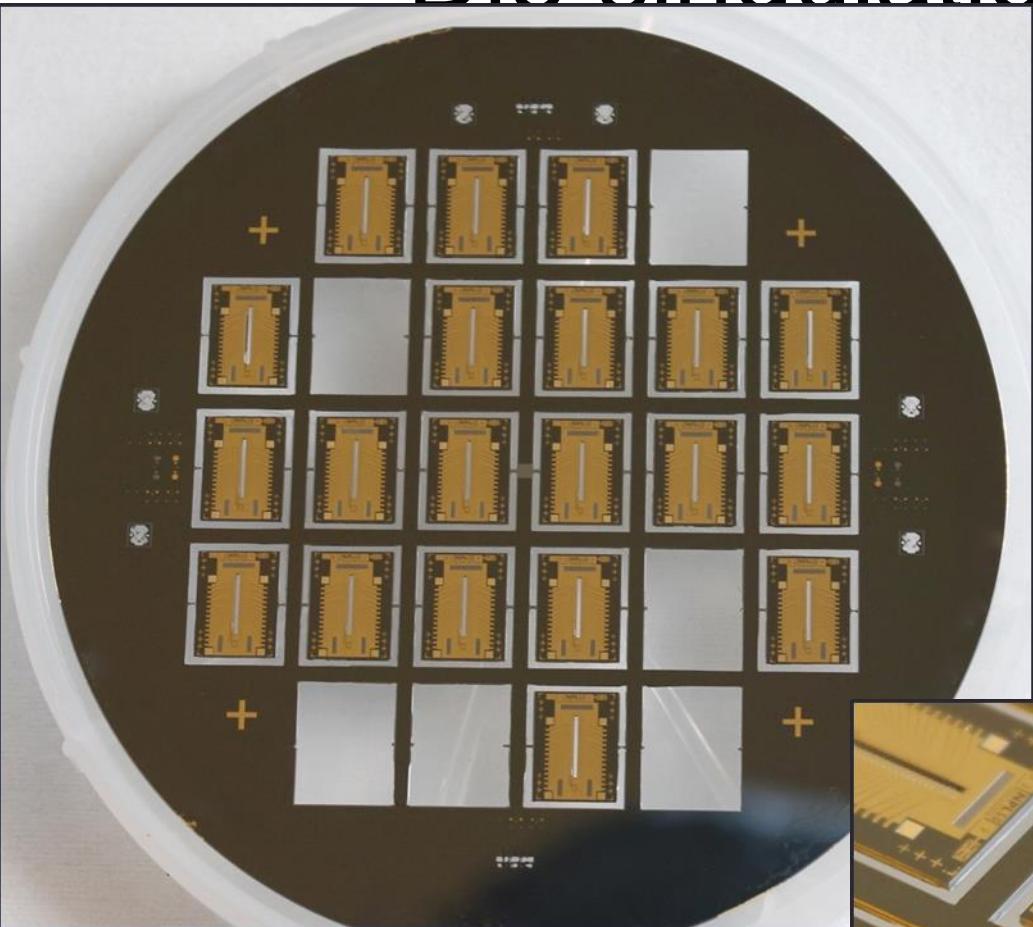
Recent heating rates (trap @ T_{ambient})



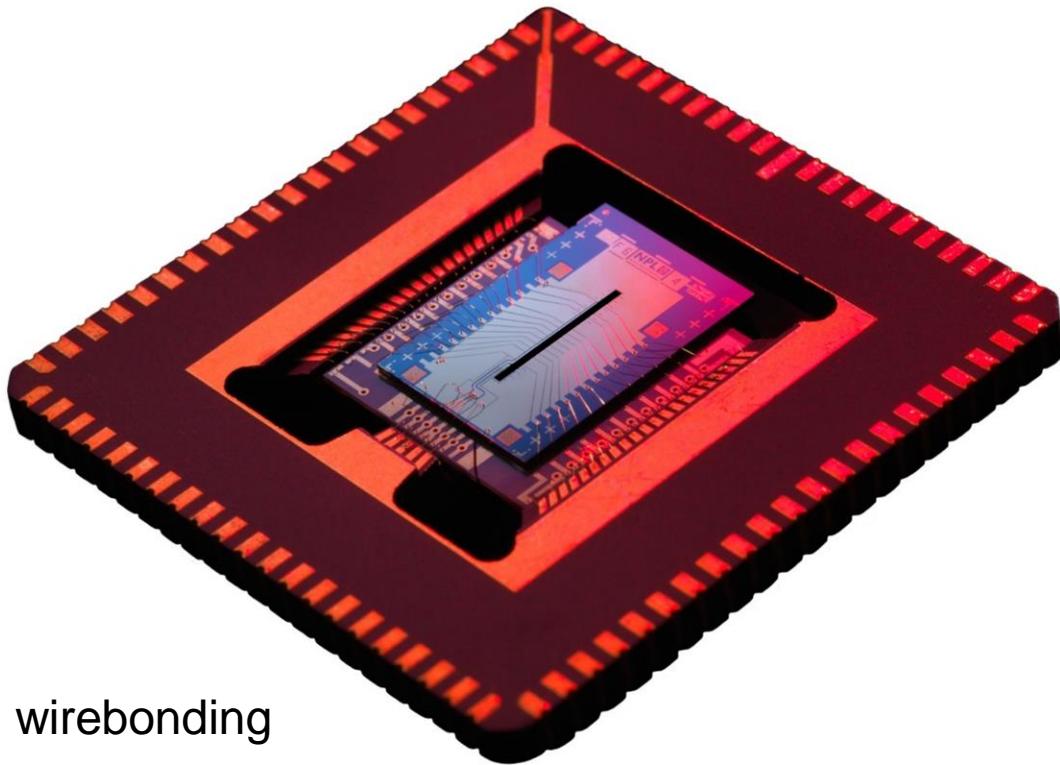
$$\dot{n} = \frac{e^2 S_E(\omega_z)}{4m\hbar\omega_z} \quad S_E(\omega) \propto \frac{1}{d^4}$$

M D Hughes, *et al*, Contemp. Phys. 52, 505 (2011)
I. A. Boldin, *et al*, arXiv:1708.03147v1 (2017)

Die simulation



Automated electronic packaging



with



Innovate UK

Molybdenum trap



$$\alpha = 0.96$$

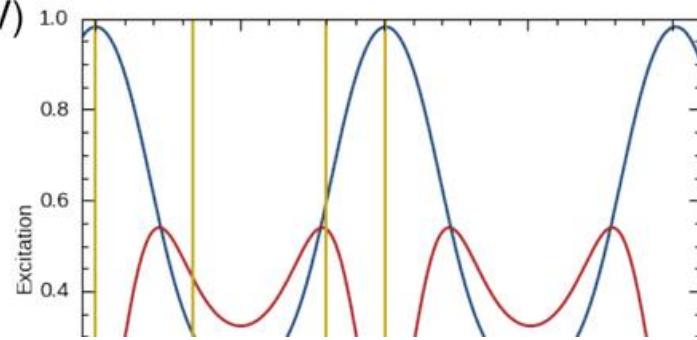
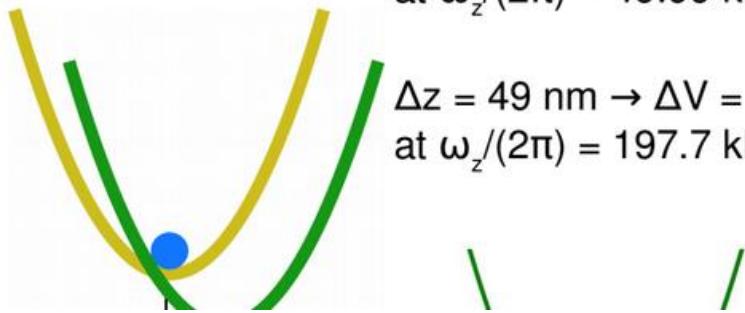
$$\bar{n}_{\text{th}} = 0.06$$

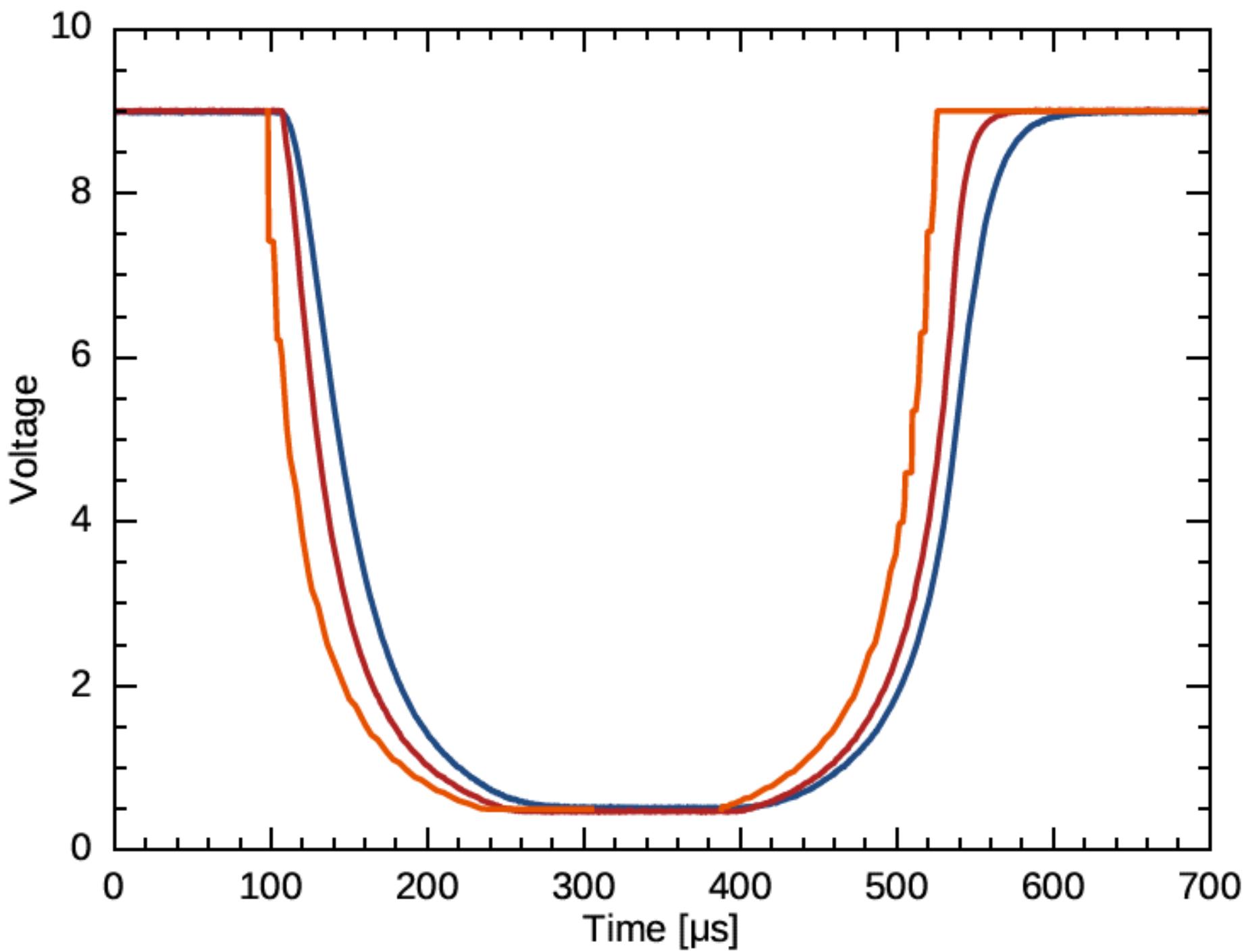
$$\Delta z = 96 \text{ nm} \rightarrow \Delta V = 0.2 \text{ mV}$$

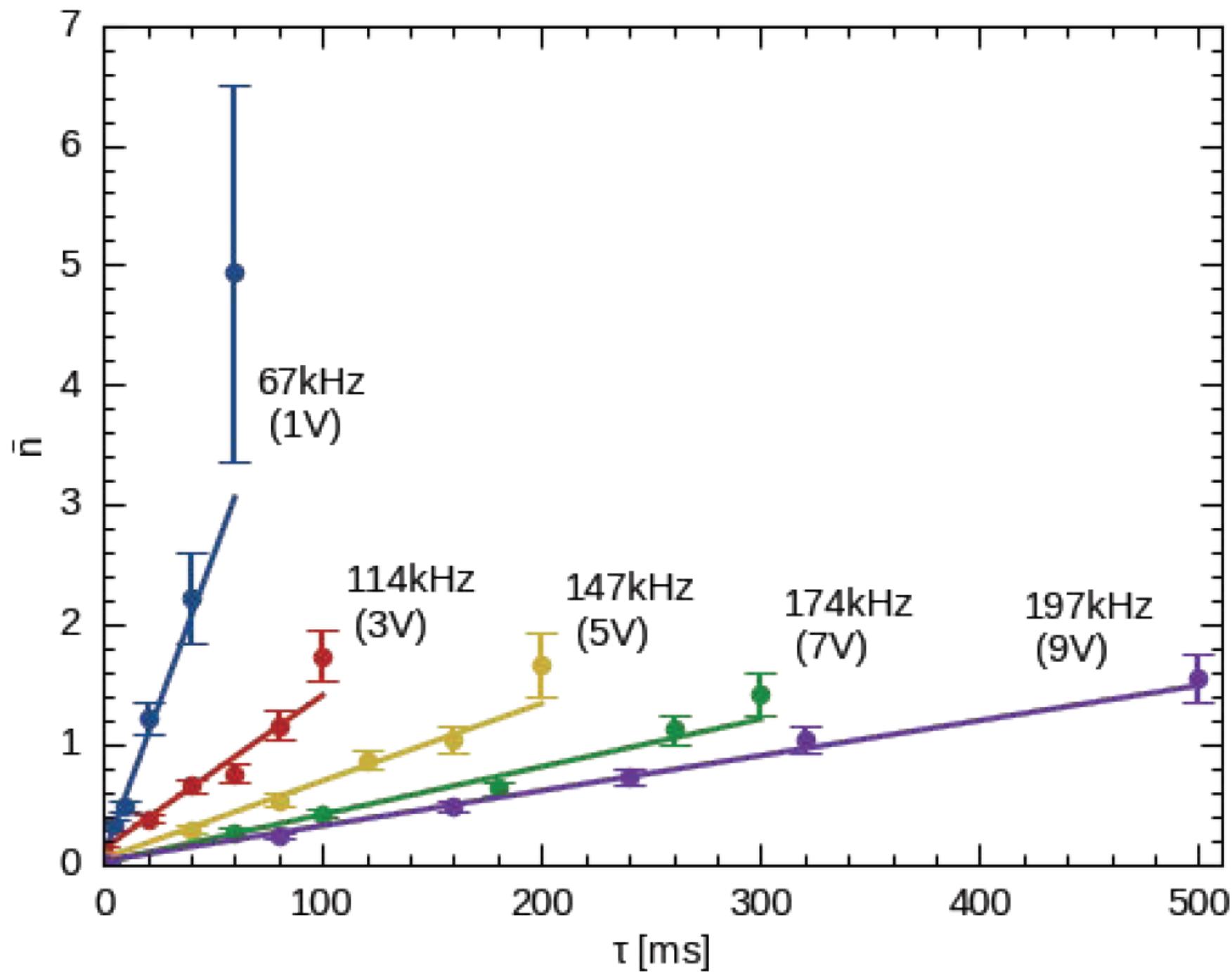
at $\omega_z/(2\pi) = 49.99 \text{ kHz}$ (0.5V)

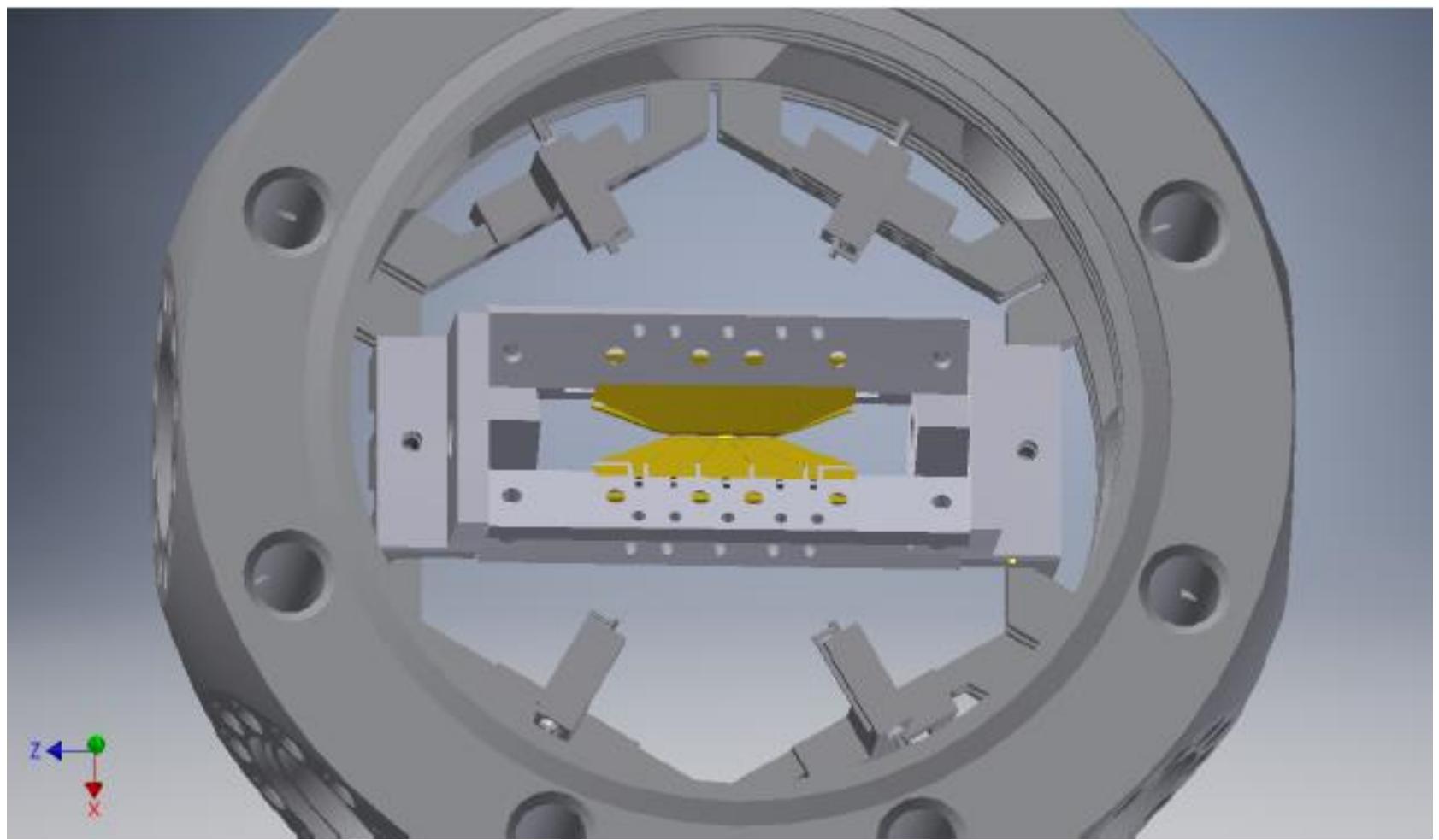
$$\Delta z = 49 \text{ nm} \rightarrow \Delta V = 1.8 \text{ mV}$$

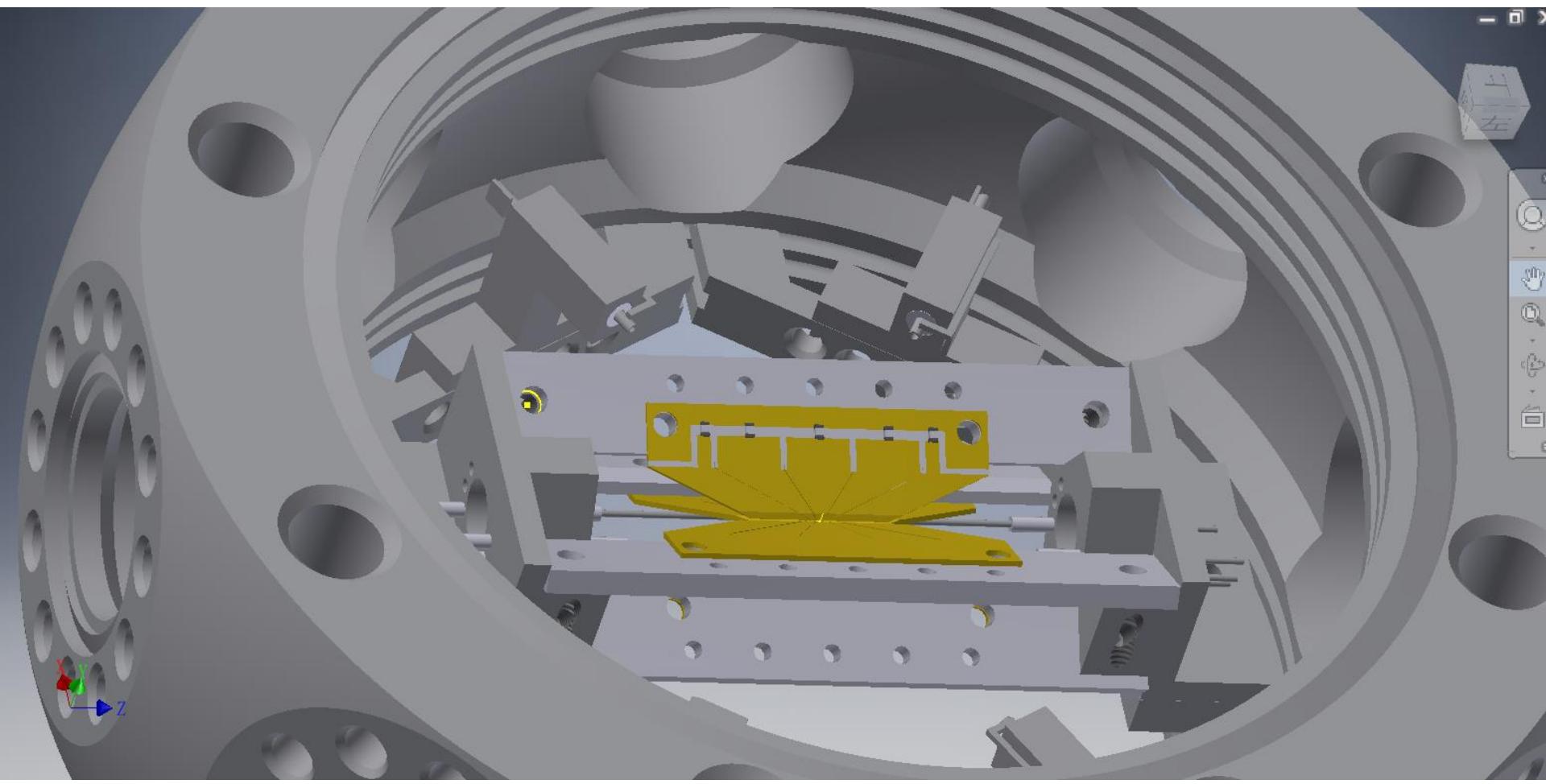
at $\omega_z/(2\pi) = 197.7 \text{ kHz}$ (9V)

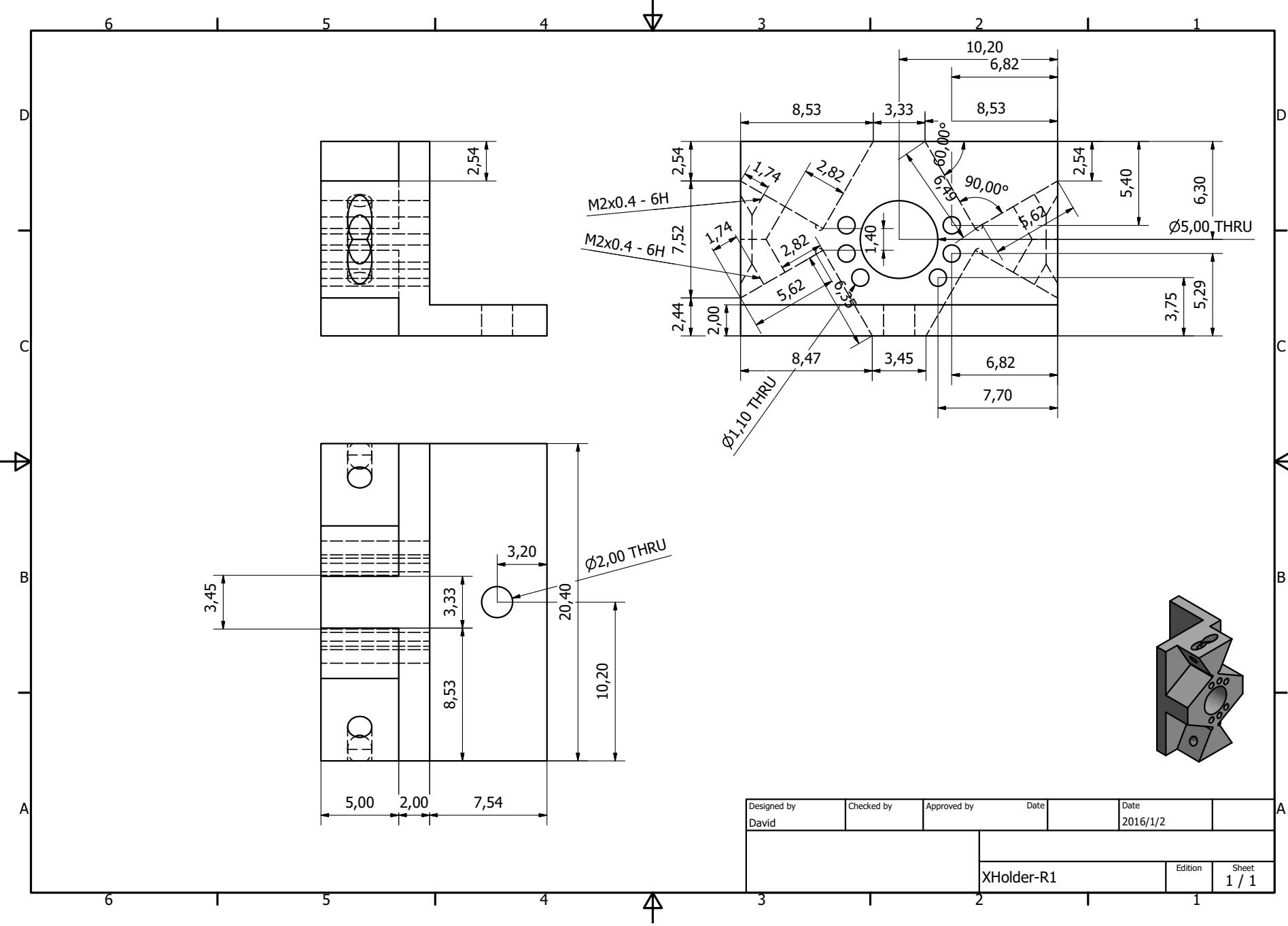


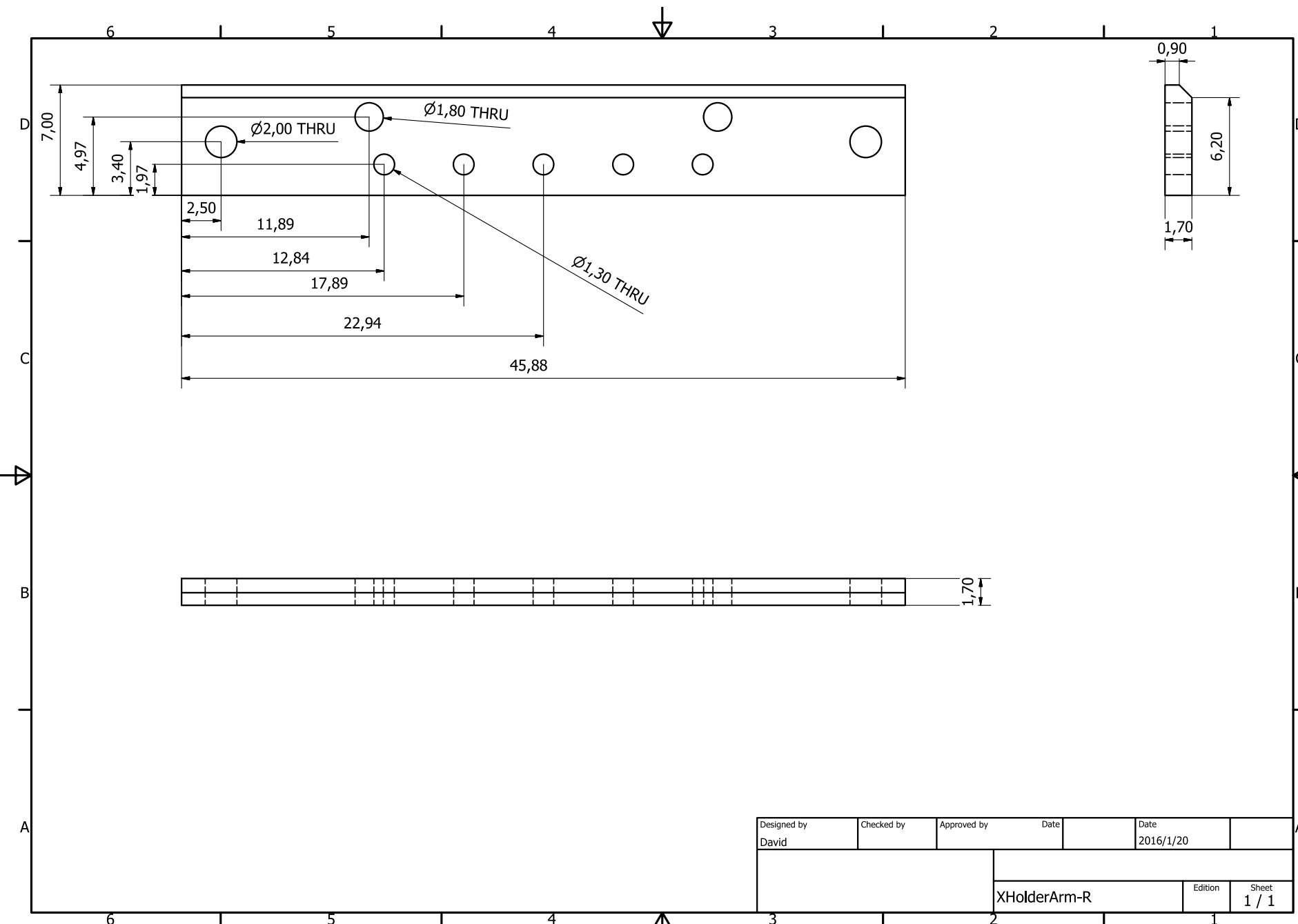






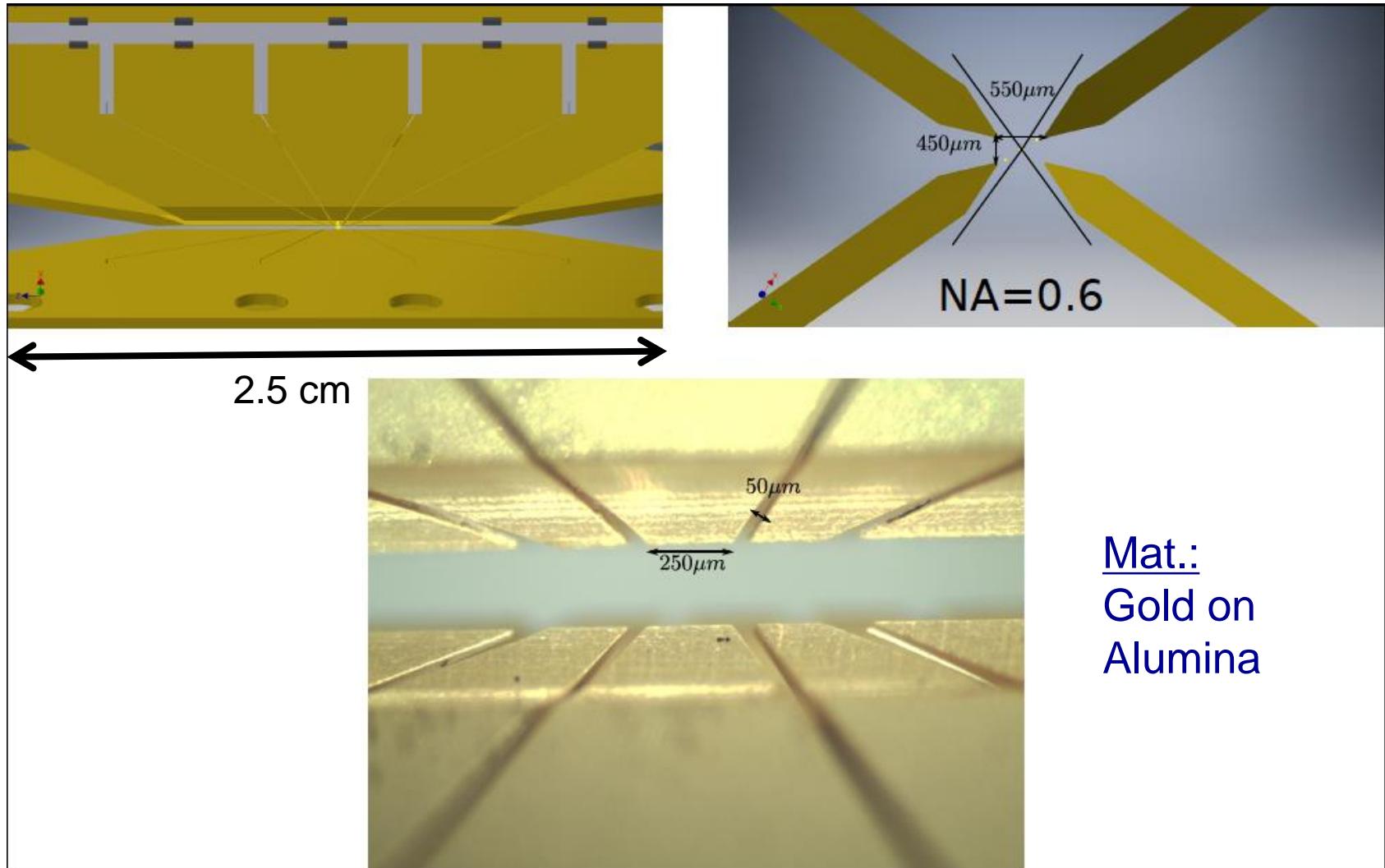






TEQ linear rf (ac) trap

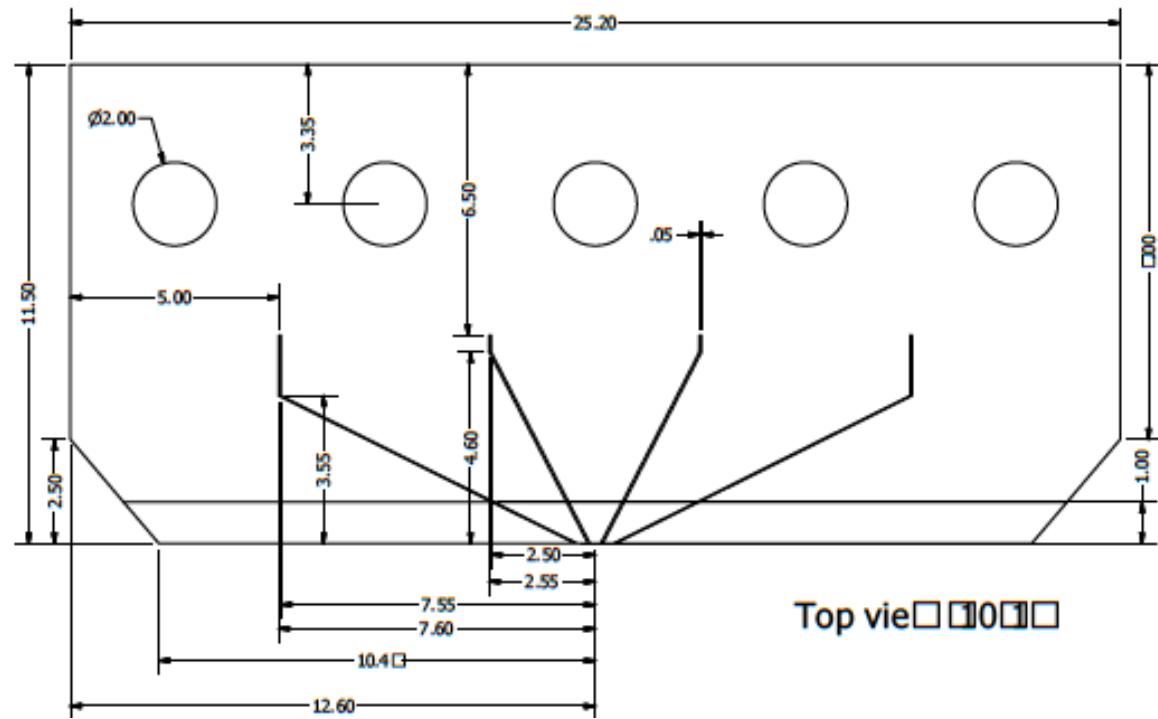
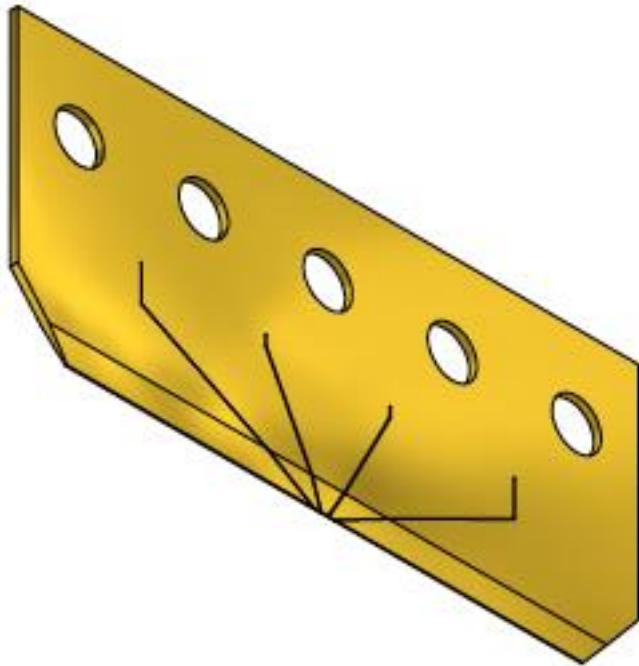
Design by Chris Monroe's Group



Design: Chris Monroe's group

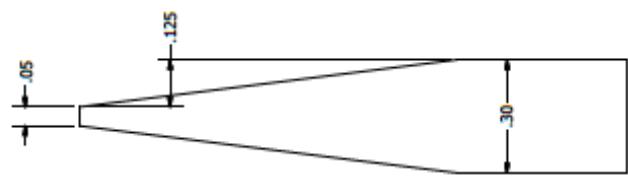
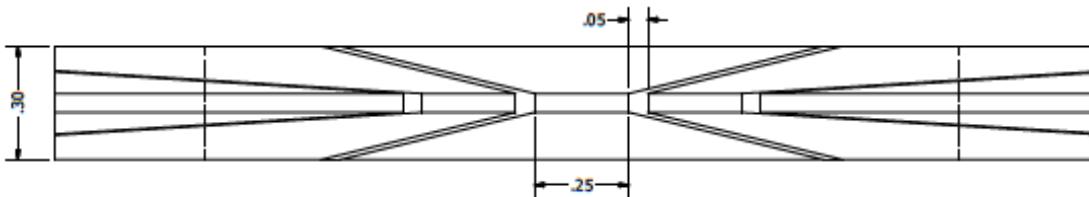
TEQ linear rf (ac) trap

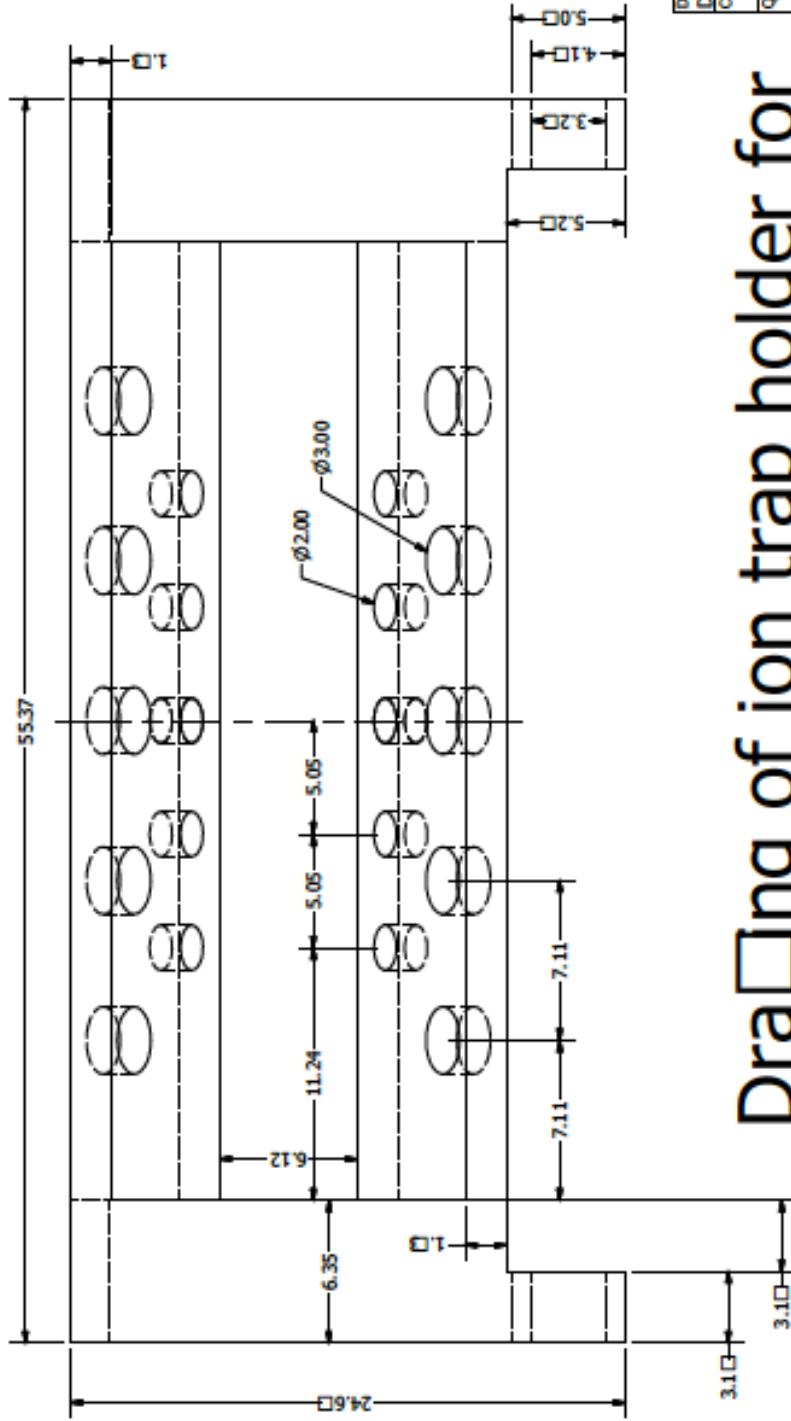
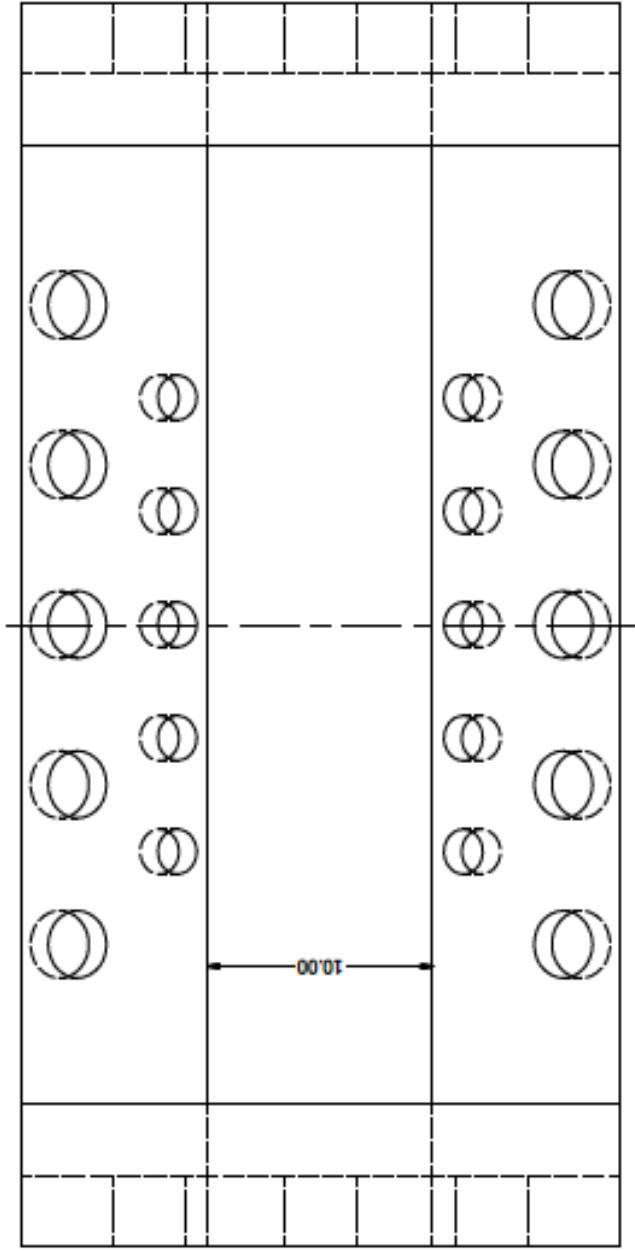
Design by Chris Monroe's Group



Front vie□□0□□

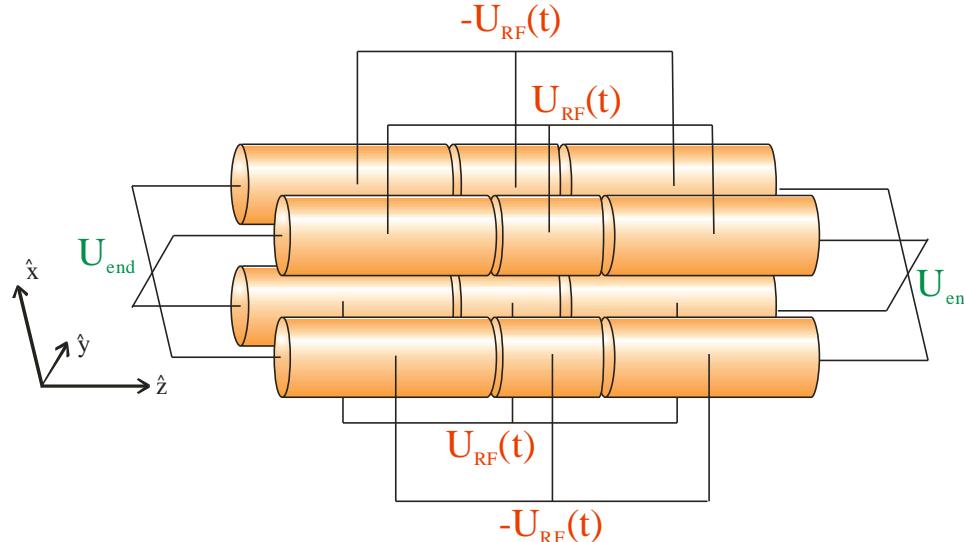
Side vie□□0□□





Dra□ng of ion trap holder for
0.3 □ thick□blades

The linear Paul trap



Sinusoidal RF potential: $U_{RF}(t)=U_{RF}\sin(\Omega t)$

Effective oscillation freq.'s:

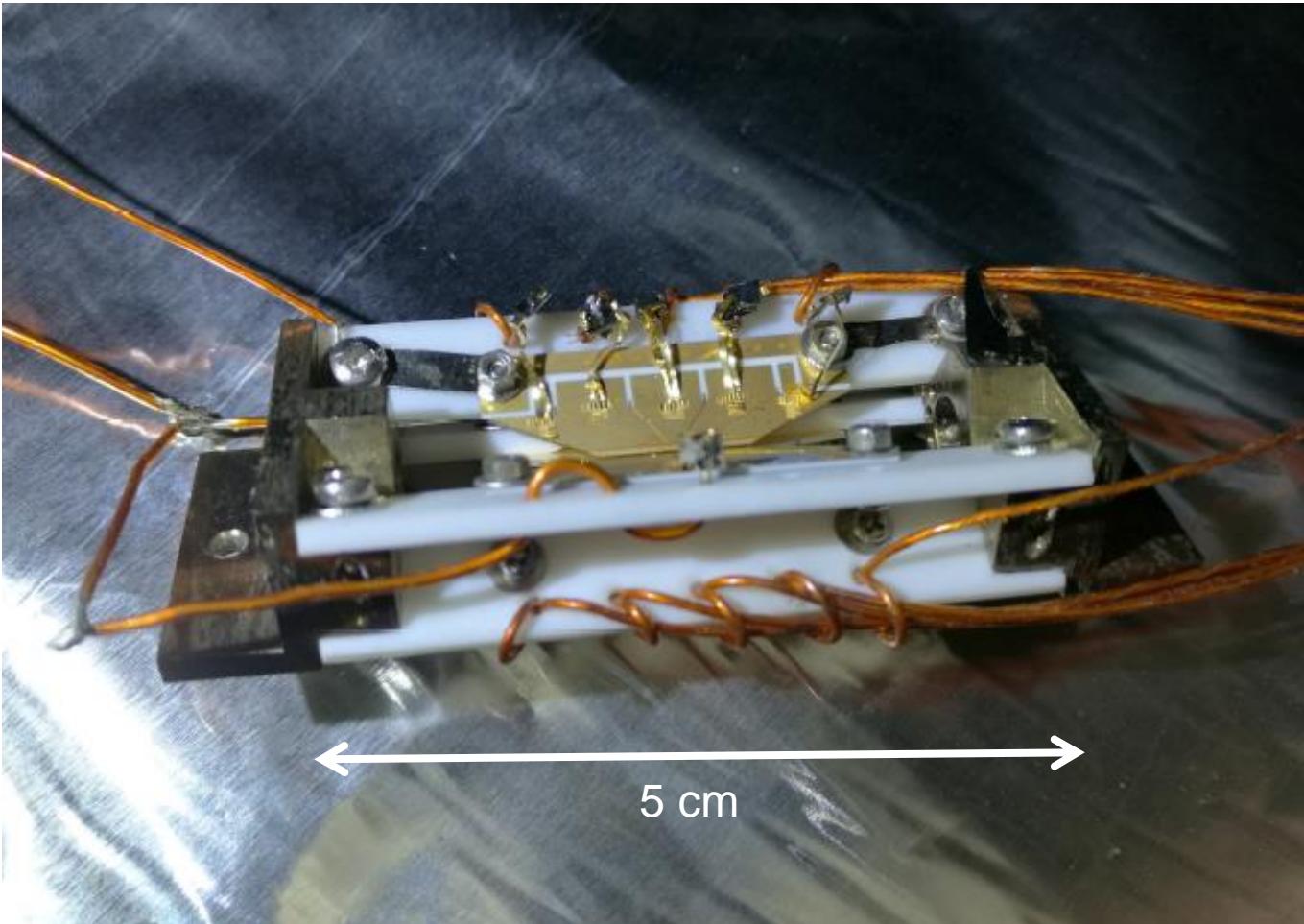
$$\omega_r = 1/2 \beta \Omega, \quad \beta = (1/2 q^2 + a)^{1/2}$$

$$\omega_z = (-1/2 a)^{1/2} \Omega$$

$$q = \frac{4Q U_{RF}}{m \Omega^2 r_0^2} \quad a = -\frac{\alpha Q U_{end}}{m \Omega^2 r_0^2}$$

TEQ linear rf (ac) trap

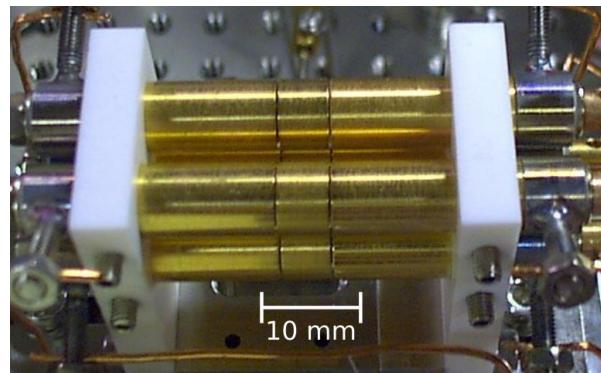
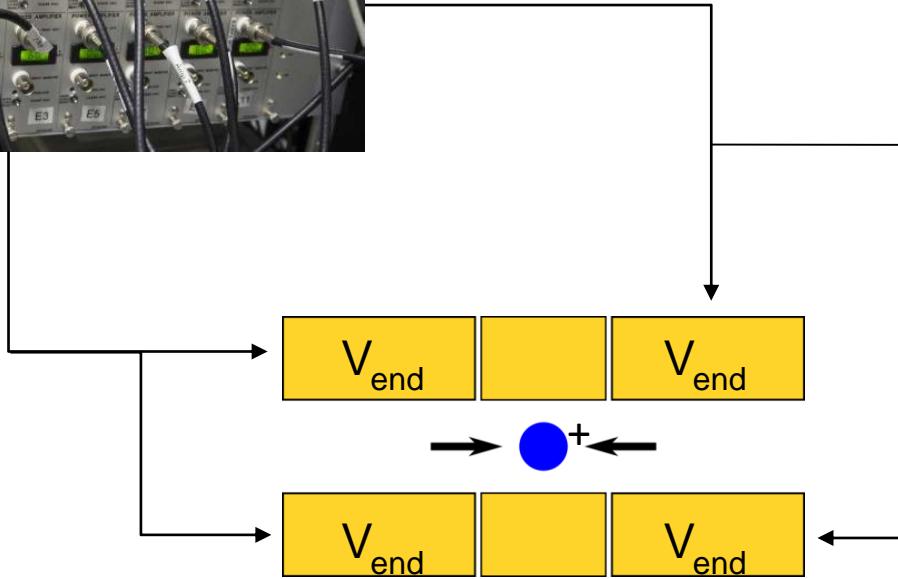
Design by Chris Monroe's Group



Past DC supply noise-tests

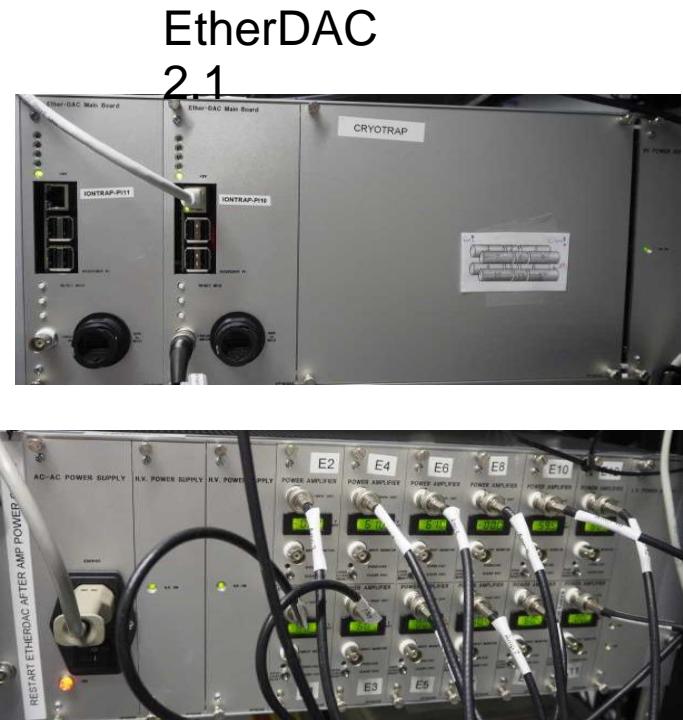
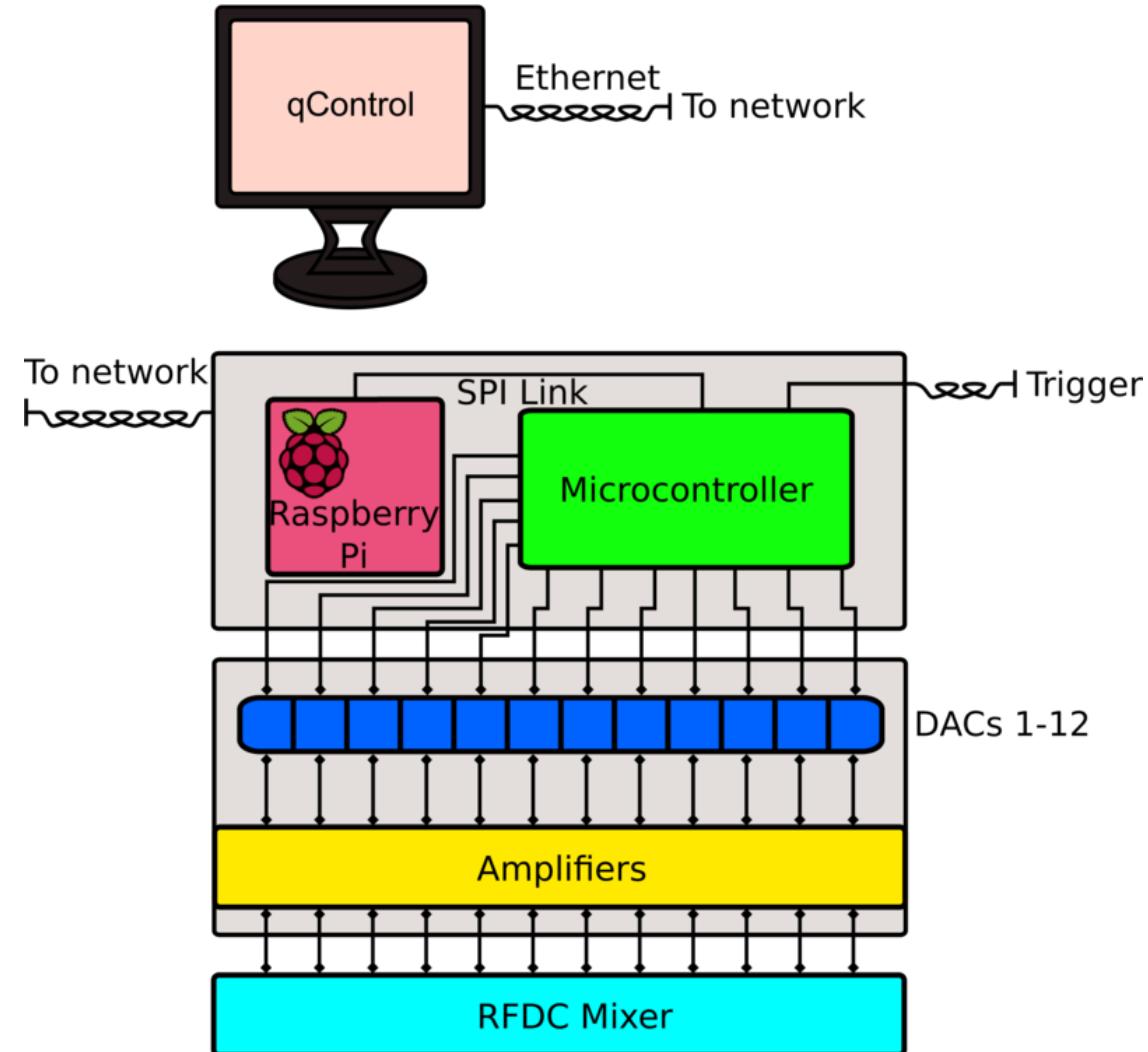


DC Supply

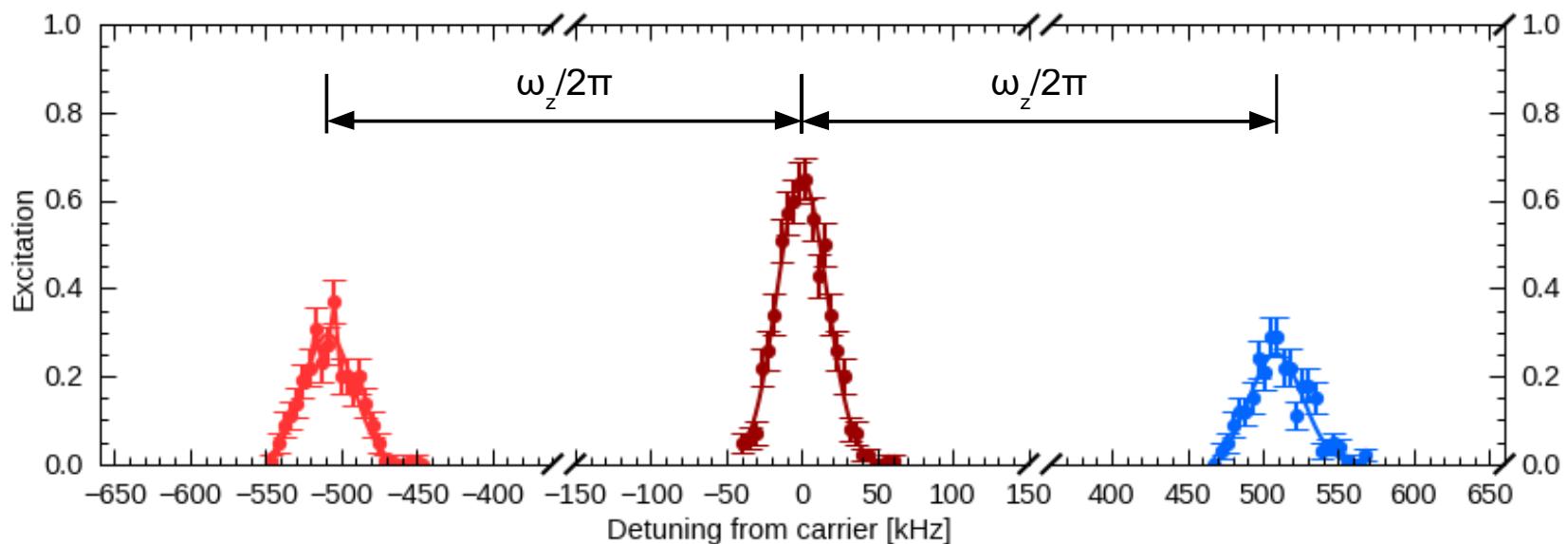
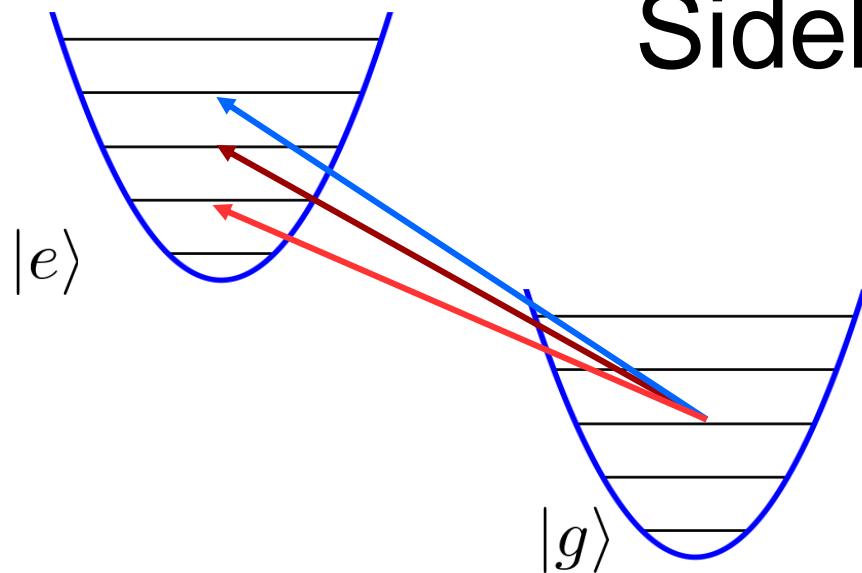


$\rightarrow z$

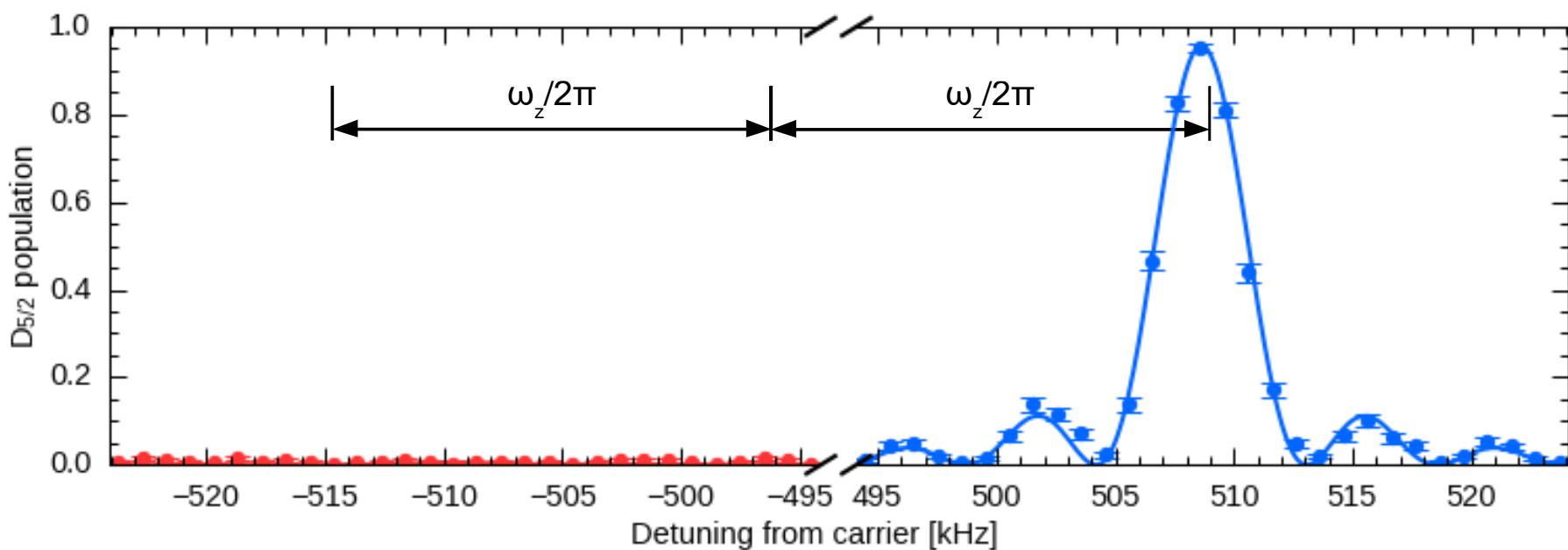
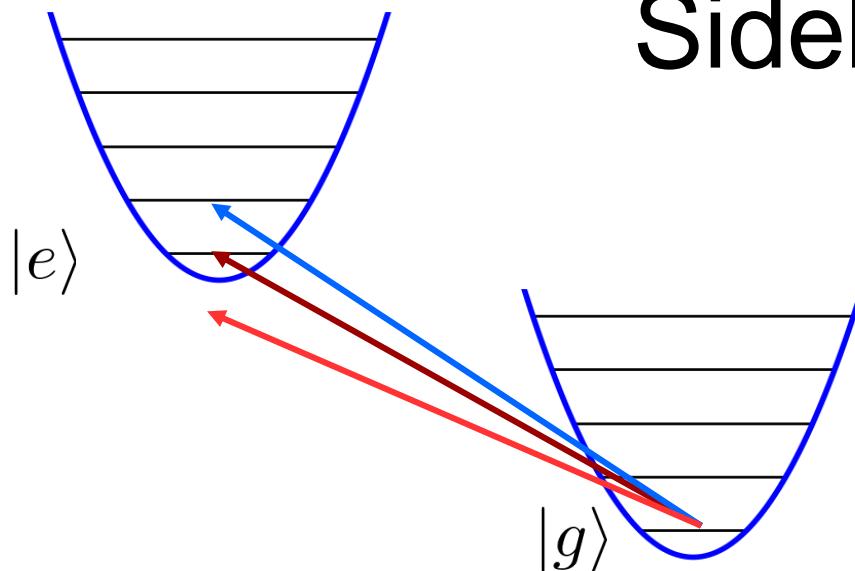
DC supply



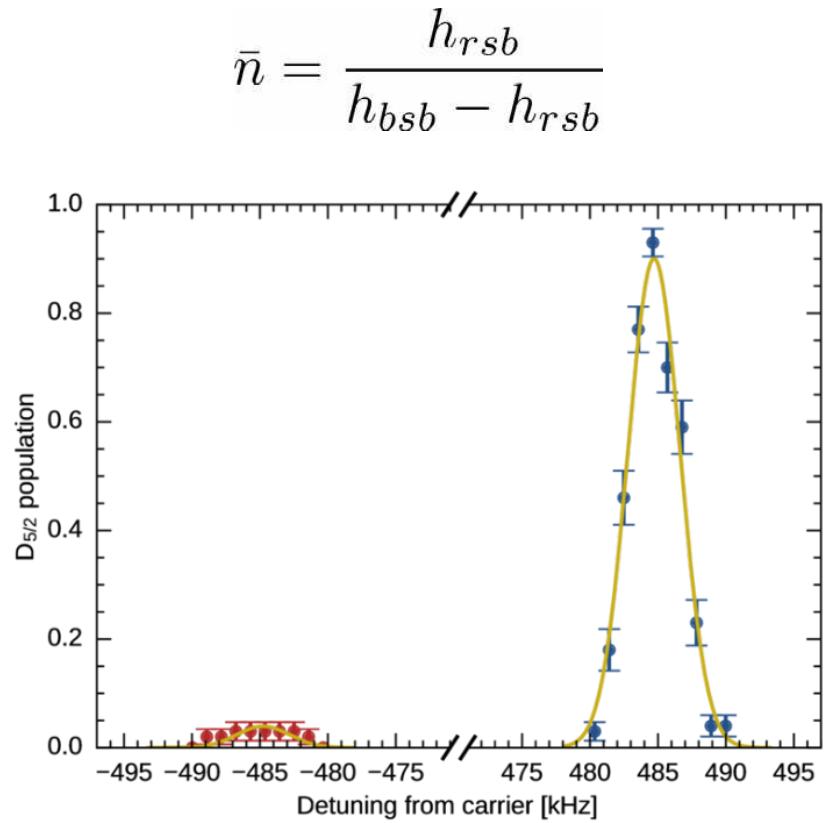
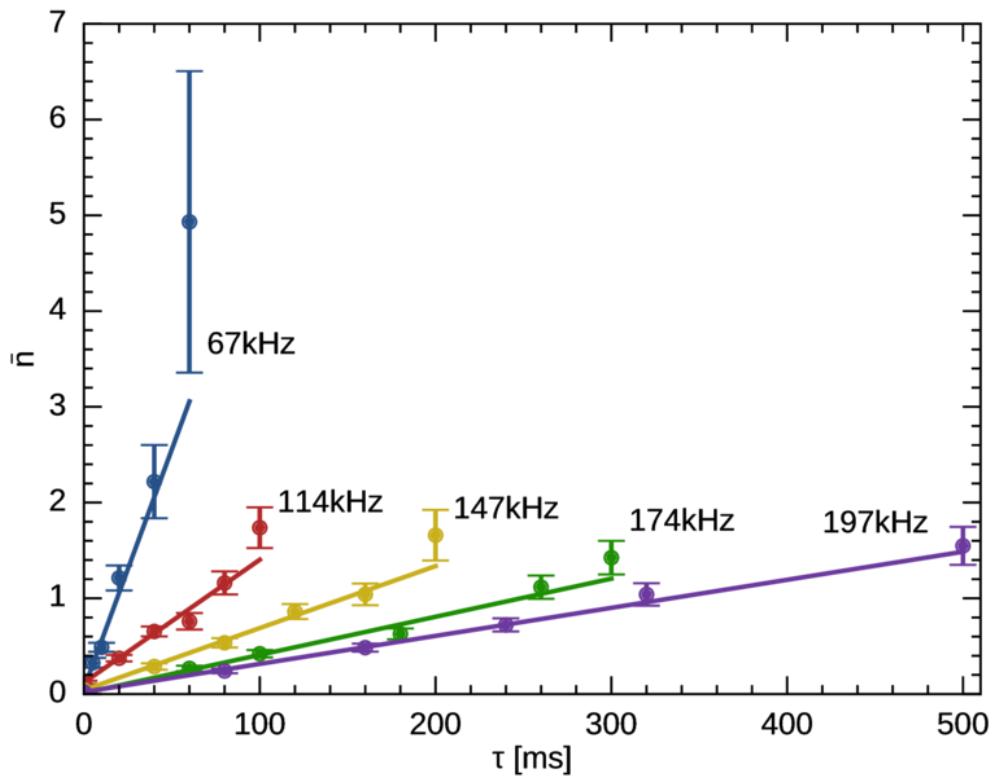
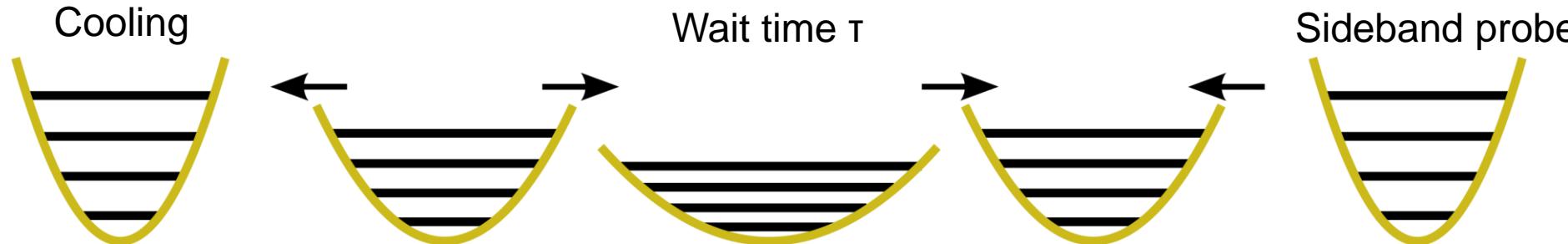
Sidebands



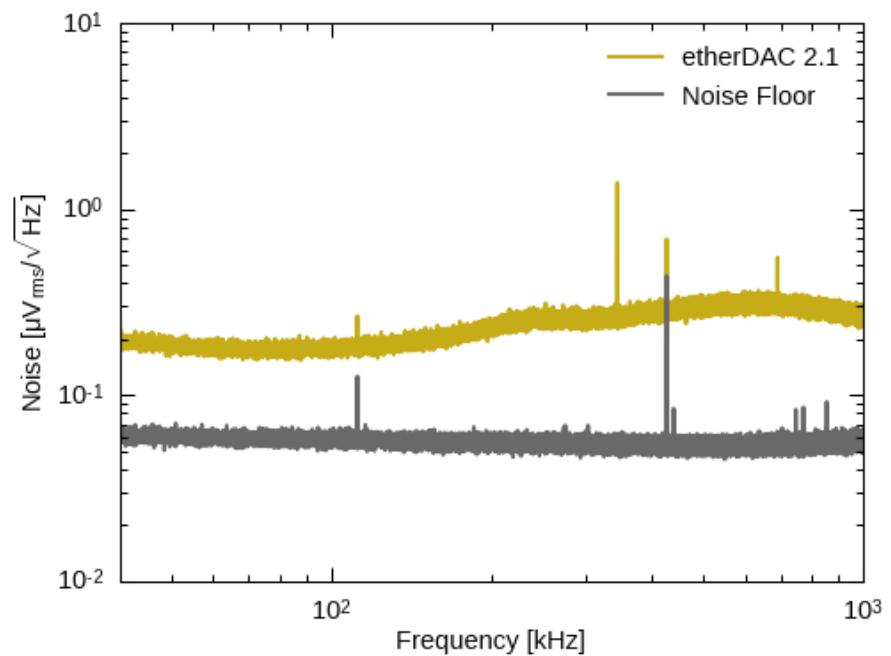
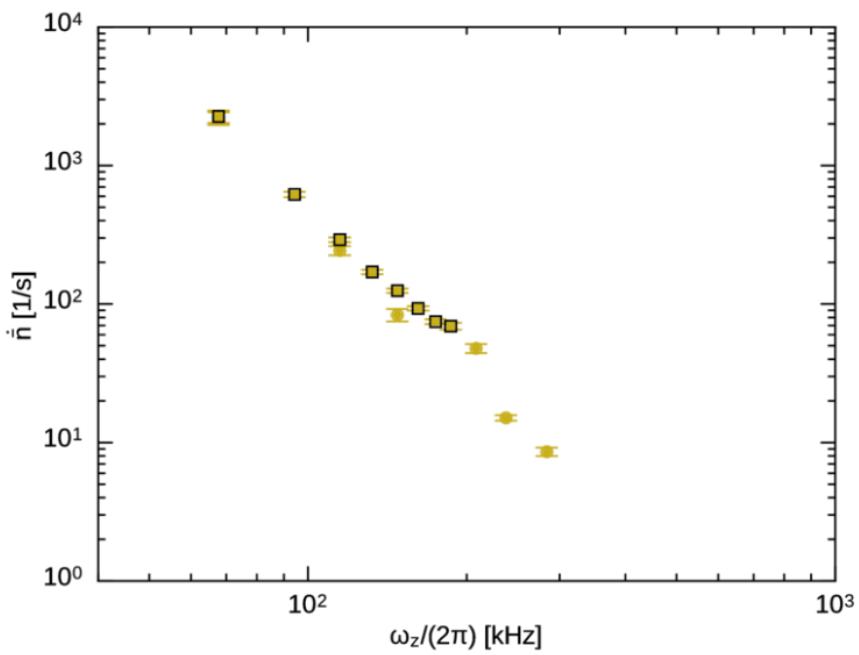
Sidebands



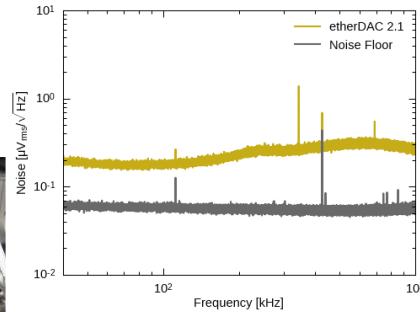
Heating rates



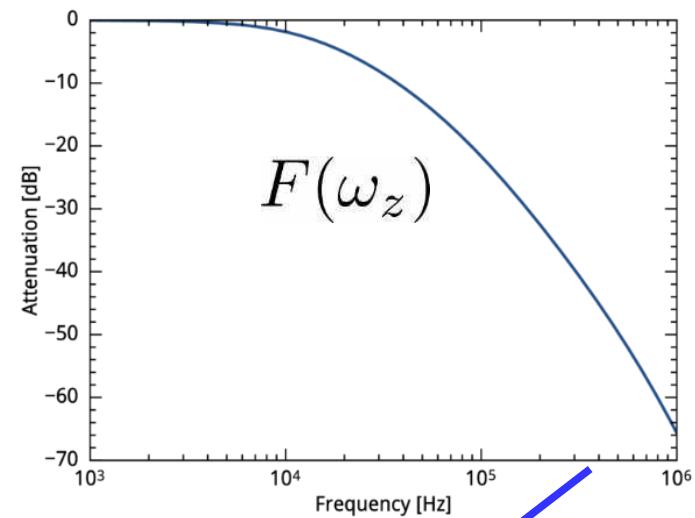
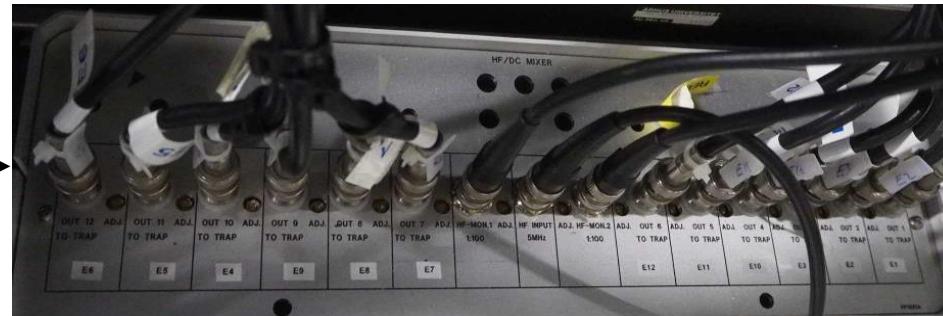
Heating rates of a single $^{40}\text{Ca}^+$



$$\sqrt{S_{V_{DC}}(\omega_z)}$$



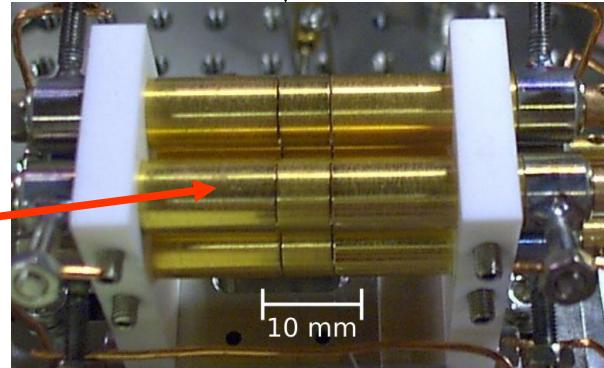
DC Supply



RF/DC Mixer

$$D = 56 \text{ mm}$$

$$S_V(\omega_z)$$

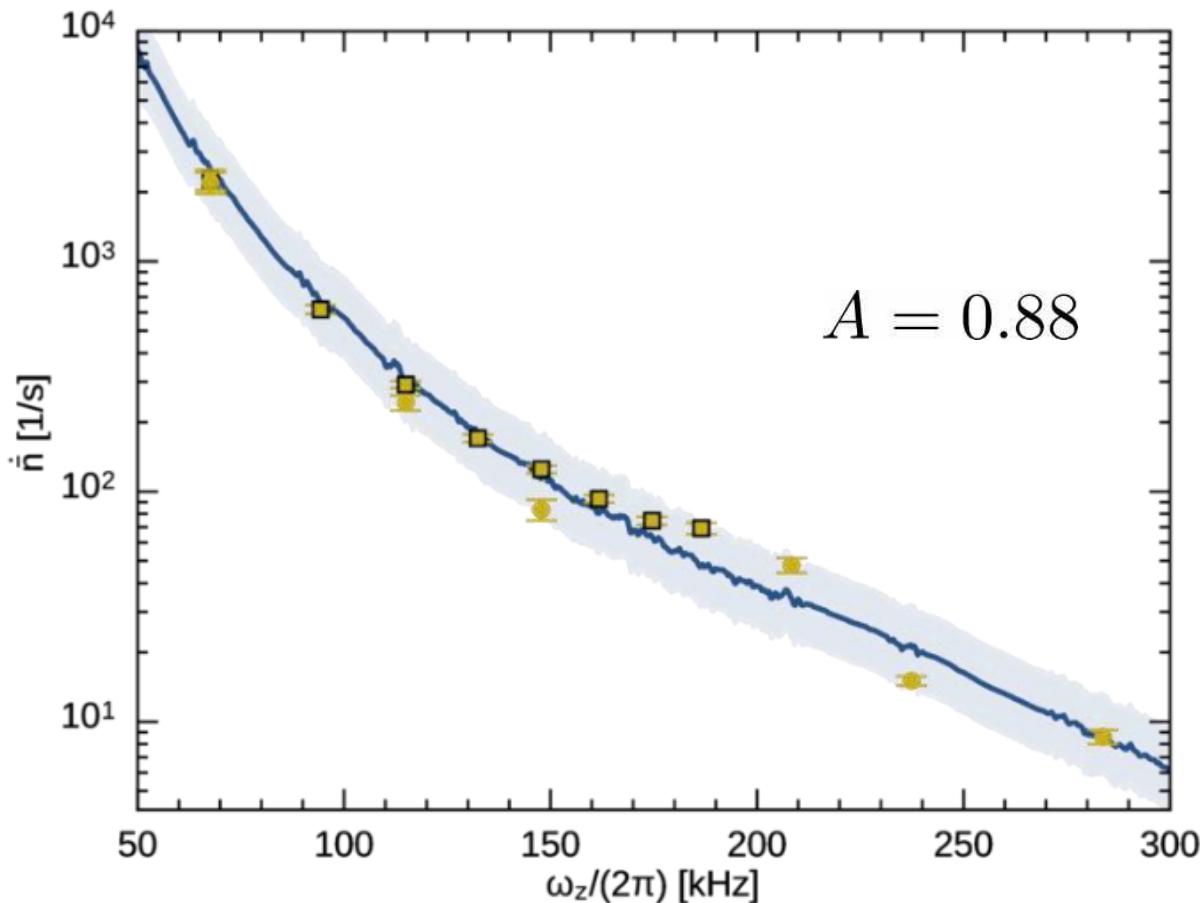


$$\dot{n} \simeq \frac{e^2}{4m\hbar\omega_z} S_E(\omega_z)$$

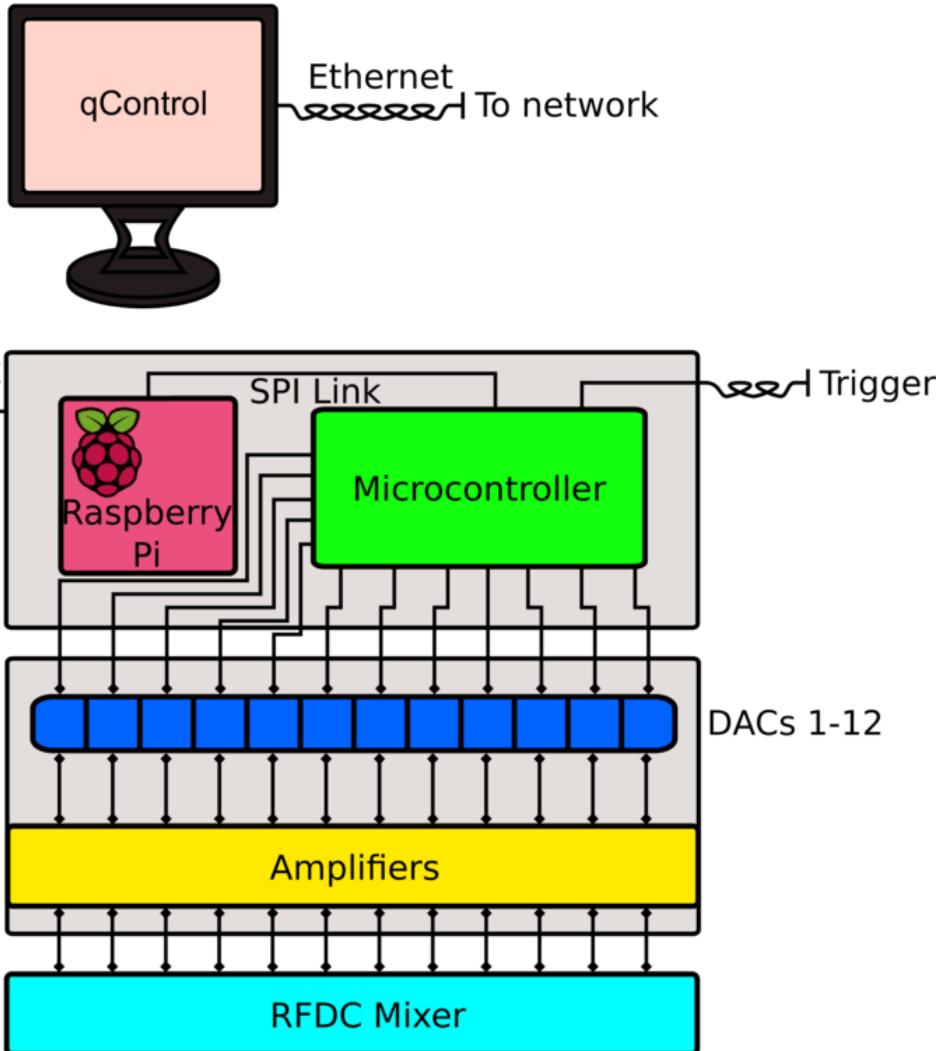
$\rightarrow z$

Heating rate model – single ion

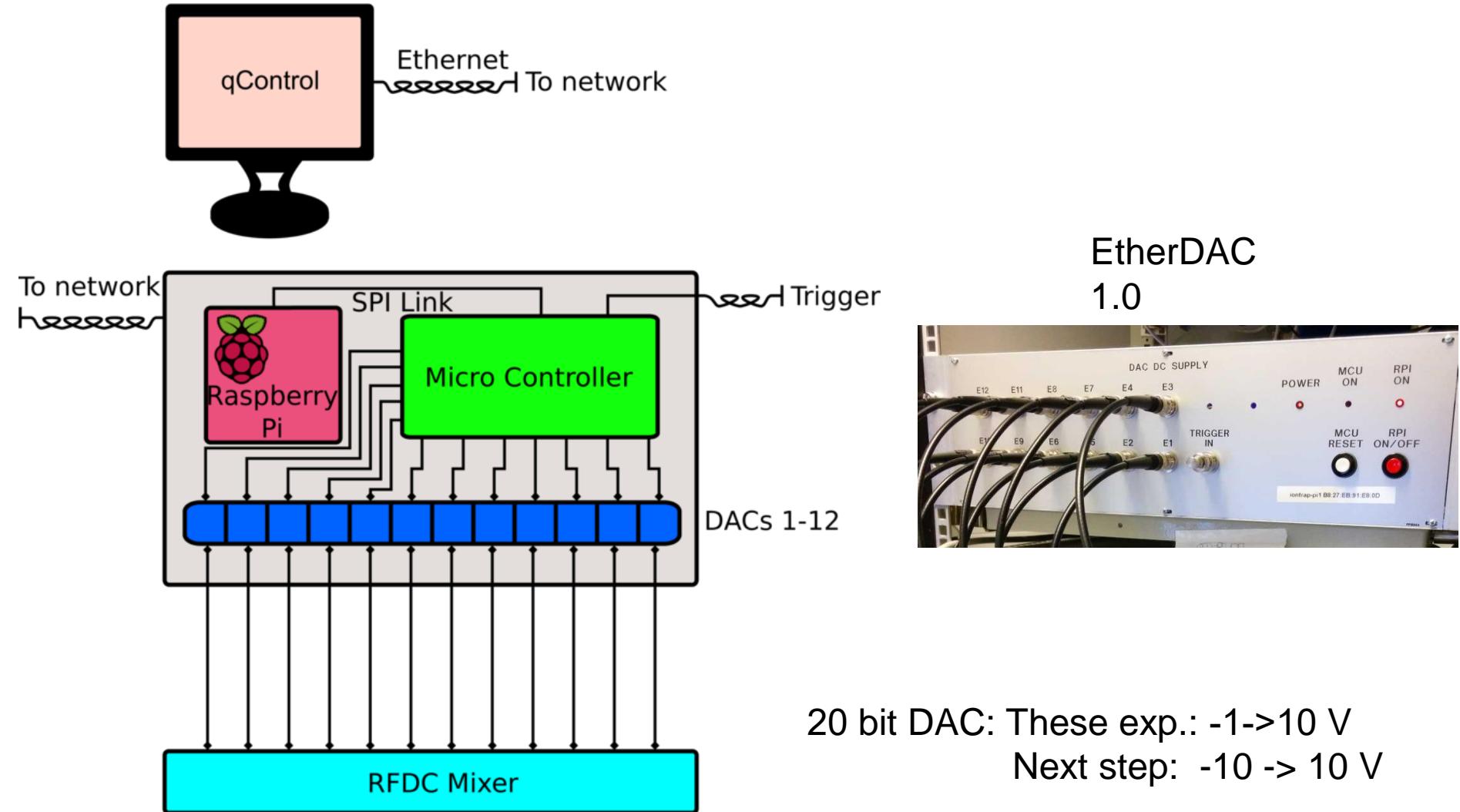
$$\dot{n} \simeq 8 \frac{e^2}{4m\hbar\omega_z} F(\omega_z)^2 \frac{S_{VDC}(\omega_z)}{D^2}$$



DC supply

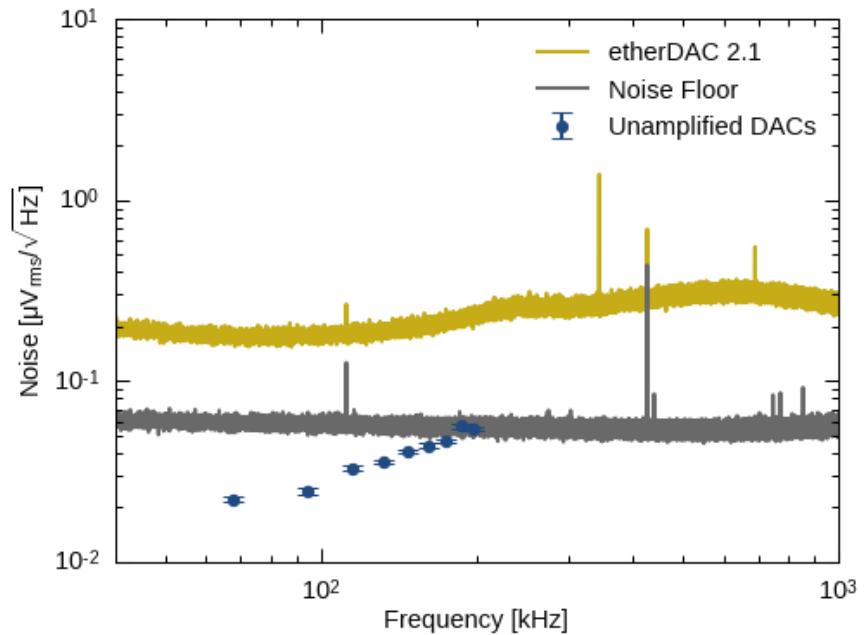
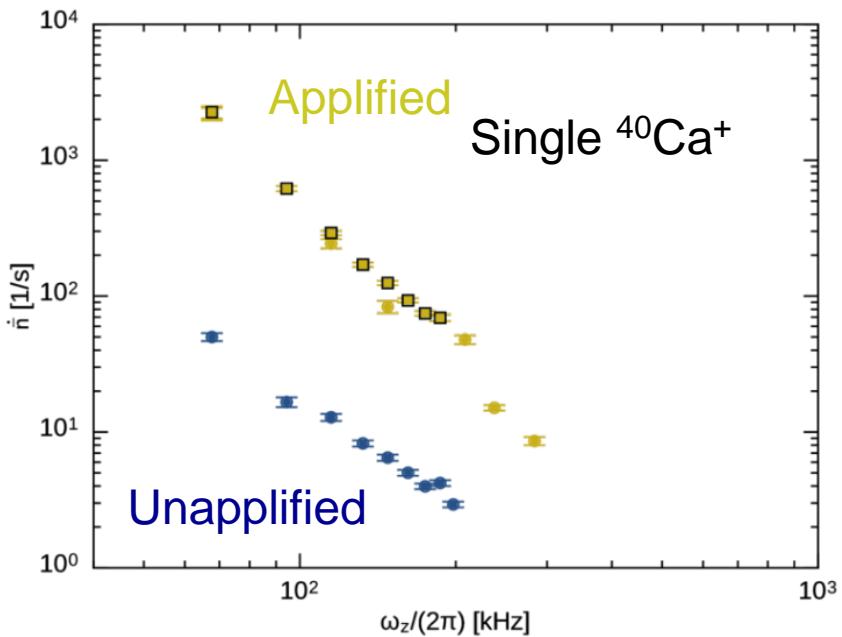


DC supply

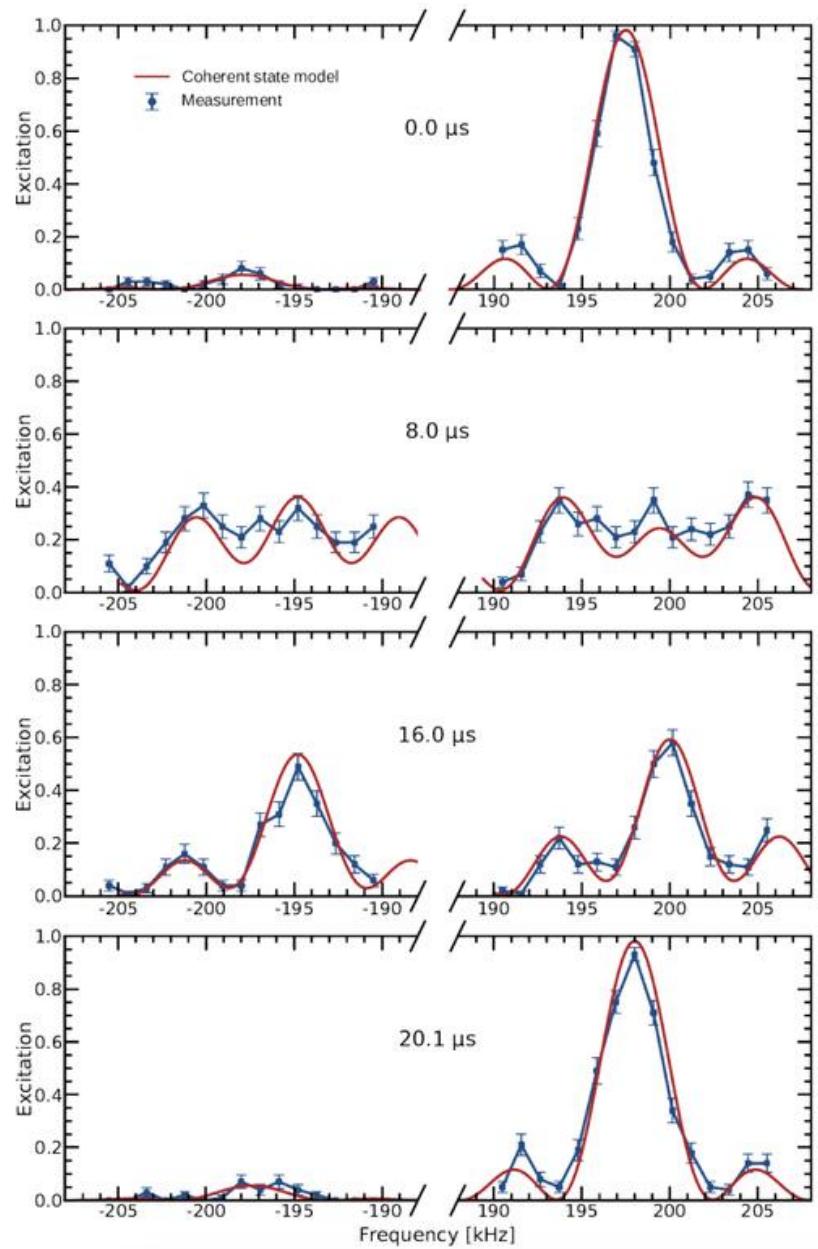


Heating rates with unamplified (DAC) supply

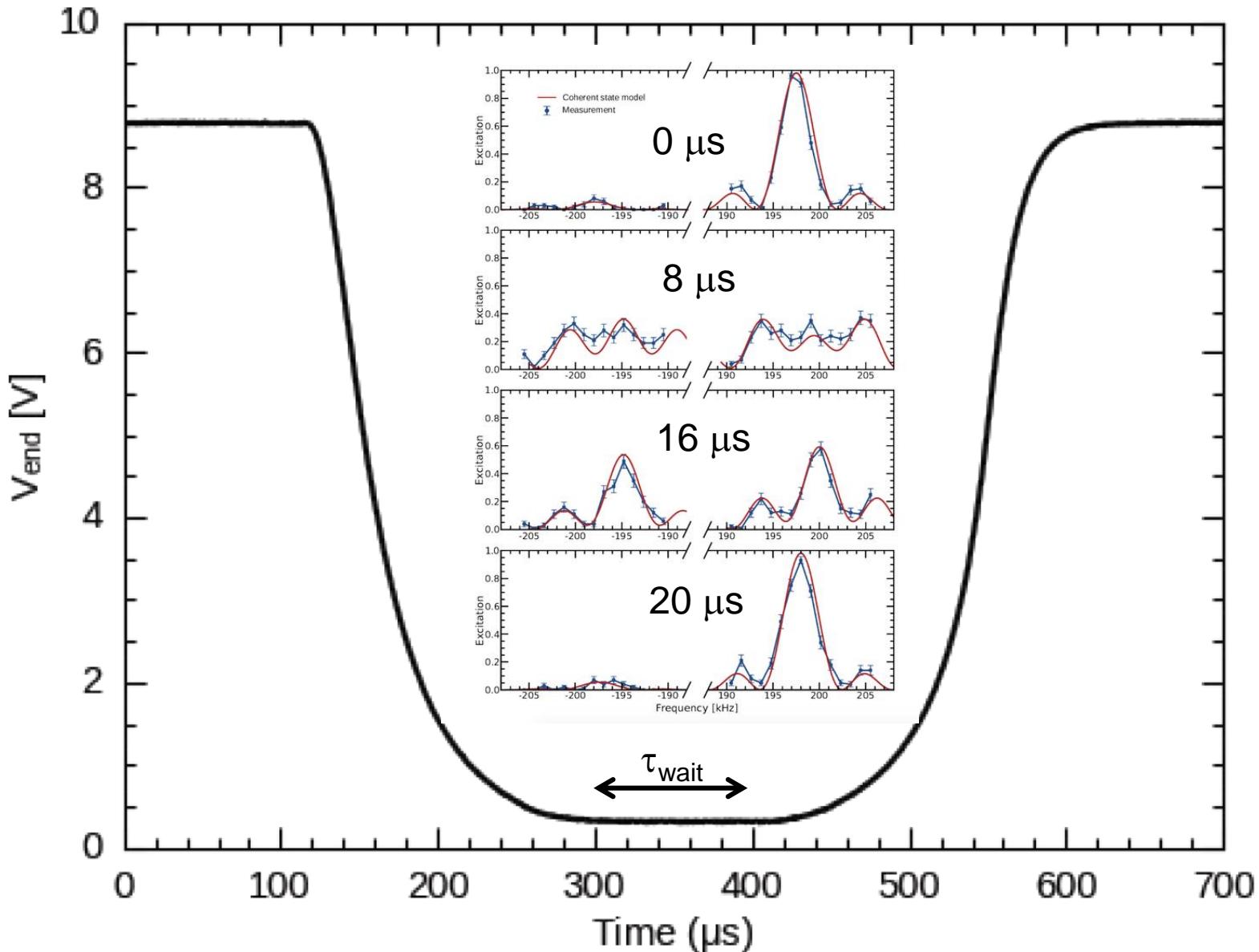
$$\dot{n} \simeq A \times 8 \frac{e^2}{4m\hbar\omega_z} F(\omega_z)^2 \frac{S_{V_{DC}}(\omega_z)}{D^2}$$



~20 times lower heating!



Motional kicks due to ramping



'Design and Realization of the TEQ experiment' meeting

Part I – Project Management

Southampton – 22nd June 2018

MINUTES

1. Welcome to the participants by Angelo Bassi, Chair. The members present at the Meeting are:

James Bain (M2)
Peter Barker (UCL)
Angelo Bassi (UniTs)
Massimiliano Bazzi (INFN)
Matteo Carlesso (UniTs)
Catalina Curceanu (INFN)
Luca De Trizio (TUD)
Michael Drewsen (AU)
Alessandro Ferraro (QUB)
Giulio Gasbarri (UniTs)
Oussama Houhou (QUB)
Marta Marchese (QUB)
Mauro Paternostro (QUB)
Thomas Penny (UCL)
Antonio Pontin (UCL)
Anishur Rahman (UCL)
Muddassar Rashid (UoS)
Ashley Setter (UoS)
Christopher Timberlake (UoS)
Marko Toros (UoS)
Hendrik Ulbricht (UoS)
Andrea Vinante (UoS)

2. Next Steering Committee Meeting
-

The Chair, in agreement with the partner TU Delft, proposes to hold the Next Steering Committee Meeting on 8-9 November 2018 in Delft. The partners agree with date and place and confirm their presence.

The Chair presents the tentative agenda for the Next Steering Committee Meeting:

Tentative agenda

Management (1/2 day):

- Monitoring of milestones/deliverables
- Discussion of critical issues (if any)
- Preparation for the review meeting

Science: Theory and Experimental Discussion

Workshop: to be defined

The agenda will be finalized in the next months.

3. Review Meeting

The Steering Committee members present at the meeting discuss the date to propose to the PO for the first Review Meeting.

According to the latest message of the PO to the PI and to the project timing, the meeting has to take place in the second half of February 2019.

The proposed dates for the Review Meeting are: **February 26 or 27, 2019**. A decision will be made between the PO and the PI. The PI reminds what was discussed at the Kick-off Meeting:

- "- The PI of every unit should be present.
- The day before the meeting a "rehearsal" will take place."

[From the minutes of the Kick-Off Meeting]

The Steering Committee members discuss the place to propose to the PO for the first Review Meeting.

According to the latest message of the PO to the PI, the SC "[...] could have the meeting at one of the partners sites in case there is experiment/equipment/physical results to be shown to the monitors to help them with their assessment on the work".

The SC members unanimously decide to propose to the PO to hold the Review Meeting in Brussels. Other venues will be taken into consideration for the other Review Meetings (M30 and M48).

The Steering Committee discuss the name of the monitors to propose to the PO for the first Review Meeting. The PO has asked for 9 names in three areas. The list of names which will be proposed to the PO includes:

a. Quantum mechanics/foundations:

Chiara Macchiavello (Pavia University, Italy)
Christiane Koch (Kassel, Germany)
Adrian Kent (Cambridge, UK)
Ward Struyve (KU Leuven, Belgium)

b. Optomechanics: Theory

Alexia Auffeves (Grenoble, France)
Radim Filip (Olomouc, Check Republic)
Vittorio Giovannetti (SNS Pisa, Italy)

c. Optomechanics: Experiments

Romain Quidant (ICFO Spain)
Lukas Novotny (ETH Zurich Switzerland)
Tracy Northrup (University of Innsbruck Austria)

The PI presents the tentative agenda for the Review Meeting, as per last message of the PO:

9:00 – 9:15	R. Borissov (chair)	Introduction, tour du table
9:15 – 9:45		Overview by the coordinator
9:45 – 10:30		WP 1
<i>Coffee (10:30 to 11:00)</i>		
11:00 – 11:45		WP 2
11:45 – 12:30		WP 3
<i>Lunch (12:30 to 13:30)</i>		
13:30 – 14:15		WP 4
14:15 – 14:30		WP 6 (management)
14:30 – 14:45		WP 7 (dissemination)
14:45 – 15:15		Financial data
15:15 – 15:45		Innovation potential discussion
15:45 – 16:15	<i>General discussion</i>	
16:15 – 16:45	<i>Assessment preparation by monitors and PO</i>	
16:45 – 17:00	R. Borissov	Closing

4. Closing

Angelo Bassi, Chair, wraps up the discussion on management issues and gives the word to the other speakers for the scientific discussion.